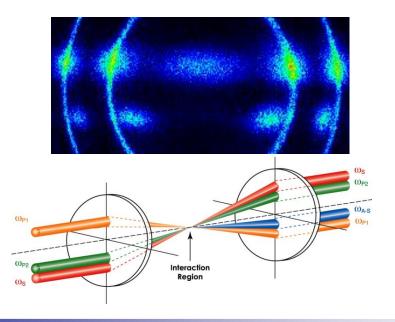
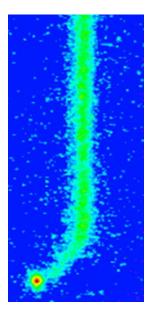


https://ntrs.nasa.gov/search.jsp?R=20170002218 2019-04-29T08:23:40+00:00Z Molecular-Based Optical Diagnostics for **Hypersonic Nonequilibrium Flows**



Paul Danehy and Brett Bathel, NASA Langley Research Center, Virginia, USA Craig Johansen, The University of Calgary, Canada Michael Winter, University of Kentucky, Kentucky, USA Sean O'Byrne, University of New South Wales Canberra, Canberra, Australia Andrew Cutler, The George Washington University, USA





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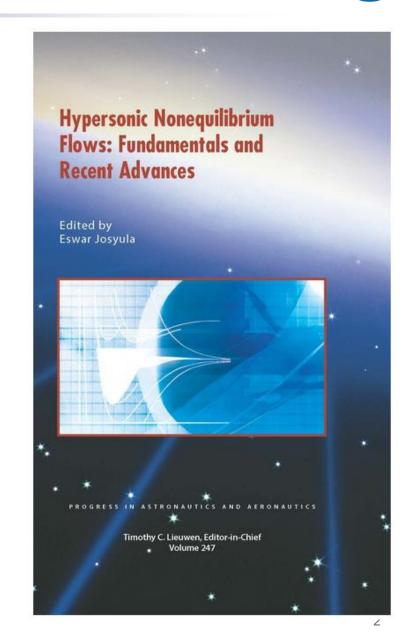


"Paul, Why are you doing this special session?"



Multi-purpose:

- Educate those new to field of laser based measurements (students)
- Let collaborators from other fields know what is possible to measure
- Provide some updates and ideas for those already working in measurement technology
- Special session is coordinated with the launch of a new AIAA Progress Series Book
 - Pedagogical treatment
 - Came out of a Fluids TC Working group led by E. Josyula
 - Our chapter: Molecular-Based
 Optical Diagnostics for Hypersonic
 Nonequilibrium Flows





AIAA Progress Series Book, May, 2015



HYPERSONIC NONEQUILIBRIUM FLOWS: FUNDAMENTALS AND RECENT ADVANCES





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Hypersonic Nonequilibrium Flows: Fundamentals and Recent Advances

Eswar Josyula, U.S. Air Force Research Laboratory, Wright-Patterson Air Force Base, Ohio

eISBN: 978-1-62410-329-2 print ISBN: 978-1-62410-328-5 DOI: 10.2514/4.103292

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About the Book

The high-temperature environment poses an unusual challenge in understanding the basic physics of hypersonic flight. A lack of such understanding can lead to risks and uncertainties in the design of aerospace vehicles. *Hypersonic Nonequilibrium Flows* documents recent, unprecedented scientific advances in the field of nonequilibrium processes for aerospace applications. These advances have been driven primarily by interest in space access and exploration, or in developing military technologies involving hypersonic flight regimes.

In the modeling of hypersonic flows, the last decade has witnessed a reexamination of fundamental principles of kinetic theory and quantum chemistry to describe the kinetic and thermal states, respectively, of the individual gas particles. Modern aerospace programs where nonequilibrium energy transfer processes play a major role may broadly be categorized as exo- and endo-atmospheric. The exo-atmospheric flight programs consist of Earth and planetary reentry programs, as well as access to space programs for applications that include space exploration, flight experiments and demonstrations, missile defense, and the nascent space tourism industry. The endo-atmospheric flight programs are primarily motivated by hypersonic military applications requiring high-precision engagement for tactical, theater and strategic defense, as well as applications involving intelligence, surveillance, and reconnaissance.

The nonequilibrium processes considered in this volume are generally associated with flight Mach numbers between 7 and 25, where the shock-layer temperatures range from 3000 to 25,000 K.

Hypersonic Nonequilibrium Flows includes fundamental governing equations of nonequilibrium fluid transport and computational approach to calculation of rates and cross-sections in quantized energy states; DSMC approach; radiative heat transfer; a CFD perspective; surface chemistry, with additional chapters on high enthalpy facilities and the associated diagnostic techniques.

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Hypersonic Nonequilibrium Flows: Fundamentals and Recent Advances



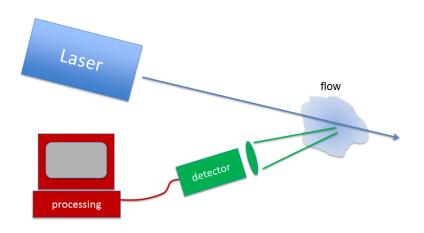
Edited by Eswar Josyula

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- 1. Fundamental Fluid Transport Equations for Hypersonic Nonequilibrium Flows, Eswar Josyula, Prakash Vedula
- 2. Computation of Hypersonic Nonequilibrium Flows using the Direct Simulation Monte Carlo Method, <u>lain D. Boyd</u>
- 3. First Principles Calculation of Heavy Particle Rate Coefficients, Richard L. Jaffe, David W. Schwenke, Marco Panesi
- 4. Radiation from Hypersonic Bodies—A Window on Non-Equilibrium Processes, **Deborah A. Levin**
- 5. CFD Methods for Hypersonic Flows and Aerothermodynamics, Graham V. Candler, Pramod K. Subbareddy, Ioannis Nompelis
- 6. Surface Chemistry in Non-Equilibrium Flows, Jochen Marschall, Matthew MacLean, Paul E. Norman, Thomas E. Schwartzentruber
- 7. High-Enthalpy Facilities and Plasma Wind Tunnels for Aerothermodynamics Ground Testing, Olivier Chazot, Francesco Panerai
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Introduction and Application Considerations for Optical Diagnostics in Hypersonic Nonequilibrium Flows

Paul Danehy and Brett Bathel, NASA Langley Research Center, Virginia, USA
Craig Johansen, The University of Calgary, Canada
Michael Winter, University of Kentucky, Kentucky, USA
Sean O'Byrne, University of New South Wales Canberra, Canberra, Australia
Andrew Cutler & Samantha Hurley, The George Washington University, USA













Outline for 1st Talk



Introduction and Application Considerations for Optical Diagnostics in Hypersonic Nonequilibrium Flows

- Temperature, equilibrium and nonequilibrium
- Characteristics of hypersonic nonequilibrium flow
 - What needs measuring?
- Advantages of spectroscopic measurement
- Aspects of a good measurement technique
- Choosing which measurement technique to use.



Temperature and Equilibrium

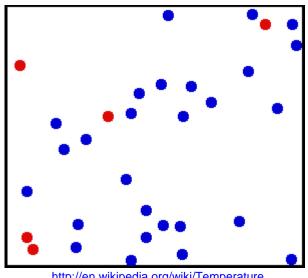


Temperature

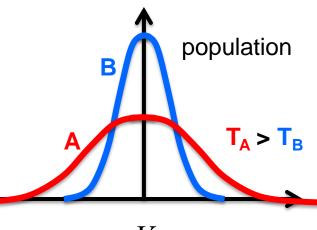
- Classical thermodynamics
 - Heat flowing from object A to B $\rightarrow T_A > T_B$
- Statistical thermodynamics
 - Describe by Boltzmann distribution
 - e.g. Maxwellian Velocity Distribution width $\sim \sqrt{T}$

Equilibrium

- Classical thermodynamics
 - Thermal equilibrium: $T_A = T_B$
- Statistical thermodynamics
 - One temperature can describe all the different <u>energy modes</u> (via Boltzmann)
- Chemical equilibrium:
 - Reactants and product concentrations don't further change with time



http://en.wikipedia.org/wiki/Temperature Greg L at the English language Wikipedia



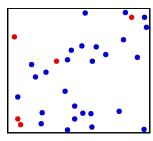
 V_{z}



Energy Modes



Translation



Rotation

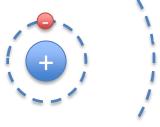


All these states are quantized! 1, 2, 3, ...

Vibration



Electronic



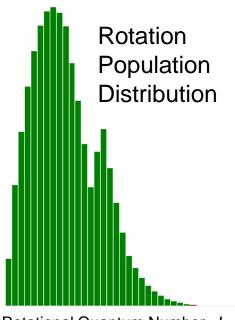
- These can all be described by a temperature:
 - $-T_{trans}$, T_{rot} , T_{vib} , T_{elec}
 - Thermal equilibrium: these T's are all equal



Nonequilibrium



- Thermal Nonequilibrium:
 - Different energy modes described by different T's
 - e.g.: $T_{rot} \neq T_{vib}$
 - Or, the distribution of population can't be described by Maxwell-Boltzmann statistics ("non-thermal" distribution)
- Chemical Nonequilibrium:
 - Products and reactants are in a state of change
 - If held at those conditions (P, T) the composition will change.
- Equilibrium occurs via collisions



Rotational Quantum Number, *J*Computed using LIFBASE
(J. Luque, SRI International)



Hypersonic Flows and Noneq.



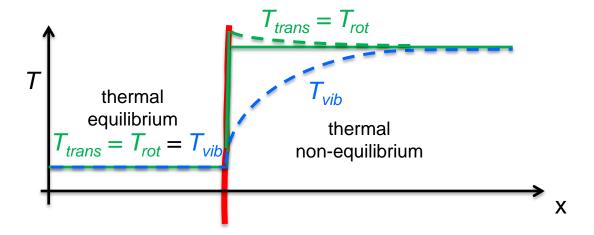
- Hypersonic vehicles fly at high altitude (low P) and high speed (M > 5) resulting in gas and vehicle heating (high T)
 - Collisions rate scales as P/\sqrt{T}
 - Low collision rate causes nonequilbrium
 - At STP for O₂: Trans: 10; Rot: 10; Vib: 20,000;
 Dissoc: 200,000 collisions to equilibrate!
 - 10 coll. ~ 1 ns; 20,000 coll. ~ 2 μs at STP
- Hypersonic flows are also characterized by:
 - Steep gradients (shocks, boundary layers, expansions)
 - Combustion (in scramjets)
 - Dissociation / recombination



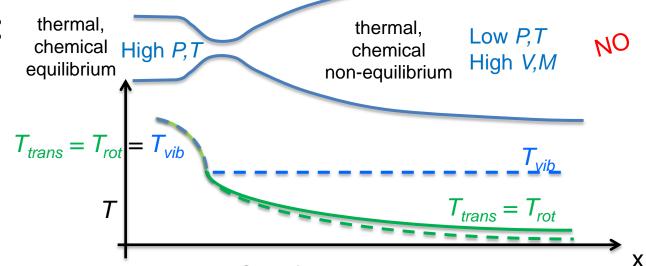
Some Hypersonic Nonequilibrium Flows



Shock wave:



Expansion:



We can measure, quantify these!



Parameters to measure



- Typical parameters of interest in Hypersonic Nonequilibrium Flows:
 - Velocity, Pressure, Density, Temperatures, Species
 - Non-thermal population distributions
 - How is energy in flow partitioned in terms of:
 - thermal energy (T)
 - chemical energy (species) and
 - kinetic energy (V)?

(O and N atom LIF at NASA ARC)



Some advantages of Spectroscopic Measurement Techniques



- Non-intrusive
 - No probes, particles perturb the flow
- Remote detection
 - Can be used in hostile environments

- Can measure multiple parameters, states:
 - Sometimes simultaneously
 - Can be instantaneous (<10 ns) and high freq. (MHz)
 - Can be precise, accurate, high spatial res. (2D, 3D)
- But... No one measurement technique can meet all requirements
 - Can have more complicated theory, expensive and complex equipment, more difficult data analysis
 - May require seeding of (sometimes toxic) gases,
 more expertise, slower data acquisition, analysis



Scope of the Content



- Content focuses on molecular based, quantitative, mostly spectroscopic measurement techniques previously applied in or <u>may be applicable to</u> nonequilibrium flows. Many examples in equilibrium.
 - Content of lectures and manuscript are not exhaustive. Not all the 'first' or 'most important' references are given. Instead they there is an emphasis on describing how the techniques work and how they can be used to measure.
 - Also there is an admitted bias towards the authors' own work.
- Content <u>excludes</u> the many relevant particle-based (PIV, LDV), probe-based and surface-based measurement techniques that could be used to study non-equilibrium flows; mostly no 'flow vis'. (No schlieren.)



What makes a good measurement technique?



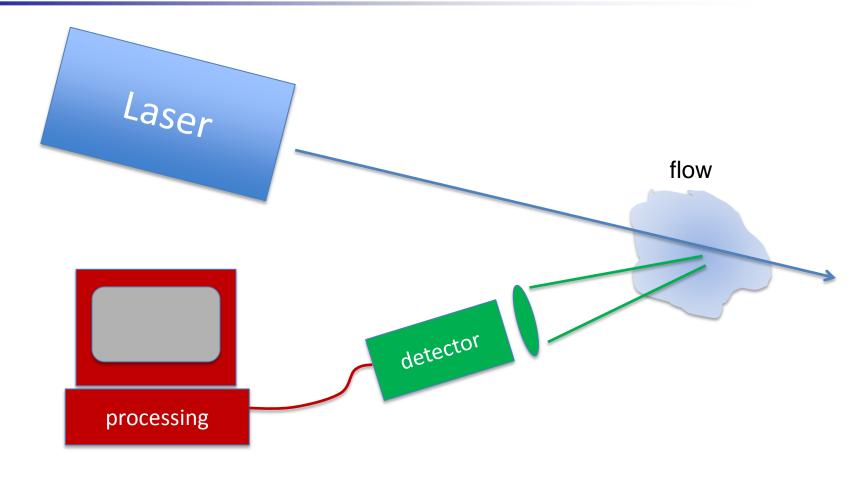
A reliable <u>measurement system</u>
 matched with <u>well-understood physics</u>
 to make a <u>quantified measurement</u>
 that meets a <u>customer's requirements</u>.

Explore each of these...



Typical Measurement System





- Need to understand equipment and physics of process to make a measurement
 - Emission, Abs., LIF, Rayleigh, Raman, CARS, etc.



Measurement System: Lasers

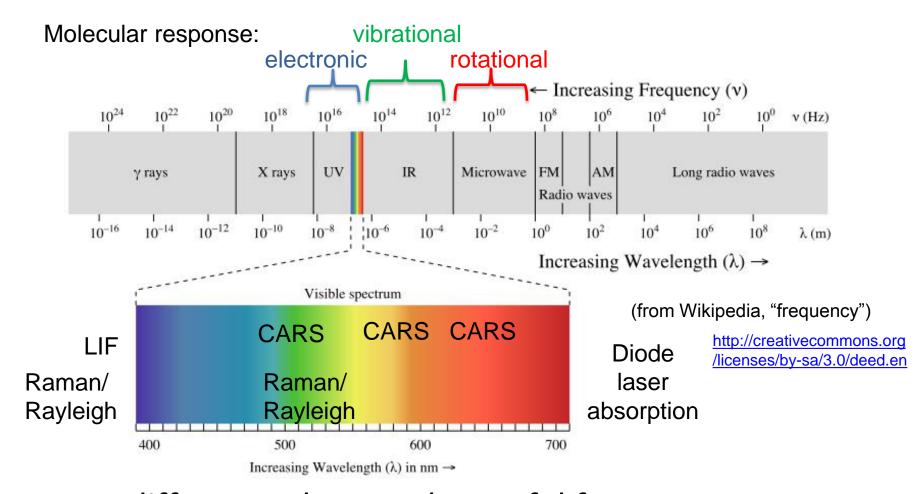


- <u>Lasers</u>: pulsed vs. continuous wave (cw)
 - Continuous wave: lower power (mW to Watt)
 - Pulsed:
 - 10 ns, picosecond, femtosecond all commercially available
 - 'Freeze' the flow
 - Much higher power vs cw (MWatt-GWatt, even TWatt)
 - Frequency conversion (useful in linear techniques such as Raman, Rayleigh, LIF)
 - Provide high powers for nonlinear techniques (CARS)
 - Repetition rate: 10-100 Hz, 16 kHz, 1 MHz, 80 MHz...
- What colors of laser light do we need?



Colors of Light: Spectroscopy





- Many different colors can be useful for spectroscopy
- As energy increases, more modes can be excited
 - LIF: can see electronic, vibrational and rotational structure



Measurement System 2

Laser



Detectors:

- Single point detectors:
 Photomultipler tubes (PMT) and photodiodes
- Camera technology is rapidly evolving:
 - CCDs provide 'scientific grade' (low noise, linear, etc.)
 - CMOS cameras are faster
 - Commercially available cameras at up to 10's, 100's of kHz steady streaming or MHz for short bursts or few pix
- Fiber optics and fiber-optic bundles often used for either transmitting laser or collecting signal

Processing:

 Some data processing codes are available (CARSFT, LIFBASE) but many are proprietary.



What makes a good measurement technique?



• A reliable measurement system matched with well-understood physics skip to make a quantified measurement that meets a customer's requirements.

Explore each of these...



Quantified Measurements



- Accuracy and precision of a measurement must be quantified to be useful, for example when comparing to a code
 - Qualitative measurements (flow vis) can be useful
- Quantified measurement:
 - Accuracy and precision are well characterized



Accurate but not precise



Precise but not accurate

(from Wikipedia, "accuracy and precision")

- Accuracy: compared to a 'standard' or 'accepted'
- Precision: 1σ of large sample of measurements
 - Averaging reduces precision's contribution to uncertainty
 - High precision required to quantify fluctuations (turbulence)



Customer Requirements



Interview the customer... (sometime the customer is you!)

- Simultaneous measurements to obtain correlations: T'u', ρu'v'
- Time resolution ($< \mu sec$), and frequency response (> MHz)
- Spatial resolution: near walls; smallest scales in shear layer
- Where are the measurement to be made?
 - Inflow to establish B.C., exit, near walls?
 - Point, line, plane, volume?
- Accuracy and precision requirement?
- What quantity of data is required? Uncertainty required?
- When is the data needed? Is "real-time" data required?
- What type of optical access is available?
- Can (toxic) seed gases be introduced? Will they influence the properties being measured? Can particles be used?
- What is the ordered priority of the above requirements?



What makes a good measurement technique?



A reliable <u>measurement system</u>
 matched with <u>well-understood physics</u>
 to make a <u>quantified measurement</u>
 that meets a <u>customer's requirements</u>.



- Now the lectures will focus on different measurement systems, introducing the physics.
 - How's the basic physics of the method work?
 - Can the measurements be made instantaneously (aka. single-shot) at high frequencies?
 - What accuracy and precision can be obtained?



Customer Requirements



- Consider a customer with arbitrary measurement requirements:
 - Would like a particular parameter measured
 - Would like the measurement at some conditions (P, T)
 - Many measurement technique signals scale as P_{static} , T_{static}
- Parameters to be measured:
 - Velocity, temperature, density, pressure, species (concentration or mole fraction)
- Can base choice of measurement technique (in part) on prior success by others:
 - We compiled past work into graphics that show static pressure and temperature of demonstrated measurements
 - Use these charts to find appropriate measurement methods





Backup Charts



Explanation of Parameter Charts



Overview:

This appendix shows the <u>static conditions</u> (temperature and pressure) at which various measurement techniques have been successfully demonstrated. When planning a new experiment to occur at a specified temperature and pressure, these graphs might be useful to see what measurements have previously been demonstrated at those conditions. The numerals used as data points indicate the reference in the attached reference list. The different measurement techniques are denoted by the colors indicated. Pressure is plotted on a logarithmic axis while temperature is on a linear axis.

Caveats:

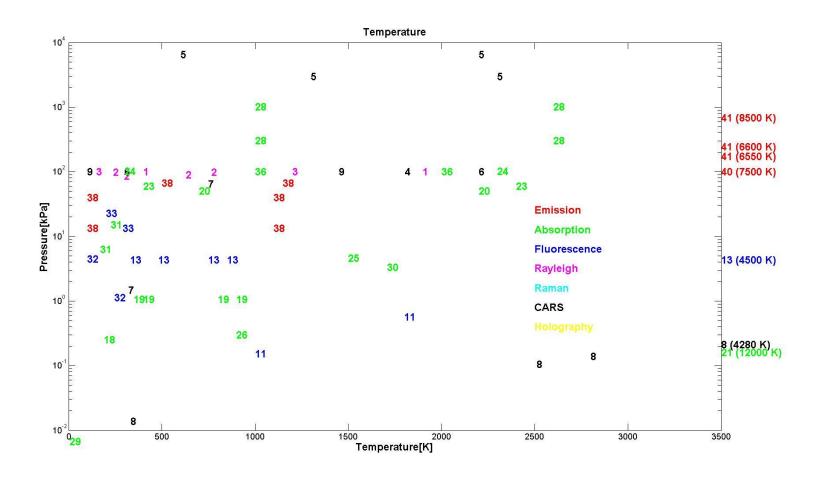
- The data includes both references contained in the manuscript as well as additional works.
- The reference numbers in the manuscript are different from those in this appendix.
- This study is not meant to be exhaustive; it provides a partial sampling of the data available in the literature.
- Some data points overlap. This is particularly true at room temperature and atmospheric pressure. Some data has been omitted to avoid overlaps.
- For temperatures greater than 3500 K, the reference number is plotted to the right of the chart with the static temperature in parentheses.
- "Species" includes either species concentrations or species mole fraction measurements.

(Not included in AIAA Progress Series manuscript)



Temperature

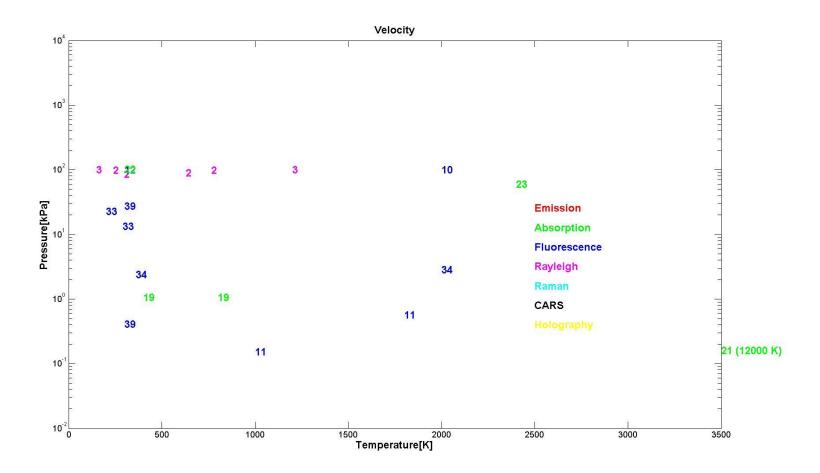






Velocity

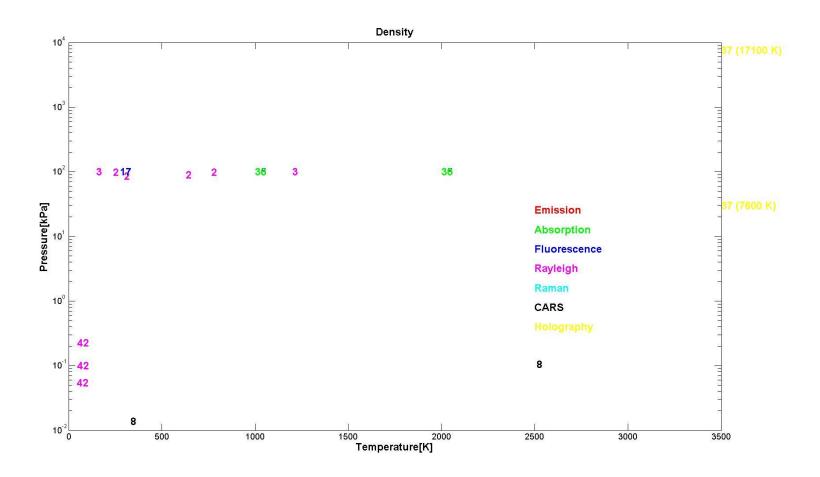






Density

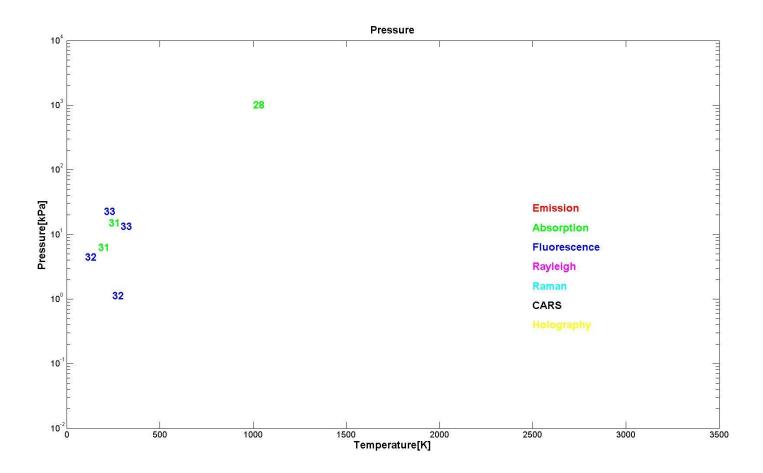






Pressure

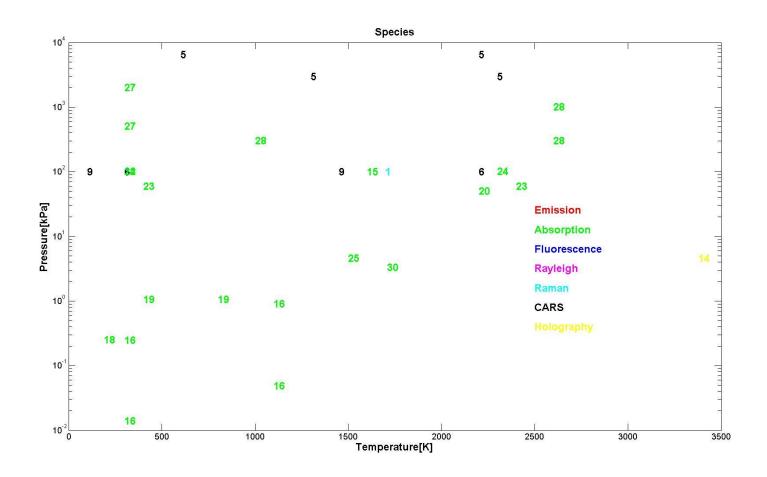






Species







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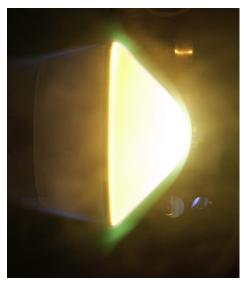
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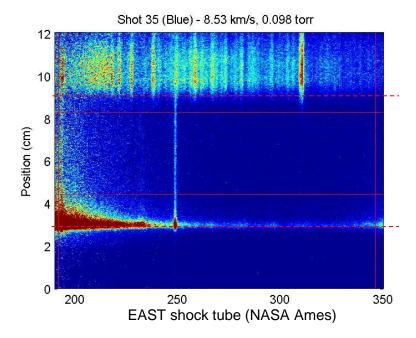
Intro to Optical Emission Spectroscopy for Hypersonic Nonequilibrium Flows



Michael Winter, University of Kentucky, Kentucky, USA Paul Danehy, NASA Langley Research Center, Virginia, USA



PICA at NASA Ames (SPRITE)





Intro to Optical Emission Spectroscopy for Hypersonic Nonequilibrium Flows



Outline:

- Introduction to emission spectroscopy
- Excitation of Atoms and Molecules (electronic, vibrational, rotational)
- Line broadening
- Spatial resolution
- Application examples of emission spectroscopy



Applications of emission spectroscopy



- Astronomy !!! composition and velocity of celestial bodies
- Diagnostics for gases at high temperatures
 - re-entry (ground test and flight)
 - electric propulsion characterization
 - plasma processing (coating, edging, ...)
 - combustion (though temperatures might be too low)
 - material analysis (laser ablation of surface material → radiation)
- Radiation transport in gases at high temperatures
 - re-entry radiation heat flux to the spacecraft (ground test and flight)
 - radiation transport within the flow field (source term in energy equation)
 - → particular importance of VUV radiation

Goals:

- Identification of elements
- Radiation heat flux determination
- Temperature determination
 - ratios of atomic lines (<u>electronic</u> excitation temperature)
 - <u>rotational</u> and <u>vibrational</u> temperature of molecules (line ratios or comparison with spectral simulation)
 - translational temperature from line broadening (Doppler effect)
 - glowing surfaces (Planck <u>blackbody</u> radiation)
- Chemical composition (usually under equilibrium consitions)

Typically valid in nonequilibrium

Equilibrium assumed but may measure thermal nonequilibrium

Typically equilibrium required 37

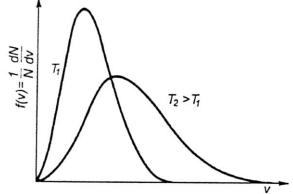


Introduction



- Each particle in a gas has a specific undirected velocity and, therefore, a kinetic energy.
- Definition of translational temperature: for the sum of all particles, a statistic distribution function can be formulated (Maxwellian velocity distribution):

Maxwellian velocity distribution
$$f(v) = \frac{dN}{N} = \frac{4 v^2}{\sqrt{\pi}} \left(\frac{1}{2RT}\right)^{\frac{3}{2}} e^{-\frac{v^2}{2RT}} dv$$



- Similar distribution functions can be formulated for other energies such as vibrational, rotational and electronic excitation (i.e. Boltzmann distributions).
- Energy is constantly exchanged through collisions.
- ➤ Electrons are lighter and more movable than heavy particles → more collisons possible → possibly different energy distribution → distinctive temperature
- ➤ For each form of energy, a temperature can be defined which controls the corresponding energy distribution (T_{vib}, T_{rot}, T_{elec}, ...).
- For many plasmas, the distribution parameters (i.e. temperatures) might all be different $\rightarrow T_{trans} \neq T_{el} \neq T_{rot} \neq T_{vib} \rightarrow non-equilibrium.$



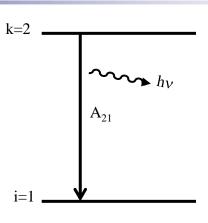
Emission of Atoms and Molecules



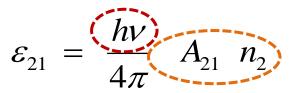
- Line position
- Line strength/intensity
- Line shape

from
$$\Delta E = E_{upper} - E_{lower} = h \nu$$
,

 \rightarrow v or λ for known energy levels

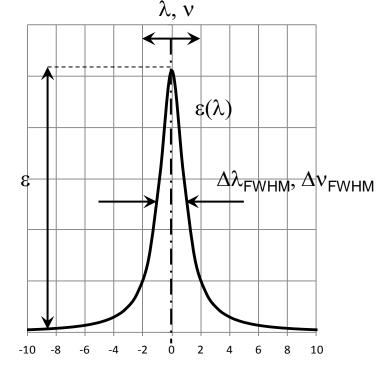


valid in general (atoms and molecules)



number of transitions

→ depends on energy of the upper state



one photon/transition

→ depends on energy difference

In equilibrium, the density n_k is related to n through the Boltzmann distribution:



Emission of Atoms: Electronic Excitation



- Line position
- Line strength/intensity
- Line shape

from $\Delta E = E_{upper} - E_{lower} = h v$, $\rightarrow v$ or λ for known energy levels

valid in general (atoms and molecules)

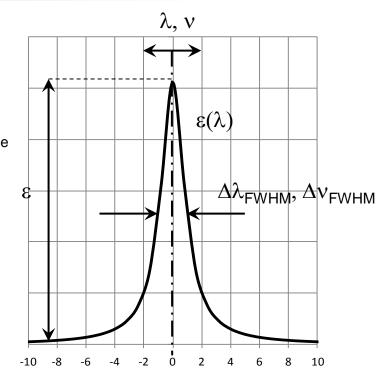
$$\varepsilon = \frac{h \nu}{4\pi} A_{ki}(n_k)$$

Population density of the excited state k

Partition function $U(T_{ex}) = \sum_{i} g_{i} \exp\left(-\frac{E_{i}}{kT_{ex}}\right)$

Number of different states which share the same energy Depends on the total angular momentum J which is the value of the vector addition of the orbital angular momentum L and the spin momentum S q = 2 J + 1

Degeneracy of the state k



 $n_{k} = \frac{g_{k}}{U(T_{ex})} n_{0} \exp\left(-\frac{E_{k}}{kT_{ex}}\right)$

excitation energy of the state k

electronic excitation temperature (in equilibrium gas temperature)

Total density of the species under consideration

In equilibrium, the density n_k is related to n through the Boltzmann distribution:



Emission of Atoms: Electronic Excitation



- Line position
- Line strength/intensity
- Line shape

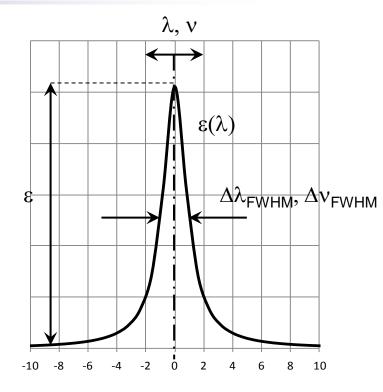
from $\Delta E = E_{upper} - E_{lower} = h \nu$, $\rightarrow \nu$ or λ for known energy levels

valid in general (atoms and molecules)

$$\varepsilon = \frac{h v}{4\pi} A_{ki} n_{k}$$

$$= \frac{h v}{4\pi} A_{ki} \underbrace{g_{k}}_{U(T_{ex})} n_{0} \exp\left(-\frac{E_{k}}{kT_{ex}}\right)$$

for electronic excitation in equilibrium



information on the transition (from quantum mechanics, e.g. from tables)

information about the thermodynamic condition of the plasma

In equilibrium, the density n_k is related to n through the Boltzmann distribution:



Electronic Excitation Temperature

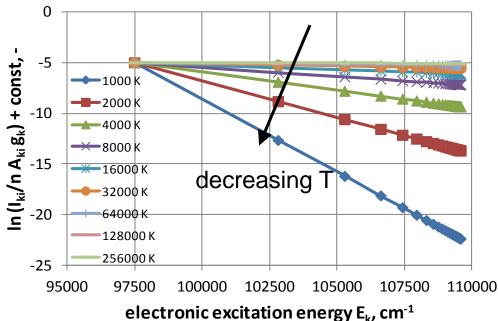


Theoretically, the ratio of two lines would be sufficient to determine the excitation temperature, but it is often in doubt if the electronic excitation is in equilibrium.

$$\ln\!\!\left(\frac{I_{ki}}{v\!A_{ki}g_k}\right) + const = -\frac{E_k}{kT_{ex}} \qquad \Rightarrow \text{Plot} \quad \ln\!\!\left(\frac{I_{ki}}{v\!A_{ki}g_k}\right) \quad \text{vs E}_k \Rightarrow \text{straight line with slope 1/-kT}$$
 (Boltzmann Plot)

If points are indeed on a straight line → Boltzmann valid → T can be determined

BUT: Even if Boltzmann seems valid, the apparent excitation temperature might not be an equilibrium temperature:





Electronic Excitation Temperature



Theoretically, the ratio of two lines would be sufficient to determine the excitation temperature, but it is often in doubt if the electronic excitation is in equilibrium.

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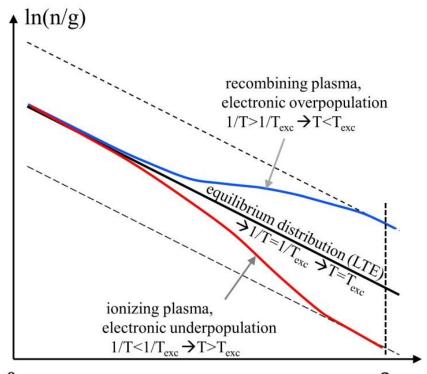
equilibrium temperature:

Recombining plasma

- high energy states will be populated through recombining ions
 - → flat distribution
 - → high excitation temperature

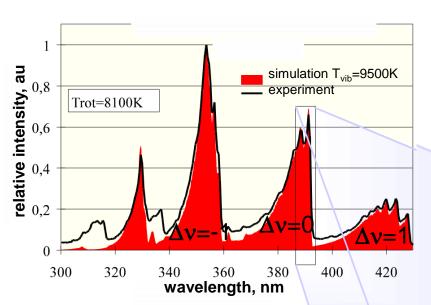
Ionizing plasma

- high energy states will be depopulated trough ionizing neutrals
- → steep distribution
- → low excitation temperature









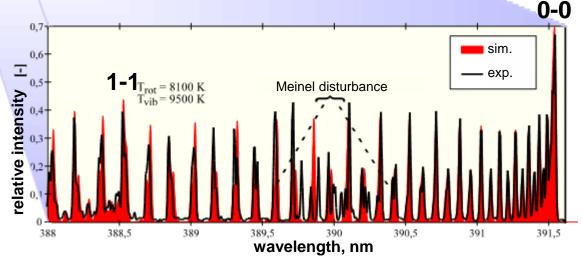
Molecule emission shows some shape but looks like a continuum

- Ratio of the different vibrational systems governed by T_{vib}
- Ratio within one vibrational transition
 (e.g. 0-0 → V_u=0, V_l=0) governed by T_{rot}

High spectral resolution

→ Single lines like atoms
but more ...

→ rotation and vibration







Radiation of molecules is caused by changes of the electronic level, the vibrational level, and the rotational level of excitation, often simultaneously.

$$\widetilde{v} = \frac{1}{hc} \left(\Delta E_{el} + \Delta E_{vib} + \Delta E_{rot} \right)$$

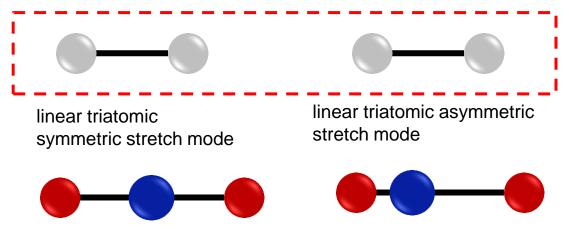
Born-Oppenheimer approximation: The total energy is the sum of the different excitations which can be computed separately.

Electronic excitation works similar to the atoms ...

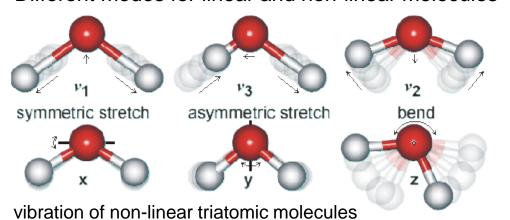




- For diatomic molecules, rotation and only one vibrational mode need to be accounted for.
- Already for tri-atomic molecules, several vibrational modes are possible.



Different modes for linear and non-linear molecules



diatomic molecules

- Rotation and vibration energies are discrete and not continuous and are obtained from solutions of the Schroedinger equation.
- For diatomic molecules, each energy is characterized through one quantum number (J for rotation, V for vibration).
- In addition, molecules may be electronically excited (same process as for atoms).

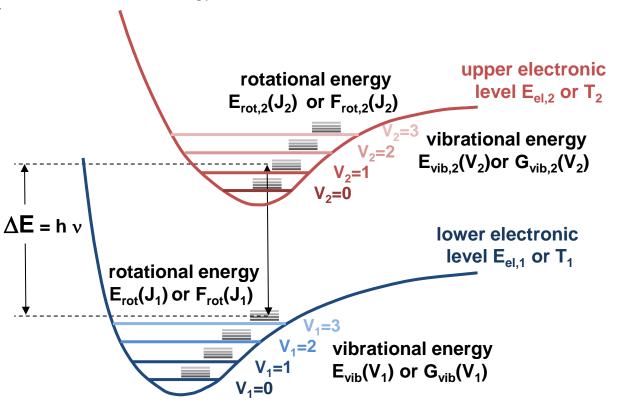


internal energy

Emission from Molecules



• Each electronic level of a molecule is described by a potential curve in terms of energy vs. inter nuclear distance.

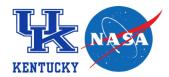


intranuclear distance

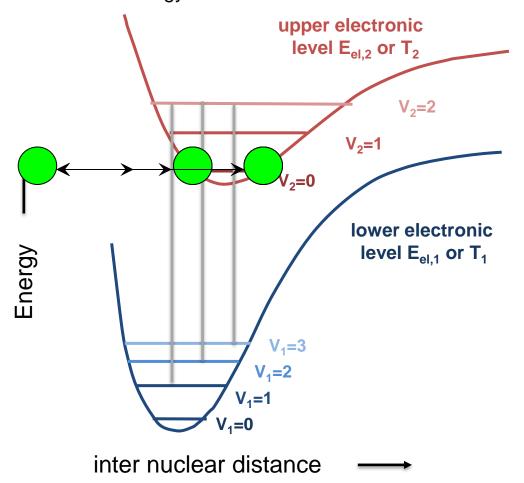
$$\widetilde{v} = \frac{1}{hc} \left(\Delta E_{el} + \Delta E_{vib} + \Delta E_{rot} \right)$$

- Different vibrational energies appear as lines of constant energy ion these potentials
- Excitation of the levels can happen through collisions (one major partner are electrons) or absorption of radiation.
- From one upper level, transitions to different lower levels are possible, each one resulting in a different emission line
- Usually, rotational energy changes in the same transition, possibly electronic excitation does, too, therefore contribution to the transition energy and the line position.





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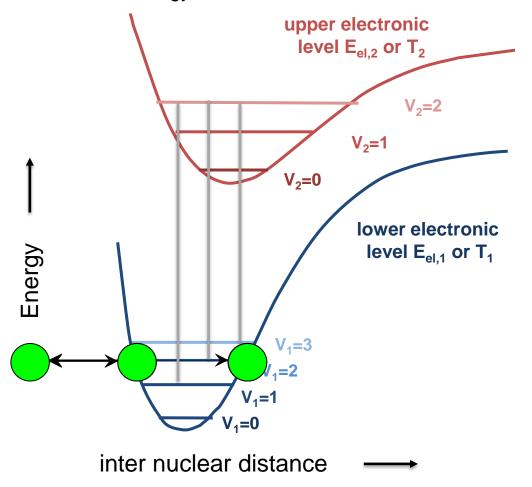
Vibrational Excitation of diatomic molecules

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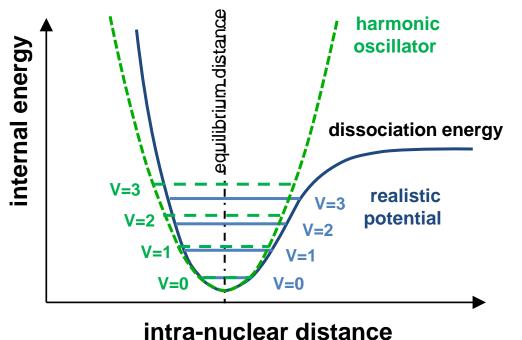
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- Rigid Rotator and Harmonic Oscillator
 - simple model, mainly to be used to account for rotational and vibrational energies in CFD codes → energy conservation
 - not suitable (at least the harmonic oscillator for spectral simulation)
 - The harmonic oscillator, however, does not describe real molecules:
 - for $r \sim \inf$. \rightarrow E = dissociation energy
 - for $r \sim 0 \rightarrow E \sim \inf$.



Morse Potential

$$U(x) = D_e \left(1 - e^{-\beta x}\right)^2$$

- x: distance to r_e
 (re: equilibrium distance between the nuclei)
- D_e: Well depth of the potential (dissociation energy- energy at minimum)

$$\beta = 1.2177 \cdot 10^{-7} \,\omega_e \sqrt{\frac{\mu_A}{D_e}}$$

• μ_A : reduced mass of the molecule

vibrational energy increment from V to V+1 now decreases with V:

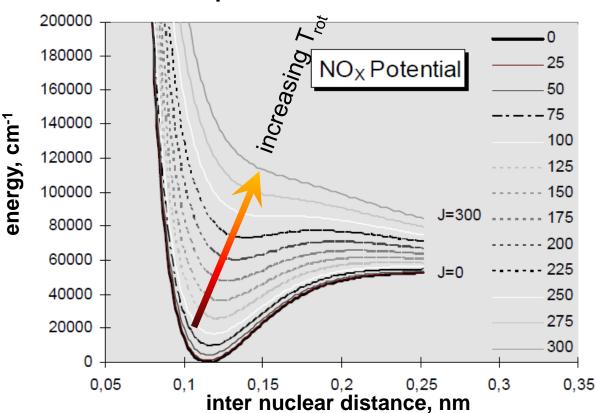
$$G(V) = \omega_e \left(V + \frac{1}{2} \right) - \omega_e x_e \left(V + \frac{1}{2} \right)^2$$





- Separation of rotational and vibrational excitation is not completely possible.
- In fact, the whole molecular potential changes shape with rotational quantum number.
- For rotationally highly excited states, only low vibrational excitation possible $\rightarrow V_{max}(J)$
- Or: limiting rotational quantum numbers different for each vibrational state $\rightarrow J_{max}(V)$

Molecular potential with rotational excitation



- limiting case:
 no more potential well
 → not stable
- will be different for each electronic state





Theoretical Simulation of Molecule Radiation

Intensity of one emission line:

$$\varepsilon = \frac{N'A_{\rightarrow}"\Delta E_{\rightarrow}"}{4\pi} = N' \frac{16\pi^3 c \, \overline{v}^4}{3} (R_e(\overline{r}_{V'V"}))^2 q_{V'V"} \frac{S_{J"A"}^{J'A'}}{2J'+1}$$
Particle density Electronic Hönl London Factor in the level e' V' J' transition moment

Assumption of Boltzmann distributions
$$\frac{N_{e'V'J'}}{N_{total}} = \frac{Q_{el}^{e'}Q_{vib}^{e'V'}Q_{rot}^{e'V'J'}}{\sum_{e'V'J'}Q_{el}^{e'}Q_{vib}^{e'V'}Q_{rot}^{e'V'J'}} \qquad \text{with the total partition function:} \\ Q = \sum_{e'V'J'}Q_{el}^{e'}Q_{vib}^{e'V'}Q_{rot}^{e'V'J'}$$

$$Q = \sum_{e'V'J'} Q_{el}^{e'} Q_{vib}^{e'V'} Q_{rot}^{e'V'J'}$$

$$(N_{e'V'J'}(T_{el}, T_{vib}, T_{rot}) = N_{total} \frac{g_{e'}\left(2J'+1\right)}{Q} \exp\left(-\frac{E_{el}^{e'}}{kT_{el}}\right) \exp\left(-\frac{E_{vib}^{e'V'}}{kT_{vib}}\right) \exp\left(-\frac{E_{rot}^{e'V'J'}}{kT_{rot}}\right)$$

electronic

$$Q_{el}^{e'} = g_{e'} \exp\left(-\frac{E_{el}^{e'}}{kT_{el}}\right)$$

vibrational

$$Q_{vib}^{e'V'} = \exp\left(-\frac{E_{vib}^{e'V'}}{kT_{vib}}\right)$$

rotational

$$Q_{el}^{e'} = g_{e'} \exp\left(-\frac{E_{el}^{e'}}{kT_{el}}\right) \qquad \qquad Q_{vib}^{e'V'} = \exp\left(-\frac{E_{vib}^{e'V'}}{kT_{vib}}\right) \qquad \qquad Q_{rot}^{e'V'J'} = \left(2J'+1\right) \exp\left(-\frac{E_{rot}^{e'V'J'}}{kT_{rot}}\right)$$





Theoretical Simulation of Molecule Radiation

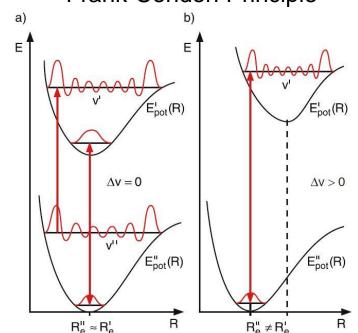
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Particle density Electronic H

in the level e' V' J'

- Electronic Hönl London Factor transition moment
- The electronic transition is fast in comparison to the motion of the nuclei during vibration.
- →The position of the nuclei relative to each other will not change during the transition.
- → The higher the overlap between the upper and lower potential, the higher the probability of the transition.
- → If wave functions are analyzed, this probability can be expressed in the electronic transition moment containing the Franck-Condon factor.

Frank-Condon Principle

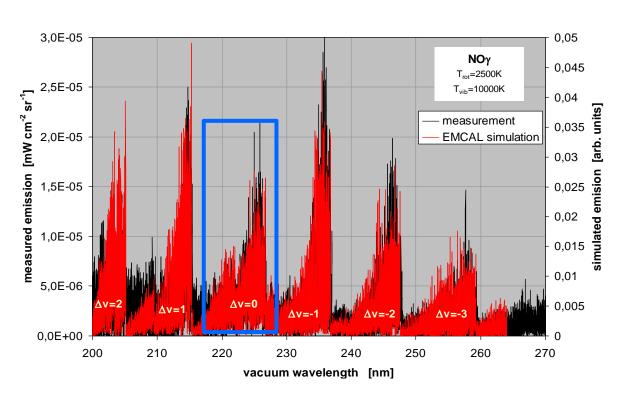


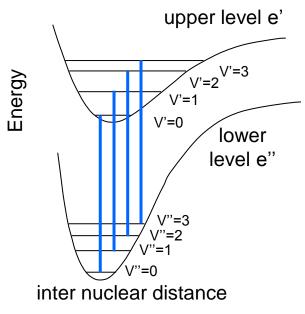




Molecular Band Structure

- Transition energies with the same difference in vibrational quantum number Δv are similar
- \rightarrow The different vibrational transitions tend to group for the same Δv .
- $\Delta V = 0$: 0-0, 1-1, 2-2, 3-3, ...



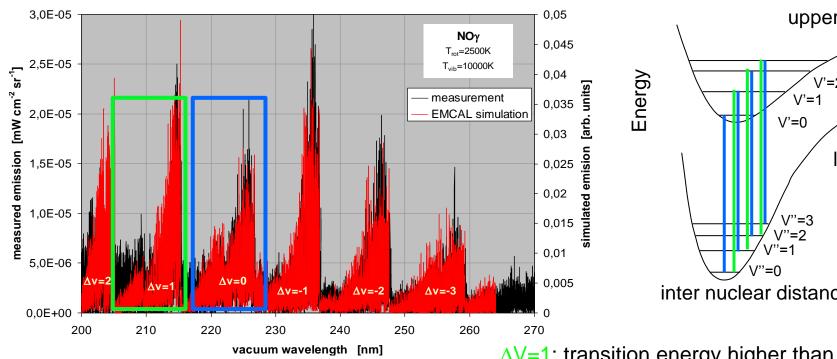


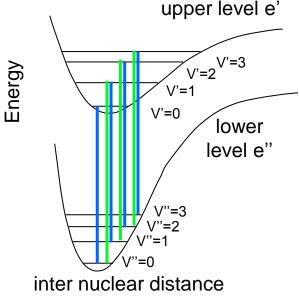




Molecular Band Structure

- Transition energies with the same difference in vibrational quantum number Δv are similar \rightarrow The different vibrational transitions tend to group for the same Δv .
- $\Delta V = 1$: 1-0, 2-1, 3-2, 4-3, ... \rightarrow higher $\Delta E \rightarrow$ lower λ





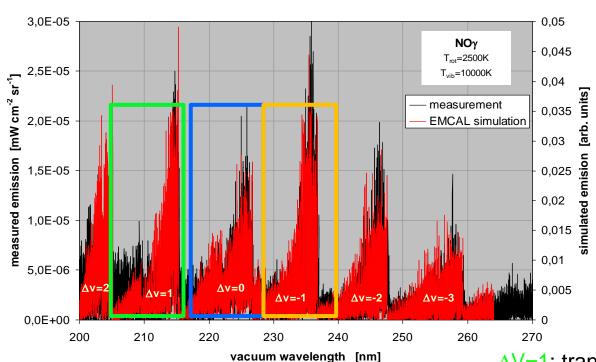
 $\Delta V=1$: transition energy higher than $\Delta V=0$

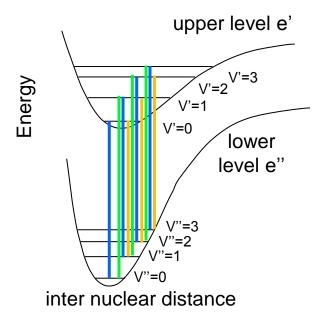




Molecular Band Structure

- Transition energies with the same difference in vibrational quantum number Δv are similar
- \rightarrow The different vibrational transitions tend to group for the same Δv .
- $\Delta V = -1$: 0-1, 1-2, 2-3, 3-4, ... \rightarrow lower $\Delta E \rightarrow$ higher λ





 $\Delta V=1$: transition energy higher than $\Delta V=0$

 $\Delta V=-1$: transition energy lower than $\Delta V=0$

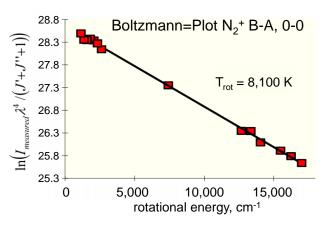


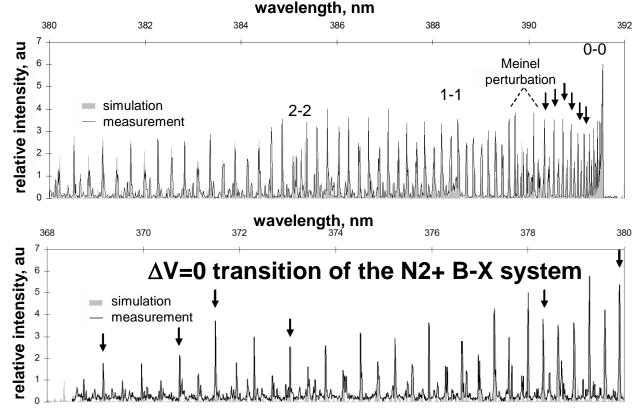


Temperature determination from molecular radiation

- Within one vibrational transition, a large number of rotational lines is present
 → rovibrational lines (may shift to lower or higher wavelengths, depending on B)
- Similar to the atoms, a Boltzmann plot can be performed to determine T_{rot}.

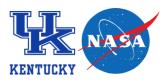
$$Q_{rot}^{e'v'J'} = (2J'+1)exp\left(-\frac{E_{rot}^{e'v'J'}}{kT_{rot}}\right)$$







Abel-Inversion



emission spectroscopy is a line of sight method
 only integrated data, no spatial resolution
 Abel integral equation:

$$I(z) = 2 \int_{r=z}^{R} \frac{r}{\sqrt{r^2 - z^2}} \varepsilon(r) dr$$

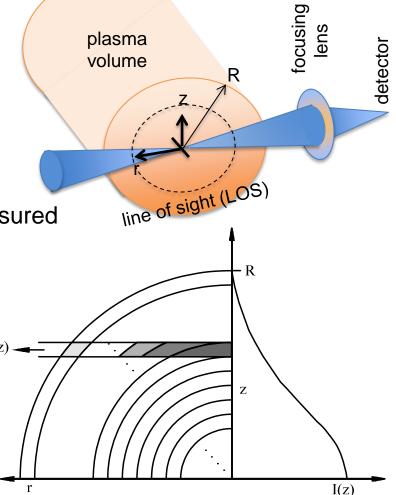
Typically, integrals along the line of sight are measured

→ the local emission is desired.

$$\varepsilon(r) = -\frac{1}{\pi} \int_{z=r}^{\infty} \frac{\left(\frac{dI}{dz}\right)}{\sqrt{z^2 - r^2}} dz$$

Solving this equation is usually only possible in I(z) special cases (e.g. a constant local distribution $\epsilon(r)$ =const. yields and elliptical profile in I(z))

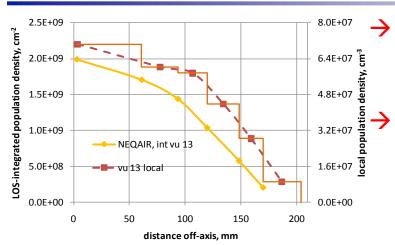
Under the assumptions of rotational symmetry and optically thin medium, local emission values - can be obtained from an Abel-Inversion.





Approximate Abel-Inversion





Different radial/vertical positions are to be measured

A matrix can be built that gives a relation between integrated and local emission

- → The matrix simplifies significantly if only few measurement positions are taken into account. constant local intensity in each ring assumed
- → A very simple system of linear equations can be obtained and solved recursively

$$I_{3,int}(Z_3) = \epsilon(r_3) * L_3(r_3)$$

$$I_{2,int}(Z_2) = \epsilon(r_3) * L_2(r_3) + \epsilon(r_2) * L_2(r_2)$$

$$I_{1,int}(Z_1) = \epsilon(r_3) * L_1(r_3) + \epsilon(r_2) * L_1(r_2) + \epsilon(r_1) * L_1(r_1)$$

$$Z_3 Z_2 Z_1$$

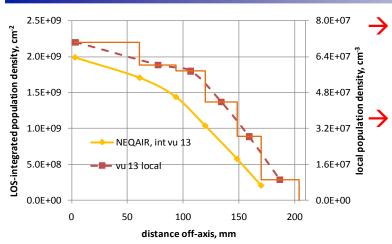
$$I_{0,int}(Z_0) = \epsilon(r_3) * L_0(r_3) + \epsilon(r_2) * L_0(r_2) + \epsilon(r_1) * L_0(r_1) + \epsilon(r_0) * L_0(r_0)$$

Winter, M. W., Prabhu, D. K., "Excited State Chemistry in the Free Stream of the NASA IHF Arc Jet Facility Observed by Emission Spectroscopy," 42nd AIAA Thermophysics Conference in Honolulu, Hawaii, 27 - 30 Jun 2011.



Approximate Abel-Inversion





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$$\begin{split} & I_{3,\text{int}} \left(\mathsf{Z}_{3} \right) = & \varepsilon(\mathsf{r}_{3}) \, * \mathsf{L}_{3}(\mathsf{r}_{3}) \\ & I_{2,\text{int}} \left(\mathsf{Z}_{2} \right) = & \varepsilon(\mathsf{r}_{3}) \, * \mathsf{L}_{2}(\mathsf{r}_{3}) + & \varepsilon(\mathsf{r}_{2}) \, * \mathsf{L}_{2}(\mathsf{r}_{2}) \\ & I_{1,\text{int}} \left(\mathsf{Z}_{1} \right) = & \varepsilon(\mathsf{r}_{3}) \, * \mathsf{L}_{1}(\mathsf{r}_{3}) + & \varepsilon(\mathsf{r}_{2}) \, * \mathsf{L}_{1}(\mathsf{r}_{2}) + & \varepsilon(\mathsf{r}_{1}) \, * \mathsf{L}_{1}(\mathsf{r}_{1}) \\ & I_{0,\text{int}} \left(\mathsf{Z}_{0} \right) = & \varepsilon(\mathsf{r}_{3}) \, * \mathsf{L}_{0}(\mathsf{r}_{3}) + & \varepsilon(\mathsf{r}_{2}) \, * \mathsf{L}_{0}(\mathsf{r}_{2}) + & \varepsilon(\mathsf{r}_{1}) \, * \mathsf{L}_{0}(\mathsf{r}_{1}) + & \varepsilon(\mathsf{r}_{0}) \, * \mathsf{L}_{0}(\mathsf{r}_{0}) \end{split}$$



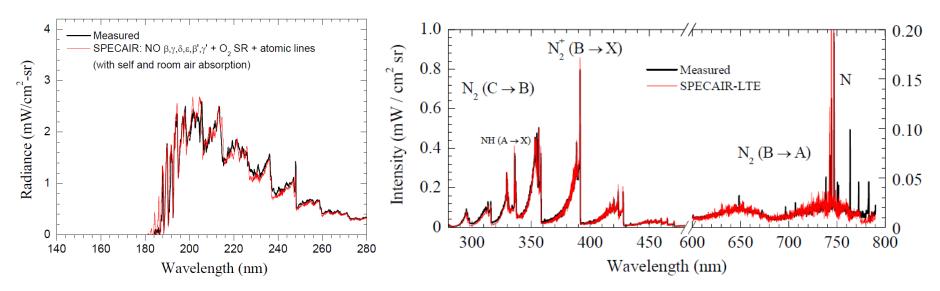
Application examples



Measurements in an atmospheric, inductively coupled plasma torch (C. Laux, Stanford University, now Ecole Centrale, Paris)

- Equilibrium plasma at up to 6000 K
 → chemistry well defined
- Used for the development of radiation models
- Excellent agreement between experiment and simulation can be achieved.

• After equilibrium characterization, used for non-equilibrium investigation.

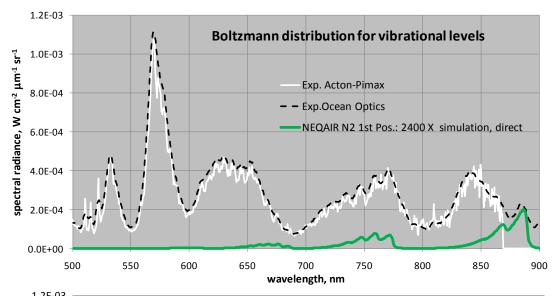


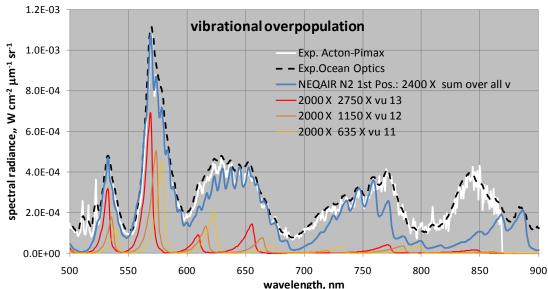
- Laux C. O.: Radiation and Nonequilibrium Collisional-Radiative Models, VKI Special Course on Physico-Chemical Models for High Enthalpy and Plasma Flows Modeling, Belgium, June 4-7, 2002. See also Laux, C.O., Pierrot, L., and Gessman, R.J., "State-to-state modeling of a recombining nitrogen plasma experiment," Chemical Physics, Vol. 398, pp. 46-55, DOI: 10.1016/j.chemphys.2011.10.028, 2012.
- Laux, C. O., "Radiation and nonequilibrium collisional-radiative models" in "Physico-chemical Models for High Enthalpy and Plasma Flows, VKI LS 2002-07, edited by D. G. Fletcher et al., Rhode-Saint-Genèse, Belgium, 2002.



NASA Ames IHF: Free Stream Investigation







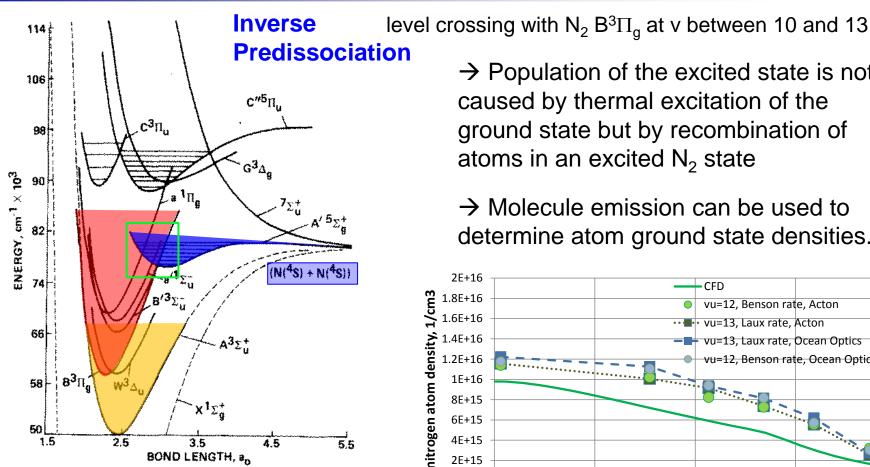
Comparison of free stream spectra at high condition with LTE simulation (VIS/NIR):

- Spectra dominated by emission of N2 B-A (1st Pos.)
- Thermodynamic quantities from CFD solution used as input for NEQAIR
- Spectra integrated along the line of sight
- Simulation and experiment do not even agree qualitatively
- If individual vibrational states are computed separately, the spectrum can be fitted by scaling these upper populations
- \rightarrow massive overpopulation of the high vibrational levels peaking at $v_{upper} = 13$



Application examples

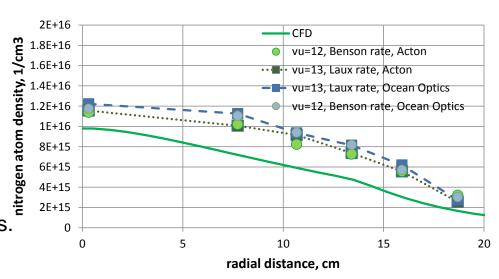




 Observed radiation comes from the 1st Pos. System (N₂ B³ Π_q \rightarrow A ³ Σ_u ⁺) with electronic excitation energies around 8eV to 10eV.

Harry Partridge, Stephen R. Langhoff, and Charles W. Bauschlicher, Jr., and David W. Schwenke, "Theoretical study of the A⁵S_a+ and C"⁵P_u states of N₂: Implications for the N₂ afterglow," J. Chern. Phys. 88 (5), 1 March 1988. Figure reproduced with permission from the authors.

- → Population of the excited state is not caused by thermal excitation of the ground state but by recombination of atoms in an excited N₂ state
- → Molecule emission can be used to determine atom ground state densities.



Winter, M, Srinivasan, C., Charnigo, R., "Non-Equilibrium Analysis of Emission Spectroscopy Data Taken in the Freestream of the NASA IHF Arc Jet Facility," AIAA AVIATION 2015, Dallas, Texas, June 2015.



200

250

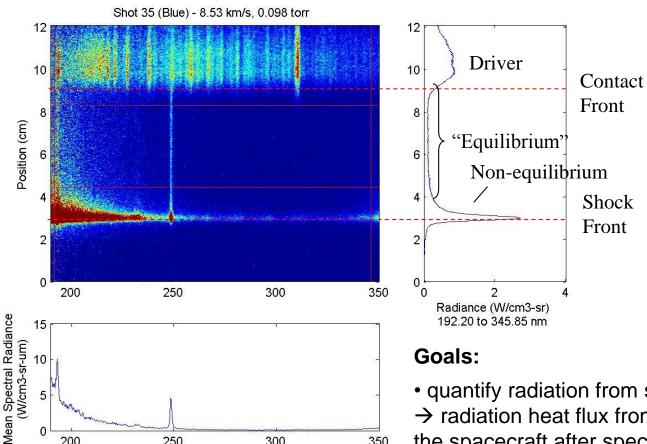
Wavelength (nm)

Application examples



Quantify radiation loads to spacecraft during atmospheric entry in impulse facilities

300



EAST shock tube (NASA Ames):

- reproduction of flight conditions
- no model testing
- 130nm 8μm in various intervals
- simultaneous measurements with 4 spectrometers possible
- one dimension resolves spectrally, the other spatially → shock and post-shock region are covered in one image
- quantify radiation from shock and post shock
- → radiation heat flux from the plasma upstream of the spacecraft after spectral integration
- → empirical correlation for radiation heat flux

- Cruden, B., Martinez, R., Grinstead, J. H., Olejniczak, J., "Simultaneous Vacuum Ultraviolet through Near IR Absolute Radiation Measurement with Spatiotemporal Resolution in an Electric Arc Shock Tube," AIAA 2009-4240, 41st AIAA Thermophysics Conference, 22 - 25 June 2009, San Antonio, Texas. - Aaron Brandis, Christopher Johnston, Marco Panesi, Brett Cruden, Dinesh Prabhu, Deepak Bose, "Investigation of Nonequilibrium Radiation for Mars Entry," AIAA 2013-1055, 51st AIAA Aerospace Sciences Meeting including the New Horizons Forum and Aerospace Exposition, 2013.

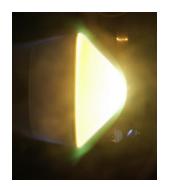
350



Application examples

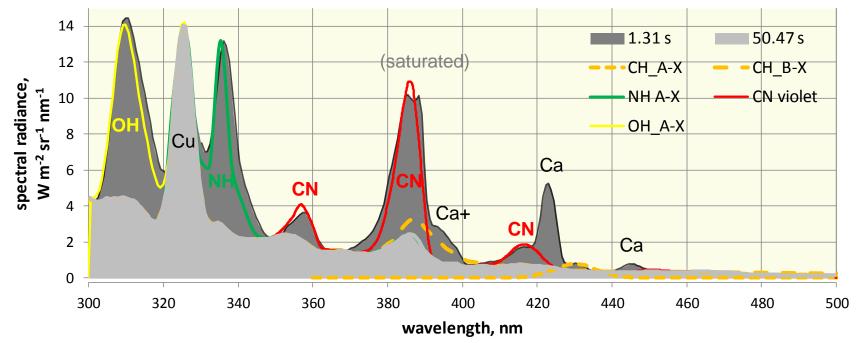


Monitoring of ablation species through optical methods



Testing of PICA at NASA Ames (SPRITE) showed the appearance of ablation products in emission spectra inside the boundary layer:
- CN, OH, NH, Ca, (Na, K)

Combination of pyrolysis products themselves and interactions with the plasma.



D. Empey, K. Skokova, P. Agrawal, G. Swanson, D. Prabhu, K. Peterson, M. Winter, E. Venkatapathy, "Small Probe Reentry Investigation for TPS Engineering (SPRITE)," AIAA-2012-0215, 50th AIAA Aerospace Sciences Meeting, Nashville, Tennessee, 9 - 12 Jan 2012... 65

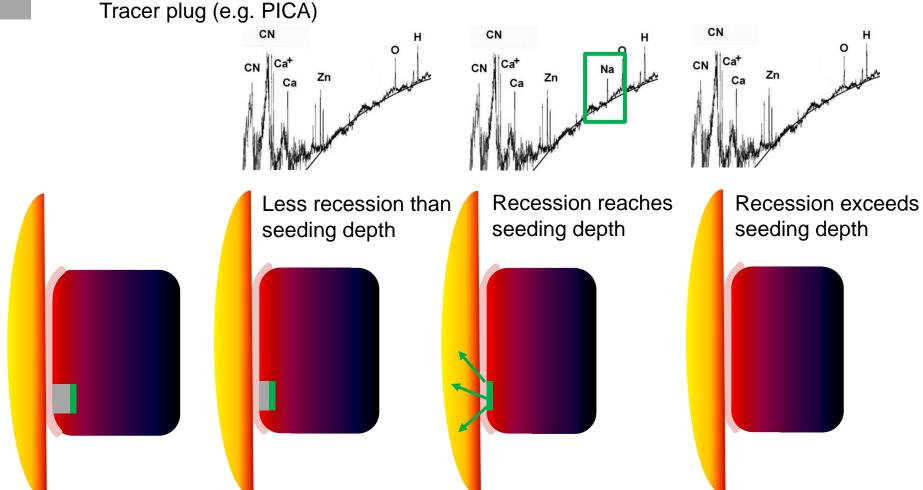


Application examples



Remote recession measurements of ablating TPS material

Tracer element (Coating/paint) (on ground and in flight)





Conclusions



- Optical emission spectroscopy is a useful tool to access information on thermal characteristics and composition of a plasma.
- Applications for which the assumption of equilibrium is rather uncritical:
 - identification of species;
 - total radiation flux (in the wavelength covered and if properly calibrated);
 - quantities from line broadening (e.g. Doppler temperature, electron density);
 - identification of thermal non-equilibrium.
- Applications for which the assumption of equilibrium is rather crucial:
 - determination of particle densities from thermal excitation;
 - measurement of excitation temperatures from line ratios.
- Proper calibration is imperative.
- Comparison with simulation (non-equilibrium chemistry and excitation, e.g. though collisional radiative models) seems the best approach as soon as these models are validated.

Thanks for your attention!

Open for

Questions?



Back-up Slides





Selection of Simulation Codes (Line-byLine)

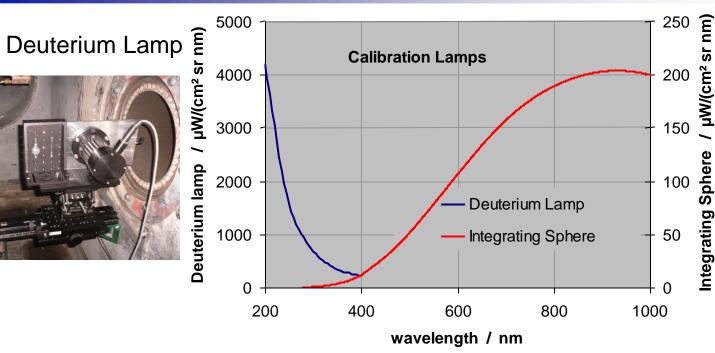


- - FORTRAN, non-eq. (QSS + multi T), air and CO₂ plasma related species + H, radiation transport capabilities Whiting, E E, Park, C, Liu, Y, Arnold, J O, and Paterson, J A, "NEQAIR96, Nonequilibrium and Equilibrium Radiative Transport and Spectra Program: User's Manual," NASA RP-1389, NASA, December 1996.
- HARA (...) NASA Langley EAR restricted
 - FORTRAN, non-eq. (QSS + multi T), air and CO₂ plasma related species, radiation transport capabilities Johnston, C. O., Hollis, B. R., and Sutton, K., "Spectrum Modeling for Air Shock-Layer Radiation at Lunar-Return Conditions," Journal of Spacecraft and Rockets, Sep.-Oct. 2008.
- SPRADIAN/RADIPAC Japan/South Korea available on request to JAXA
 FORTRAN, non-eq. (QSS + multi T), air + ablation related species, radiation transport capabilities
 Fujita, K., and Abe, T., "SPRADIAN, Structured Package for Radiation Analysis: Theory and Application,"
 The Institute of Space and Astronautical Science Report No. 669, July 1997.
- PARADE European Space Agency ESA available on request to ESA FORTRAN, non-eq. (QSS + multi T), air + CO₂ plasma related species, rad. transport capabilities (HERTA) Smith, A. J., Wood, A., Dubois, J., Fertig, M., Pfeiffer, B.: *Plasma Radiation Database PARADE V22 Final Report Issue* 3, ESTEC contract 11148/94/NL/FG, FGE TR28/96, Issue 3, Oktober 2006.
- SPECAIR Ecole Centrale Paris Windows version available by download air, multi T, no radiation transport
 - Laux, C. O., "Radiation and nonequilibrium collisional-radiative models" in "Physico-chemical Models for High Enthalpy and Plasma Flows," VKI LS 2002-07, edited by D. G. Fletcher et al., Rhode-Saint-Genèse, Belgium, 2002. http://www.specair-radiation.net
- LIFBASE Stanford Research Institute SRI Windows version available by download
 LIF related diatomic molecules (CH, NH, OH, CO, NO, ...), no radiation transport
 J. Luque and D.R. Crosley, "LIFBASE: Database and spectral simulation (version 1.5)", SRI International Report MP 99-009 (1999)
 http://www.sri.com/psd/lifbase/

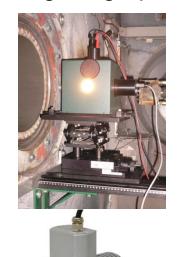


Intensity Calibration – How?





Integrating Sphere

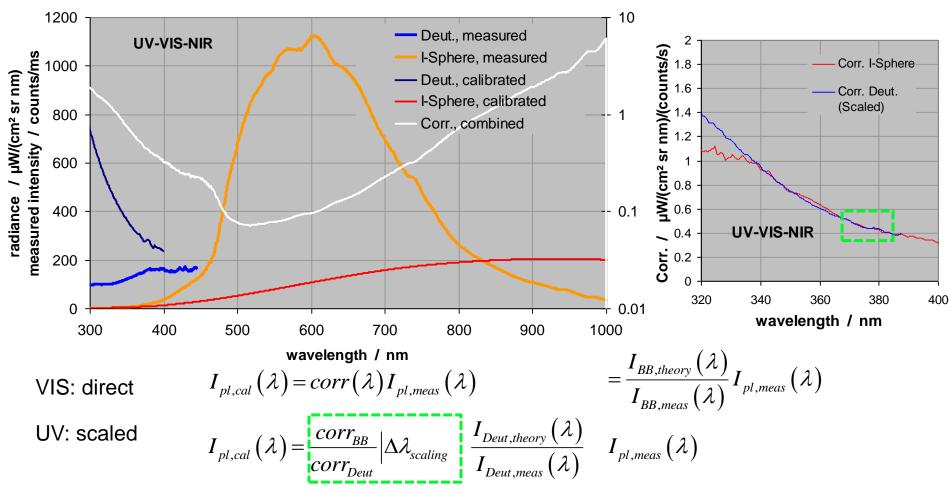


- Calibration with an integrating sphere (halogen bulbs UV-VIS-NIR) and a Deuterium lamp (UV) both calibrated to spectral radiance in μW/(cm² sr nm)
- Correction factor: ratio of factory calibration value and measurement of calibration lamp
- Deuterium lamp (UV) can not easily be used for absolute calibration
 → scaling of Deuterium correction factor to the I-Sphere in overlapping region.
- Best calibration: place the calibration lamp at the location of the measured plasma
 → all set-up influences are covered and direct calibration is possible.
 - Lamp area must be larger than measurement spot !!!



Intensity Calibration – How?





- \rightarrow Correction factor corr(λ) which is the inverse sensitivity of the set-up.
- → Use of Deuterium lamp only for qualitative calibration followed by scaling (cross calibration) through halogen lamp/black-body.

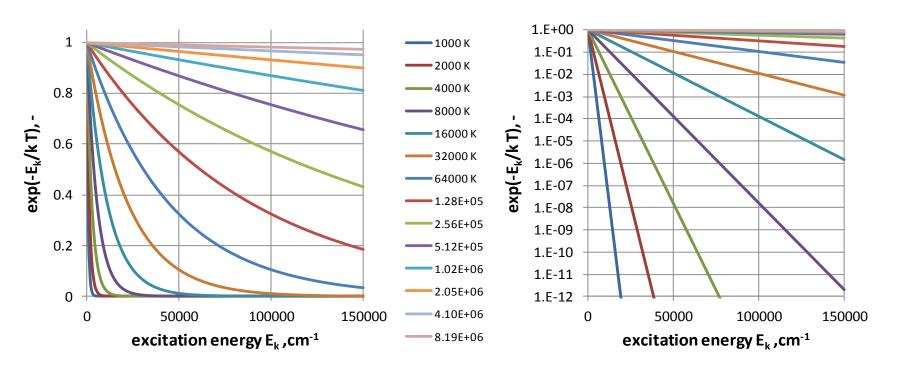


Emission of Atoms: Electronic Excitation



$$\varepsilon = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4 \pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{k T_{ex}}\right)$$

- For low temperatures, only the first energy levels are populated.
- With temperature going to infinity, all levels would be populated according to g_k/U.



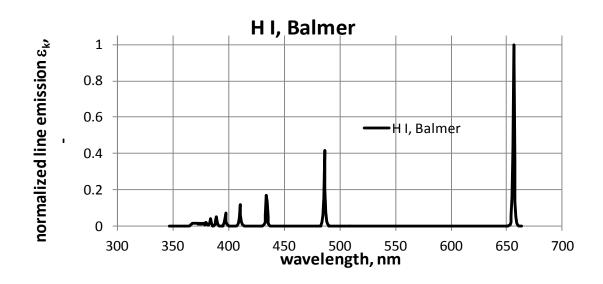


Electronic Excitation of Hydrogen



$$\varepsilon = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4 \pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{kT_{ex}}\right)$$

Balmer spectrum of hydrogen



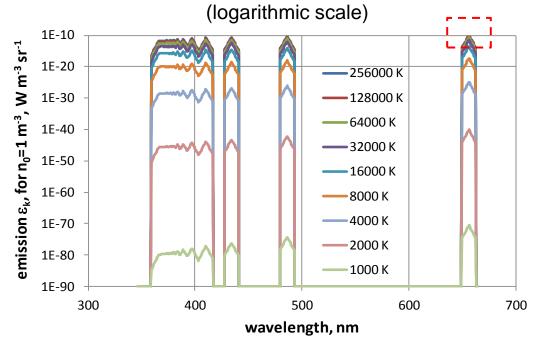


Electronic Excitation of Hydrogen



$$\varepsilon = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4 \pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{k T_{ex}}\right)$$

Balmer spectrum of hydrogen for different temperatures:



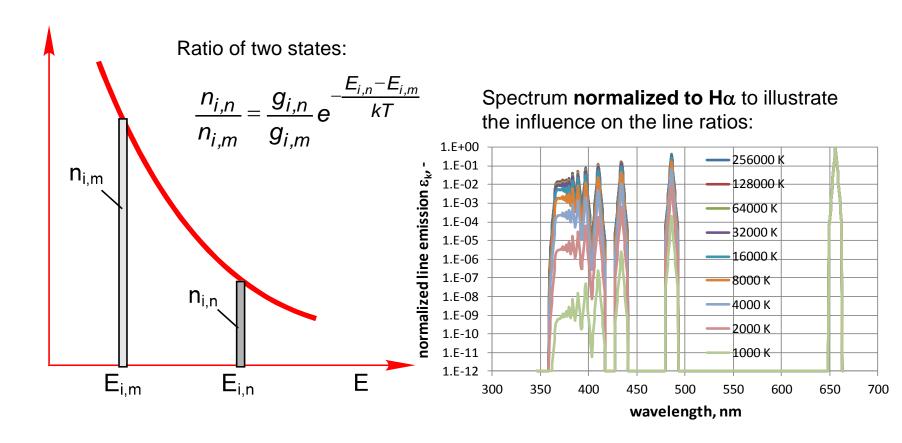
- Emission increases by 60 orders of magnitude between 1000K and 8000K
- Ratio of different lines in the Balmer series changes with temperature (hard to see on log scale).
- To illustrate the ratios, we normalize the spectrum to the H_α line.



Electronic Excitation of Hydrogen



$$\varepsilon = \frac{h \nu}{4\pi} A_{ki} n_k = \frac{h \nu}{4 \pi} A_{ki} \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{k T_{ex}}\right)$$





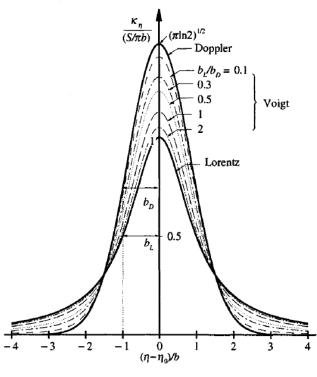
Emission of Atoms and Molecules



Line Broadening

Emission and absorption lines can be broadened through different processes:

- natural broadening (Heisenberg uncertainty principle)
- Doppler broadening (thermal motion)
- Collision broadening
 - Van-der-Waals: collisions with neutrals
 - Resonance: collisions with the 'like' species particles (perturber's state connected by an allowed transition to the upper or lower state of the transition under consideration)
 - Stark for interactions with ions or electrons, specific for each transition/line
- (Zeeman effect interaction with magnetic fields)
 - Each of these processes is actually a line shift for one photon.
 - The integration over many photons with different shifts produces a broadening.
 - → distributing the transition energy over a certain wavelength/wavenumber range
- Depending on the physical effect, the final line shape will follow a Gauss or a Lorentz profile.
- Usually, the broadening is described by the line width at its half maximum (full width FWHM, or half width HWHM).
- Half widths of Lorentz profile can be summed up linearly.
- Half widths of Gauss profiles can be combined quadratically through $FWHM_{G,total} = \sqrt{FWHM_{G,1}^2 + FWHM_{G,2}^2}$.





Emission of Atoms and Molecules



Line Broadening

Collision broadening (Lorentz)

$$\kappa_{\eta} = \frac{S}{\pi} \frac{b_C}{(\eta - \eta_0)^2 + b_C^2}, \quad S \equiv \int_{\Delta \eta} \kappa_{\eta} \, d\eta,$$

HWHM decreases with T

$$b_c = b_{c0} \left(\frac{p}{p_0}\right) \sqrt{\frac{T_0}{T}},$$

HWHM increases with T

$$\kappa_{\eta} = \sqrt{\frac{\ln 2}{\pi}} \left(\frac{S}{b_0} \right) \exp \left[-(\ln 2) \left(\frac{\eta - \eta_0}{b_0} \right)^2 \right]$$

Doppler broadening (Gauss)

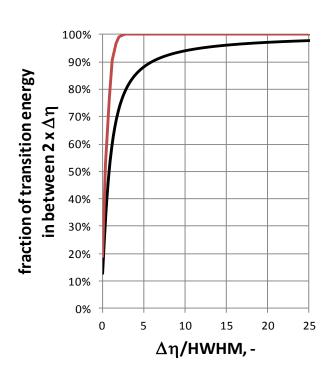
$$b_D = \frac{\eta_0}{c_0} \sqrt{\frac{2kT}{m}} \ln 2.$$

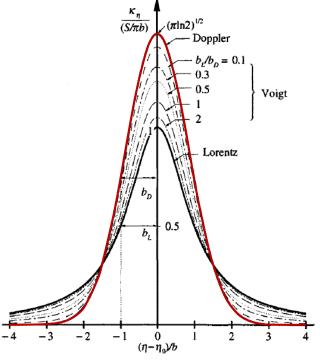
Lorentz:

- 90% of the transition energy within 6 HWHM
- 99% is reached after
 50 HWHM

Gauss:

• 99% in 2 HWHM





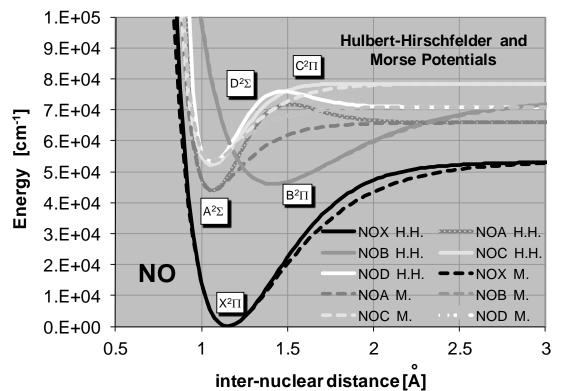


Emission from Molecules



The Anharmonic Oscillator – Higher Order Potentials

- Higher order potentials
 Lippincott 3 parameter fit
 Hulbert-Hirschfelder 5 parameter fit
- may provide better agreement with experimental data



Morse Potential

$$U(x) = D_e \left(1 - e^{-\beta x}\right)^2$$

- x: distance to r_e
 (re: equilibrium distance between the nuclei)
- D_e: Well depth of the potential (dissociation energy- energy at minimum)

$$\beta = 1.2177 \cdot 10^{-7} \, \omega_e \sqrt{\frac{\mu_A}{D_e}}$$

• μ_A : reduced mass of the molecule

vibrational energy increment from V to V+1 now decreases with V:

$$\int_{3}^{3} G(V) = \omega_{e} \left(V + \frac{1}{2} \right) - \omega_{e} x_{e} \left(V + \frac{1}{2} \right)^{2}$$



Emission from Molecules



Higher Order Approximations - Dunham Expansion

- Vibrational energy expressed as a polynomial function of V
- For small quantum numbers equivalent to Morse

$$G(V) = \omega_e \left(V + \frac{1}{2} \right) - \omega_e x_e \left(V + \frac{1}{2} \right)^2 + \omega_e y_e \left(V + \frac{1}{2} \right)^3 + \omega_e z_e \left(V + \frac{1}{2} \right)^4 + \dots$$

- Rotational energy contains higher orders of J
- coupling constants now depend on V

$$F_V(V,J) = B_V J(J+1) - D_V J^2 (J+1)^2 + \dots$$

$$B_{V} = B_{e} - \alpha_{e} \left(V + \frac{1}{2}\right) + \gamma_{e} \left(V + \frac{1}{2}\right)^{2} + \dots$$

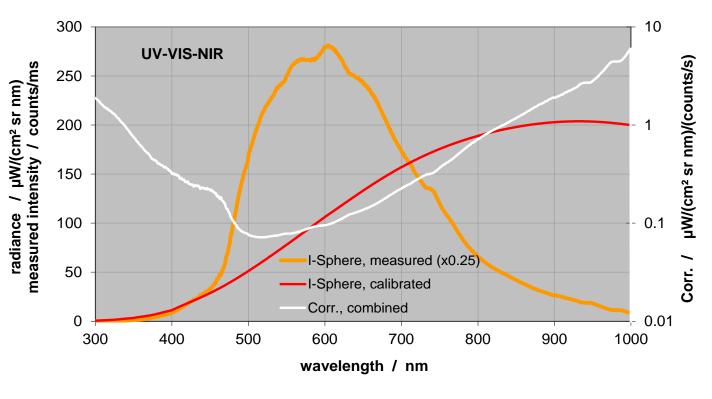
$$D_V = D_e + \beta_e \left(V + \frac{1}{2}\right) + \delta_e \left(V + \frac{1}{2}\right)^2 + \dots$$

Different sets of constants given in literature



Intensity Calibration – How?





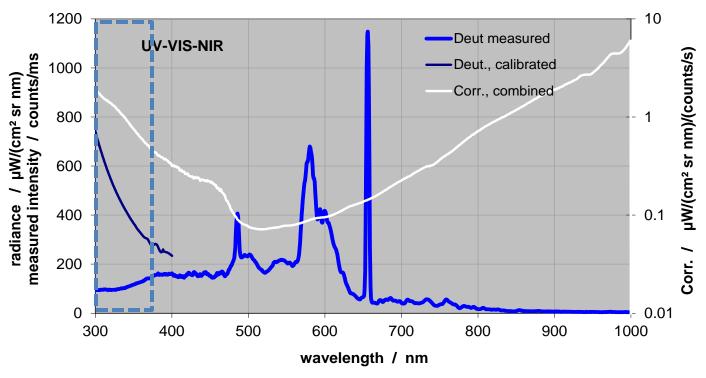
$$I_{plasma,cal}(\lambda) = corr(\lambda) * I_{plasma, measured}(\lambda) = [I_{lamp,theory}(\lambda)/I_{lamp,measured}(\lambda)] * I_{plasma, measured}(\lambda)$$

- Best calibration: place the calibration lamp at the location of the measured plasma
 all set-up influences are covered and direct calibration is possible.
 - Lamp area must be larger than measurement spot !!!



Intensity Calibration – How?





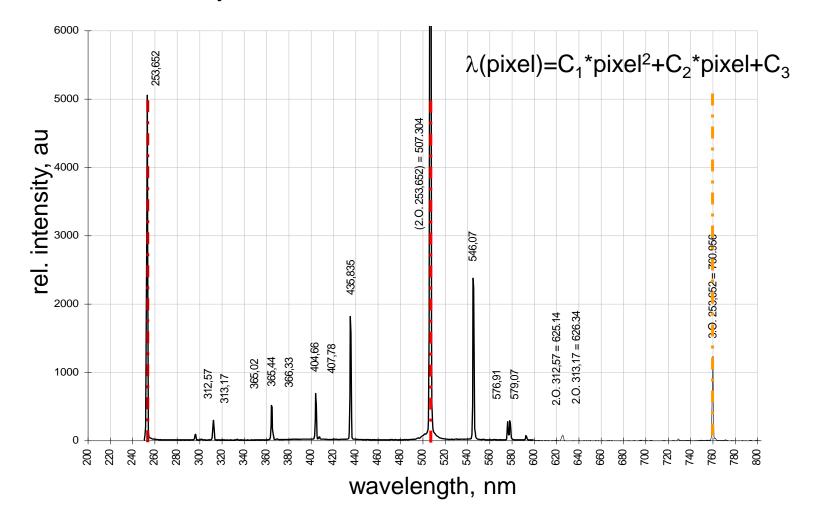
- Deuterium lamp (UV) uses a hydrogen discharge to produce high radiation in VUV-VIS
- Usually, only the continuum emission from UV down is used for calibration.
- Although calibrated to radiance in μW/(cm² sr nm), the dimensions of the discharge are small (~1mm) → measurement spot usually larger
- Discharge shows gradients → additional uncertainties introduced.
- → Use of Deuterium lamp only for qualitative calibration followed by scaling (cross calibration) through halogen lamp/black-body.



Wavelength Calibration



- Compare measured line positions (pixel) with known line positions (e.g. Hg lamp):
 - scanning spectrometer: typically linear with time → at least 2 lines needed;
 - CCD measurement: typically binomial → at least 3 lines needed.
- additional lines may serve as a calibration check ...





Electronic Excitation Temperature



The emission coefficient

$$\varepsilon = \frac{h\nu}{4\pi} A_{ki} n_k$$

With the Boltzmann distribution

$$n_k = \frac{g_k}{U(T_{ex})} n_0 \exp\left(-\frac{E_k}{kT_{ex}}\right)$$

Theoretically, the ratio of two lines would be sufficient, but it is often in doubt if the electronic excitation is in equilibrium.

→Boltzmann Plot:

Plot
$$\ln \left(\frac{I_{ki}}{vA_{ki}g_k} \right)$$
 vs E_k

→ Straight line with slope 1/-kT

If points are indeed on a straight line

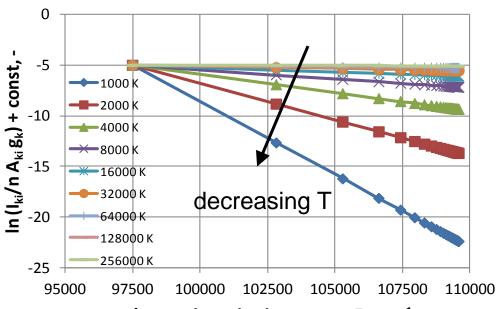
- → Boltzmann valid
- → T can be determined

is integrated along the line of sight

$$I_{ki} = \int \varepsilon(x) dx = \frac{h v}{4\pi} A_{ki} n_k l$$

follows:

$$\ln\left(\frac{I_{ki}}{vA_{ki}g_{k}}\right) + const = -\frac{E_{k}}{kT_{ex}}$$

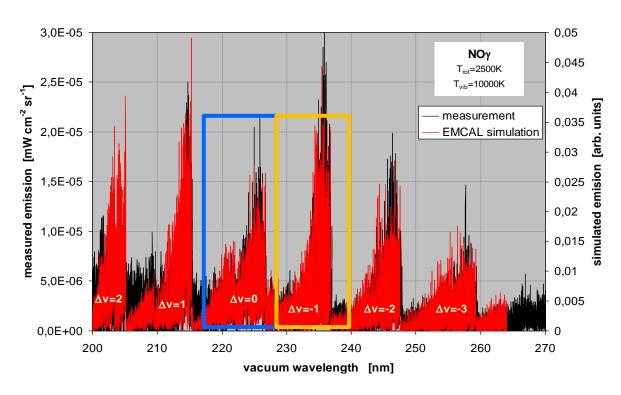


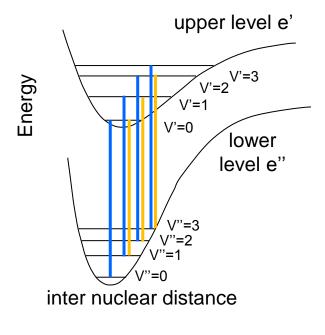


Molecular Band Structure



- Transition energies with the same difference in vibrational quantum number Δv are similar
- \rightarrow The different vibrational transitions tend to group for the same Δv .
- $\Delta V = -1$: 0-1, 1-2, 2-3, 3-4, ... \rightarrow lower $\Delta E \rightarrow$ higher λ





 $\Delta V=-1$: transition energy lower than $\Delta V=0$



Emission from Molecules



Theoretical Simulation of Molecule Radiation

Intensity of one emission line:

$$\varepsilon = \frac{N'A_{\rightarrow}"\Delta E_{\rightarrow}"}{4\pi} = N' \frac{16\pi^3 c\,\overline{v}^4}{3} (R_e(\overline{r}_{V'V"}))^2 q_{V'V"} \frac{S_{J"\Lambda"}^{J'\Lambda'}}{2J'+1}$$
Particle density Electronic Hönl London Factor in the level e' V' J' transition moment

- There are (2J+1) allowed rotational states (rotational multiplicity)
- The selection rules allow for ∆J=-1,0,1
- The Hönl London Factor controls how the (2J+1) states are distributed among the branches



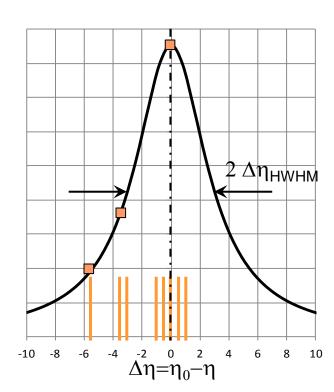
Emission of Atoms and Molecules



Line Broadening

Emission and absorption lines can be broadened through different processes:

- natural broadening (Heisenberg uncertainty principle)
- Doppler broadening (thermal motion)
- Collision broadening
 - Van-der-Waals: collisions with neutrals
 - Resonance: collisions with the 'like' species particles (perturber's state connected by an allowed transition to the upper or lower state of the transition under consideration)
 - Stark for interactions with ions or electrons, specific for each transition/line
- (Zeeman effect interaction with magnetic fields)
 - Each of these processes is actually a line shift for one photon.
 - The integration over many photons with different shifts produces a broadening.
 - → distributing the transition energy over a certain wavelength/wavenumber range
 - Temperature measurement (low pressures, high temperatures)
- Electron density measurement (lines with large Stark coefficients, e.g. H_{α} or H_{β})





Emission of Atoms and Molecules



Line Broadening

Emission and absorption lines can be broadened through different processes:

natural broadening (Heisenberg uncertainty principle)

Gauss

Lorentz

Doppler broadening (thermal motion)

Lorentz

- Collision broadening
 - Van-der-Waals: collisions with neutrals
 - Resonance: collisions with the 'like' species particles (perturber's state connected by an allowed transition to the upper or lower state of the transition being studied)
 - Stark for interactions with ions or electrons, specific for each transition/line
- (Zeeman effect interaction with magnetic fields)

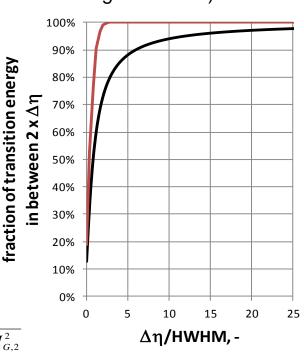
Lorentz:

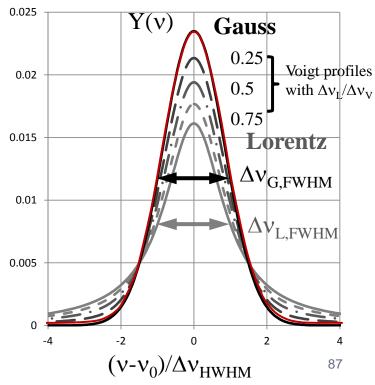
- 90% of the transition energy within 6 HWHM
- 99% is reached after
 50 HWHM
- Half widths are added linearly.

Gauss:

- 99% in 2 HWHM
- are combined as the geometric sum

 $FWHM_{G,total} = \sqrt{FWHM_{G,1}^2 + FWHM_{G,2}^2}$



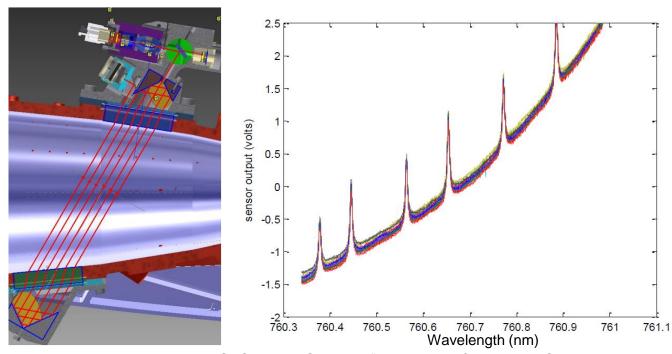




Intro to Absorption Spectroscopy in Nonequilibrium Hypersonic Flows



Craig Johansen, The University of Calgary, Canada <u>Sean O'Byrne</u>, University of New South Wales Canberra, Canberra, Australia



J. Kurtz, M. Aizengendler, Y. Krishna, and S. O'Byrne, S (2015) "Flight Test of a Rugged Scramjet-Inlet Temperature and Velocity Sensor," *AIAA SciTech*, 5-9 January, Kissimee, Florida, USA.



Outline

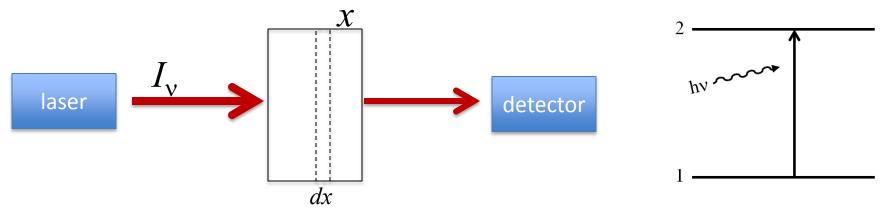


- Introduction & Background
- Velocity measurement
- Temperature:
 - Translational
 - Rotational
 - Vibrational
- Tomography and Hyperspectral
- Flight Application



Tunable Diode Laser Absorption Spectroscopy





Absorption is described by the Beer-Lambert Law:

$$-dI_{\nu} = I_{\nu}k_s(\nu)dx$$

where $k_s(v)$ is the spectral absorption coefficient.

This leads to exponential decay of laser intensity:

$$I_{\nu,x} = I_{\nu,0}e^{-k_s(\nu)x}$$

- Measure $I_{
 m v}$, know x, directly measure $k_s(v)$
- $k_s(v)$ contains information about temperature, concentration, velocity of gas



TDLAS: Strengths and Weaknesses



Strengths

- Can probe non-luminous flows and ground-state populations
- Simple, rugged optical arrangements with no moving parts
- Comparatively inexpensive
- Fast wavelength scanning capability (wavelength agile)
- Can provide quantitative multiparameter measurement with a single instrument
 - No systematic errors due to quenching

Weaknesses

- Path-integrated technique
 - Distributions can be determined tomographically, but time consuming and analysis can be complex
- Spatial and temporal flow nonuniformity can produce bias errors in measurements unless the freestream is well characterized
- Some important diatomics (eg N₂) do not have a dipole moment and do not have a direct absorption spectrum



Broadening Mechanisms



- Spectral shape of $k_s(v)$ is from "broadening"
- Pressure (Homogeneous) Broadening

$$g_H = \frac{\Delta v_H}{2\pi} \frac{1}{(v - v_0)^2 + (\Delta v_H/2)^2}$$

- Caused by collisions with other atoms/molecules,
 a high-pressure effect causing a Lorentzian shape
- Generates a broadening

$$\Delta v_c = P \sum_i (\chi_i^2 \gamma_i)$$

and a shift in the transition

$$\Delta v_s = P \sum (\chi_i \delta_i)$$

P is the pressure χ_i is the concentration γ_i is collision width per unit pressure δ_i is collision shift per unit pressure

If temperature can be independently determined, pressure can be measured from these quantities



Broadening Mechanisms



- Doppler (Inhomogeneous) Broadening
 - Due to thermal motion of absorbing particles towards or away from laser

$$g_{D} = \frac{2\sqrt{\ln 2}}{\pi^{1/2} \Delta v_{D}} e^{\left[\frac{-4(\ln 2)(v - v_{0})}{\Delta v_{D}^{2}}\right]}$$

 $-\Delta v_D$ is the full-width at half-maximum of the measured peak, and is given by

$$\Delta v_D = 2v_0 \sqrt{\frac{2kT_{trans}}{(MW)c^2}} \ln 2$$

 v_0 is the transition center k is the Boltzmann constant



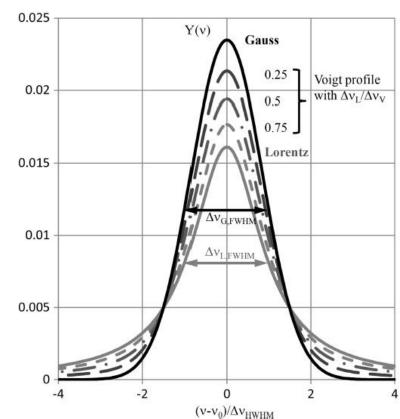
Voigt Profile



 The Voigt profile is a convolution of the two previous broadening effects

$$V(a,x) = \frac{a}{\pi} \int_{-\infty}^{\infty} \frac{e^{-y^2}}{a^2 + (x - y)^2} dy$$

$$a = \sqrt{\ln 2} \frac{\Delta v_H}{\Delta v_D}, \quad x = 2\sqrt{\ln 2} \frac{(v - v_0)}{\Delta v_D}$$





Laser Sources



- In 1970s, dye lasers were often used in visible and NIR absorption studies, and Pb salt for IR. Now mostly replaced with:
- Diode laser sources
 - Distributed feedback (DFB) lasers
 - Tune over ~0.1 nm
 - Robust and well tested in telecoms
 - Very spectrally narrow (1-30 MHz)
 - Vertical cavity surface-emitting lasers (VCSELs)
 - Tune over 1 nm
 - Tune very rapidly
 - Spectrally narrow (<30 MHz)
 - Quantum cascade lasers (QC)
 - High-power pulsed source operating in the IR





Direct absorption

Simple, direct measurements, but poor use of dynamic range

Difference amplification

Removes intensity modulation, but only when perfectly balanced

Log-ratio detection

- Simple circuit, and cancels common-mode electronic and laser noise very efficiently
- Can be autobalanced, to remove offset caused by mismatch in reference and signal intensities
 - M.G. Allen et al. Applied Optics 34.18 (1995): 3240-3249
- Bandwidth decreases as photocurrent decreases





Wavelength modulation

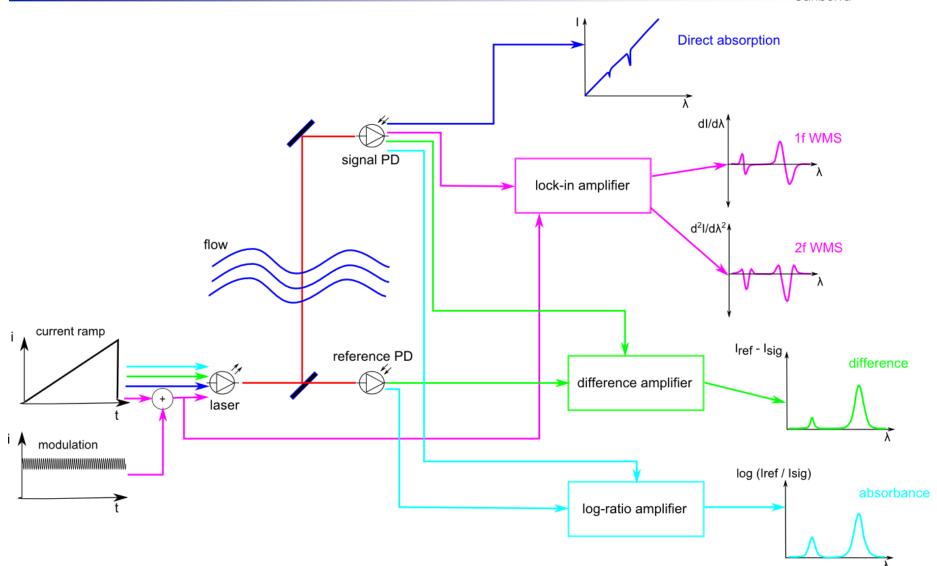
- Removes DC offset from signal
- Signal proportional to the derivative of the input intensity
- Phase-sensitive detection at a multiple of the modulation frequency can reduce 1/f noise in the signal
- Traditionally required careful calibration to samples under controlled conditions, but recent innovation using the ratio of second-harmonic (2f) and first-harmonic (1f) signals to account for the laser intensity
 - GB Rieker et al. Appl. Opt. 48.29 (2009): 5546-5560.

Cavity-based methods

 Useful for measurements of trace quantities, but practical challenges in hostile environments.



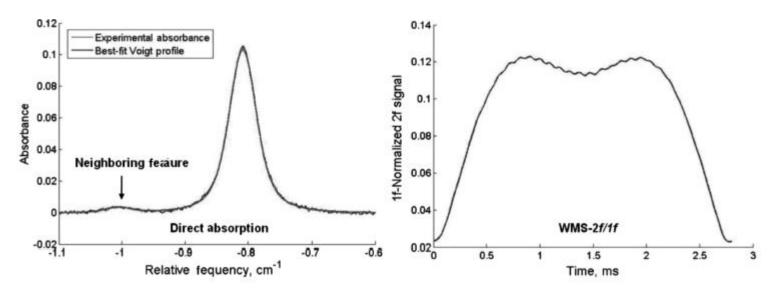








- E.g. Goldenstein et al.
 - Measured spectra of water vapor in UVa scramjet test facility
 - Small amplitude of second feature limits signal-to-noise ratio for direct absorption
 - 2f/1f ratio measurement provided consistently better signal-to-noise ratios, but both methods consistent with computational predictions



C.S. Goldenstein, I.A. Schultz, J.B. Jeffries and R.K. Hanson "Tunable Diode Laser Absorption Sensor for Measurements of Temperature and Water Concentration in Supersonic Flows," 49th AIAA Aerospace Sciences Meeting including the New Horizons Forum and Aerospace Exposition, Orlando FL, Jan 4–7, 2011, AIAA Paper 2011–1094.





Operation Mode	Expected Value	DA	WMS
11% Steam	700–1000 K	776 \pm 10 K	742 ± 9 K
(Combustor Entrance)	$11.4 \pm 0.2\% \text{ H}_2\text{O}$	$10.9 \pm 0.1\% H_2O$	$10.8 \pm 0.1\% \text{ H}_2\text{O}$
9% Steam	700–1000 K	860 \pm 30 K	831 ± 9 K
(Exit Plane)	$9\pm0.2\%~H_2O$	$9.1\pm0.2\%~H_2O$	$9.1 \pm 0.1\% H_2O$
12% Steam	700–1000 K	875 \pm 50 K	850 \pm 6 K
(Exit Plane)	$12 \pm 0.2\% \ H_2O$	$12.1 \pm 0.5\% \ H_2O$	$11.5 \pm 0.1\% \ H_2O$
H_2 -Air Combustion $\varphi = 0.33$	1800–2200 K	1802 ± 94 K	1765 ± 41 K
(Exit Plane)	13% H ₂ O	$12.8 \pm 0.5\% \ H_2O$	$13.3 \pm 0.3\% \ H_2O$

C.S. Goldenstein, I.A. Schultz, J.B. Jeffries and R.K. Hanson "Tunable Diode Laser Absorption Sensor for Measurements of Temperature and Water Concentration in Supersonic Flows," 49th AIAA Aerospace Sciences Meeting including the New Horizons Forum and Aerospace Exposition, Orlando FL, Jan 4–7, 2011, AIAA Paper 2011–1094.



Velocity Measurements



- Simplest quantity to measure in a high-speed flow
 - Measured through Doppler shift between beams with velocity components in two different directions relative to the flow

$$U = \frac{c\Delta v_{Dopp}}{v_{Source}}$$

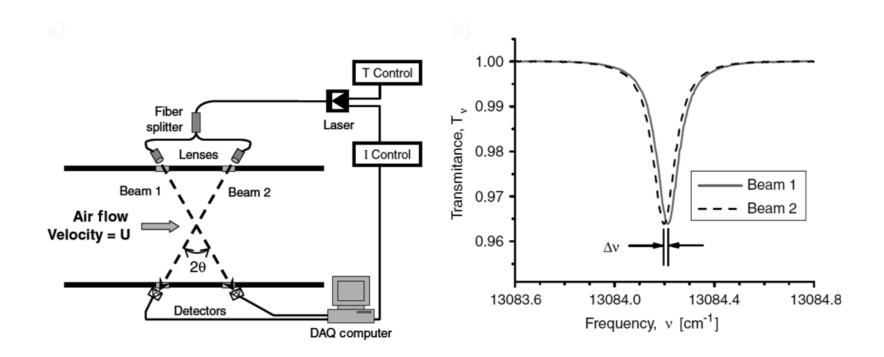
- Shift in the peak position relatively insensitive to amplitude noise.
- Shift typically calibrated to etalon measurements



Velocity Measurements



- E.g. Lyle et al., mass flux sensor based on measurements of density and velocity using oxygen A-band near 760-nm.
- Measured speed with time-averaged precision of 0.25 m/s.



K. H. Lyle, J. B. Jeffries and R. K. Hanson "Diode-laser Sensor for Air-mass flux 1: Design and Wind Tunnel Validation," AIAA Journal, 45 (9), 2204–2212, 2007.



Translational Temperature



• Can be determined through the Doppler width, but as $T_{trans} \propto \left(\frac{\Delta v_D}{v_0}\right)^2$, small errors in Doppler width have a significant effect on T

$$\frac{\Delta T}{T} = \frac{2\Delta(\Delta v_D)}{\Delta v_D}$$

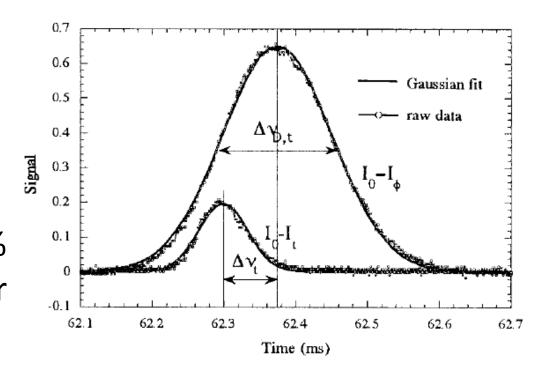
- E.g. An uncertainty in width measurement of 1.5% for a Doppler-broadened transition in the oxygen A-band will cause an uncertainty of 3% in temperature
- Uncertainty further increased in the presence of pressure broadening
- Measuring T through linewidth has the advantage of only requiring 1 transition for a measurement



Translational Temperature



- E.g. Measurements of temperature in an arcjet facility using an AR I line at 811.531 nm
- 12% uncertainty in width translated to 30% uncertainty in T_{trans} over 2000–1000 K



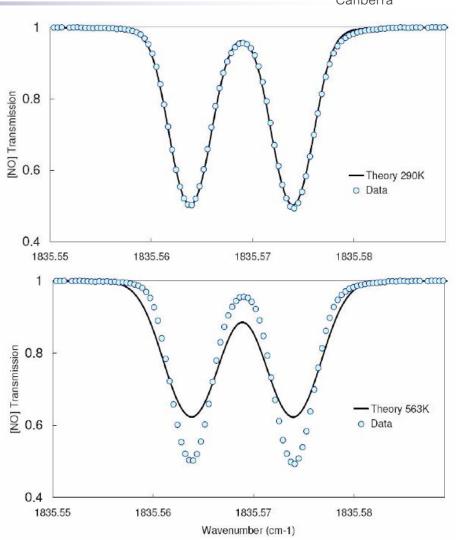
F-Y Zhang, K Komurasaki, T lida, and T Fujiwara, "Diagnostics of an Argon Arcjet Plume with a Diode Laser," Applied Optics, 38 (9), pp. 1814–1822, 1999.



Translational Temperature



- E.g. Measurements of NO translational temperature at 5.44 μm in the LENS I facility, using direct absorption
- Fit temperature of 290 K significantly different to the predicted temperature of 563K



R. A. Parker, T. Wakeman, M. MacLean, and M. Holden, "Measuring Nitric Oxide Freestream Concentration using Quantum Cascade Lasers at CUBRC," 44th AIAA Aerospace Sciences Meeting and Exhibit, AIAA Paper 2006-926, 2006.



Rotational Temperature



 Typically measured using the ratio of integrated absorbance a over two lines with different linestrength variations with T

$$a_j = P\chi_i LS_j$$

- for transition j of an absorbing species i
- L is the path length and S_j is the linestrength of the transition
- All quantities other than S_j are common to the two lines and divide out

$$\frac{a_1}{a_2} = \frac{S_1}{S_2} = \frac{S_1(T_0)}{S_2(T_0)} e^{-\frac{hc\Delta E_{rot}}{k} \left(\frac{1}{T_{rot}} - \frac{1}{T_0}\right)}$$

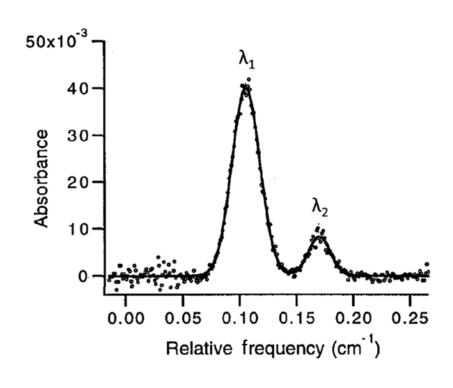
R. A. Parker, T. Wakeman, M. MacLean, and M. Holden, "Measuring Nitric Oxide Freestream Concentration using Quantum Cascade Lasers at CUBRC," 44th AIAA Aerospace Sciences Meeting and Exhibit, AIAA Paper 2006-926, 2006.



Rotational Temperature



- E.g. Wehe et al. measured H₂O rotational and translational temperature in the 10 MJ/kg Calspan 96-inch hypersonic shock tunnel freestream
- v1 + v3 band near 1396 nm (λ_2) and 1400 nm (λ_1)
- 8 kHz scan rate
- T_{rot} uncertainty of ± 2.3 % compared with T_{trans} uncertainty of ± 2.7 % and ± 6.4 % for the T_{trans} measurements on the two lines



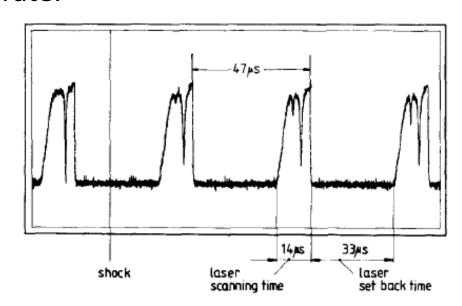
S. Wehe, D. S. Baer, and R. K. Hanson "Tunable Diode-laser Absorption Measurements of Temperature, Velocity, and H₂O in Hypervelocity Flows," 33rd Joint Propulsion Conference and Exhibit, Seattle, WA, AIAA Paper 97-3267, 1997.

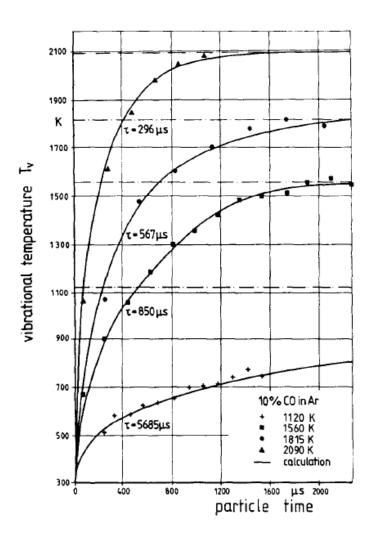


Vibrational Temperature



• E.g. Brandt and Roth measured T_{vib} and T_{trans} in CO in a reflected shock tube, using a lead salt laser operating at 2100-2200 cm⁻¹, at 20 kHz scan rate.





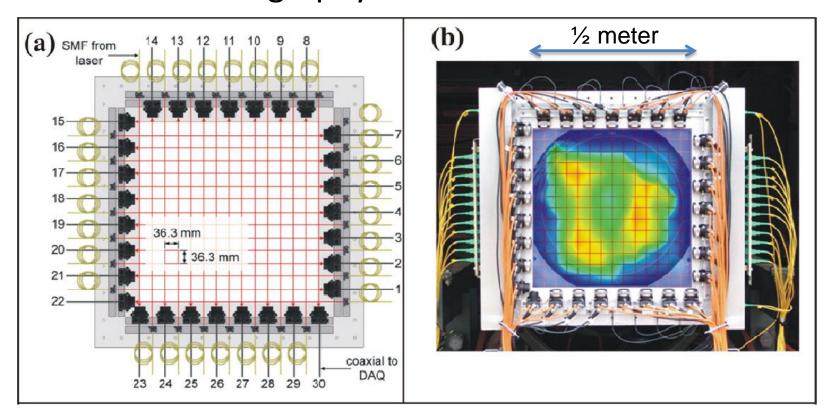
O. Brandt, and P. Roth, "Temperature Measurements behind Shock Waves using a Rapid Scanning IR-diode Laser," Physics of Fluids, Vol. 30, No. 5, pp. 1294–1298., 1987.



TDLAS Tomography



- Major limitation of TDLAS: path-averaged
 - Can do tomography



15x15 grid provides data at 225 points (36 mm grid)

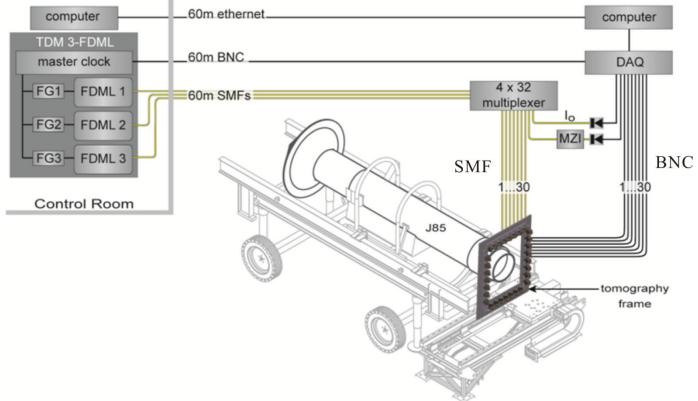
L. Ma, X. Li, S. T. Sanders, A. W. Caswell, S. Roy, D. H. Plemmons, and J. R. Gord, "50-kHz-rate 2D imaging of temperature and H₂O concentration at the exhaust plane of a J85 engine using hyperspectral tomography," Optics Express, Vol. 21, Issue 1, pp. 1152-1162, 2013



TDLAS Tomography



- General Electric J85 gas turbine engine
 - University of Tennessee Space Institute (UTSI)



Measure water and temperature at 50 kHz rate

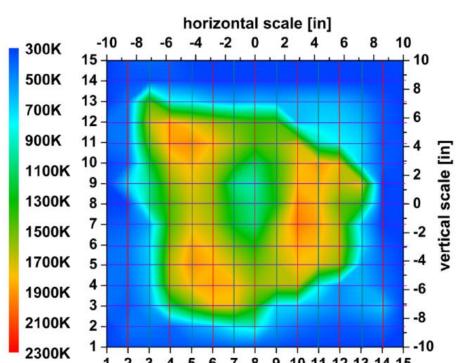
L. Ma, X. Li, S. T. Sanders, A. W. Caswell, S. Roy, D. H. Plemmons, and J. R. Gord, "50-kHz-rate 2D imaging of temperature and H₂O concentration at the exhaust plane of a J85 engine using hyperspectral tomography," Optics Express, Vol. 21, Issue 1, pp. 1152-1162, 2013



TDLAS Tomography Results

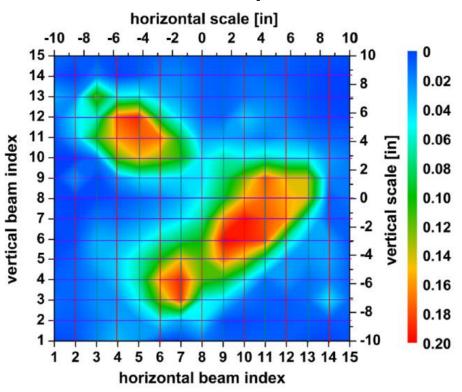






horizontal beam index

Water Vapor

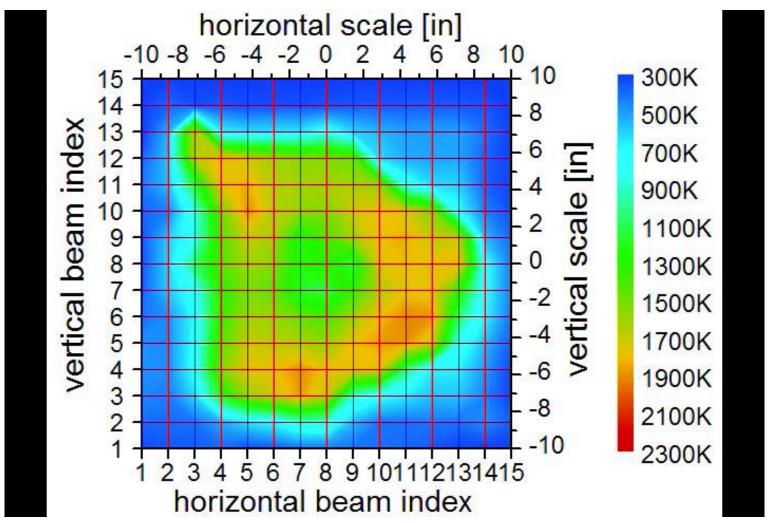


- Measurement is over ~0.5 meter square
 - Time resolution is 20 μsec (50 kHz)
 - Spatial resolution is ~36 mm



TDLAS Tomography Results





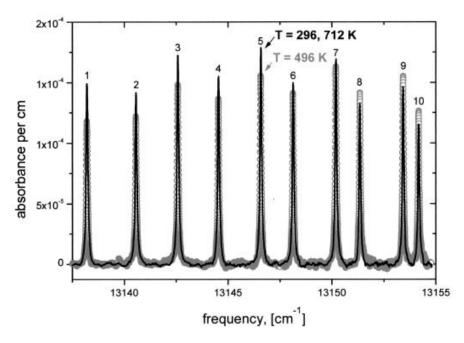
L. Ma, X. Li, S. T. Sanders, A. W. Caswell, S. Roy, D. H. Plemmons, and J. R. Gord, "50-kHz-rate 2D imaging of temperature and H_2O concentration at the exhaust plane of a J85 engine using hyperspectral tomography," Optics Express, Vol. 21, Issue 1, pp. 1152-1162, 2013



Using Spectral Information



- Many hypersonic environments (flight vehicles, test facilities) have limited optical access for tomography
 - Can use spectral information to infer spatial variations of temperature.



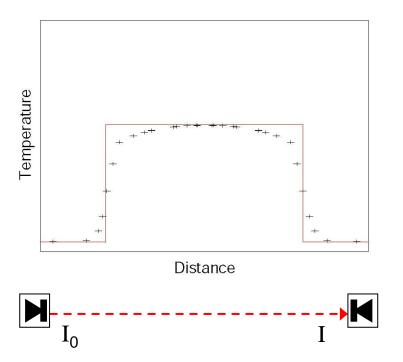
S.T. Sanders, J. Wang, J.B. Jeffries, and R. K. Hanson. "Diode-laser absorption sensor for line-of-sight gas temperature distributions." *Applied Optics* 40,(24) 4404-4415., 2001.

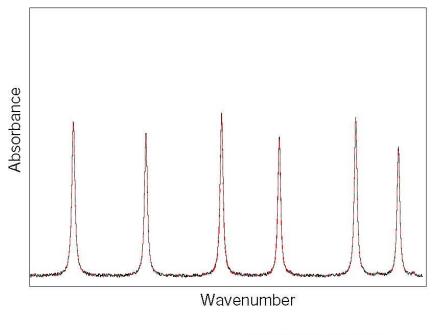


Extracting Line-of-Sight Temperatures



- Example: Temperature in a tube furnace using a single VCSEL line of sight
 - The 'distribution technique' assumes a priori knowledge of the distribution shape.





'experimental' spectrum — theoretical spectrum – – -

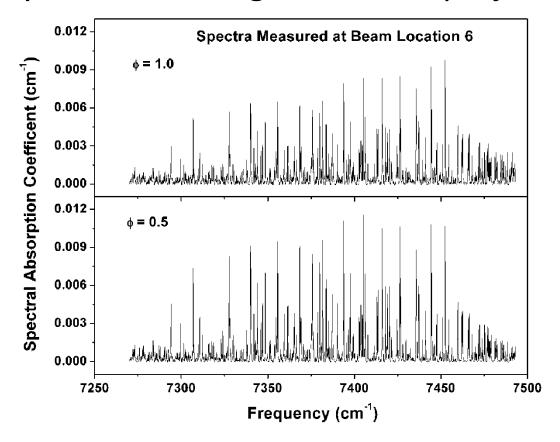
L. C. Webster, S. O'Byrne, A. F. P. Houwing, "Determination of Temperature Distributions in Air using a Scanning Vertical Cavity Surface-Emitting Laser," *Proc.* 4th Australian Conference on Laser Diagnostics in Fluid Mechanics and Combustion, Adelaide, Australia, 2005.



TDLAS Hyperspectral Tomography



 Using hyperspectral sources, can gain spectral images over many lines, reducing number of projections



L. Ma, W. Cai, A. W. Caswell, T. Kraetschmer, S. T. Sanders, S. Roy, and J. R. Gord, "Tomographic imaging of temperature and chemical species based on hyperspectral absorption spectroscopy," Optics Express 17(10), 8602–8613, 2009.

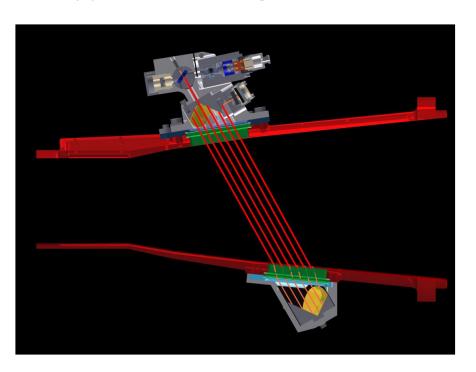


Flight-Testing TDLAS Systems



 Small size and power requirements have allowed TDLAS systems to be used in hypersonic flight tests



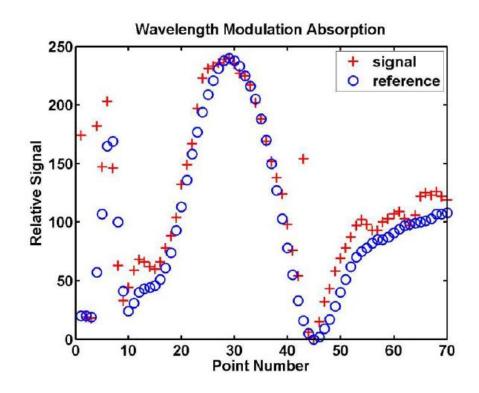


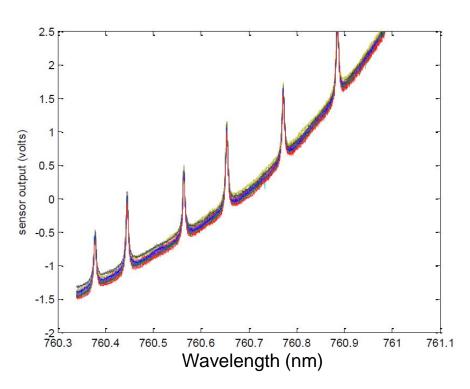
T. Barhorst and S. Williams, "Development of an In-Flight Non-Intrusive Mass Capture System," *45th AIAA/ASME/SAE/ASEE Joint Propulsion Conference & Exhibit. AIAA, Denver, Colorado, USA, 2009.*J. Kurtz, M. Aizengendler, Y. Krishna, and S. O'Byrne, S (2015) "Flight Test of a Rugged Scramjet-Inlet Temperature and Velocity Sensor," *AIAA SciTech*, 5-9 January, Kissimee, Florida, USA.



Flight-Testing TDLAS Systems USEN







M. S. Brown, and T.F. Barhorst. "Post-flight analysis of the diode-laser-based mass capture experiment onboard HIFiRE flight 1." In *Proceedings of 17th AIAA International Space Planes and Hypersonic Systems and Technologies Conference paper AIAA-2011-2359*. 2011.

J. Kurtz, M. Aizengendler, Y. Krishna, and S. O'Byrne, S (2015) "Flight Test of a Rugged Scramjet-Inlet Temperature and Velocity Sensor," *AIAA SciTech*, 5-9 January, Kissimee, Florida, USA.



Conclusions

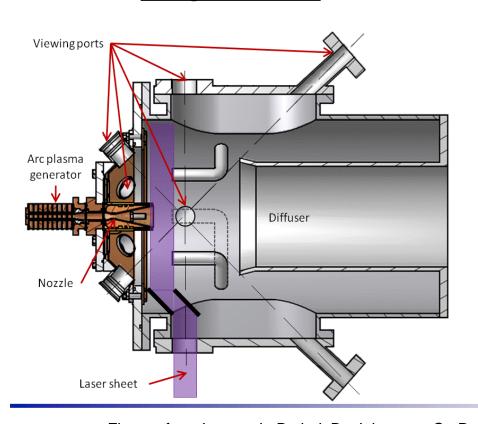


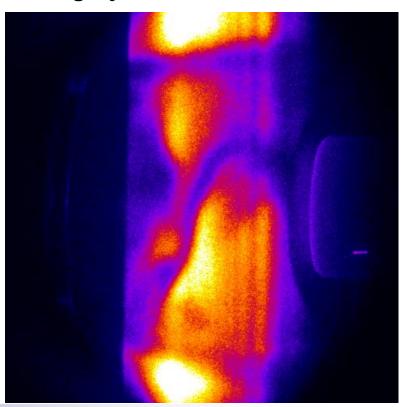
- TDLAS is a reliable and well established nonintrusive measurement technique, capable of precise pathaveraged measurements of velocity, density and trans/rot/vib temperatures
- Availability of telecoms lasers and detectors makes it comparatively economical
- Path-averaging disadvantages can be mitigated using tomography or additional spectral information
- Particularly valuable for flight-test applications and time-resolved online facility monitoring
- Rapid development in mid-IR sources and detectors will significantly expand applications



Intro to Planar Laser-Induced Fluorescence for Hypersonic Nonequilibrium Flows

Brett Bathel, NASA Langley Research Center, Virginia, USA Paul Danehy, NASA Langley Research Center, Virginia, USA <u>Craig Johansen</u>, The University of Calgary, Canada





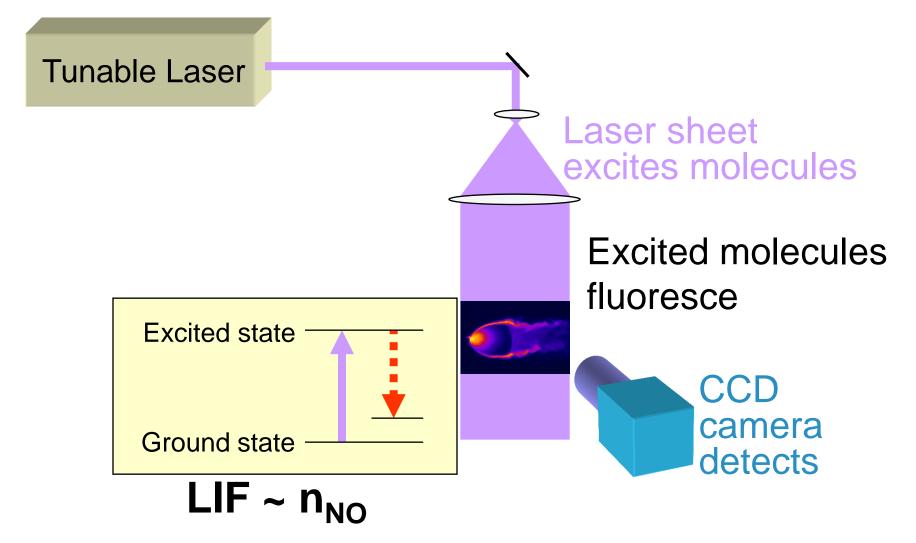
Figures from Inman, J., Bathel, B., Johansen, C., Danehy, P., Jones, S., Gragg, J., and Splinter, S., (2013) "Nitric oxide planar laser-induced fluorescence measurements in the Hypersonic Materials Environment Test System," *AIAA Journal*, Vol. 51, No. 10, pp. 2365-2379





Planar Laser-Induced Fluorescence (PLIF)







PLIF can probe nonequilibrium



- Commonly used in <u>equilibrium</u> environments
- Useful probe for thermal non-equilibrium:
 - Translational temperature
 - Rotational temperature
 - Vibrational temperature (often $T_{vib} \neq T_{rot} \approx T_{tran}$)
 - Species specific:
 - Different species can have different temperatures (especially vibrational temperatures)
- Can measure, quantify species in <u>chemical</u> non-equilibrium (eg. NO in shock tunnels)



LIF Theory (Two-Level Model)



2 Energy of absorbing species at excited state (2)

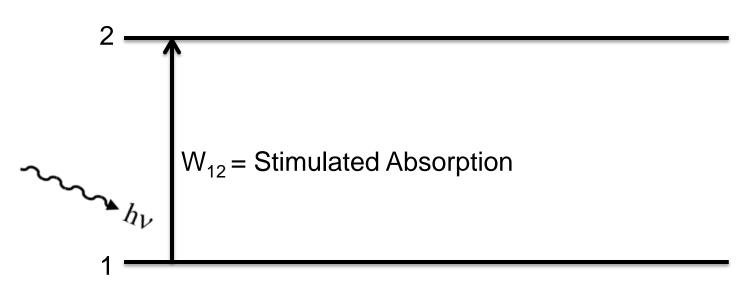
Energy of absorbing species at ground state (1)

Assumptions:

- A. There are only two important states to consider (ground state and excited state). Other levels (rotational and vibrational) are ignored.
- B. Prior to excitation, population of absorbers in excited state is negligible $(N_2=0)$







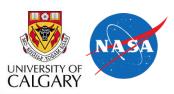
An incident photon from the light source (e.g. laser) is absorbed and sends some of the ground state population to the excited state

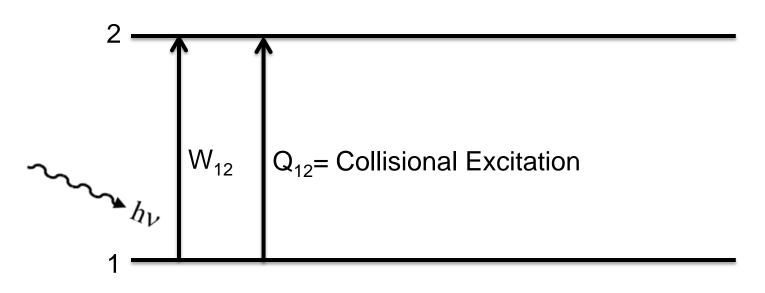
$$\frac{dN_1}{dt} = -N_1 W_{12}$$

$$\frac{dN_2}{dt} = N_1 W_{12}$$

Population rate equations (incomplete at this point)







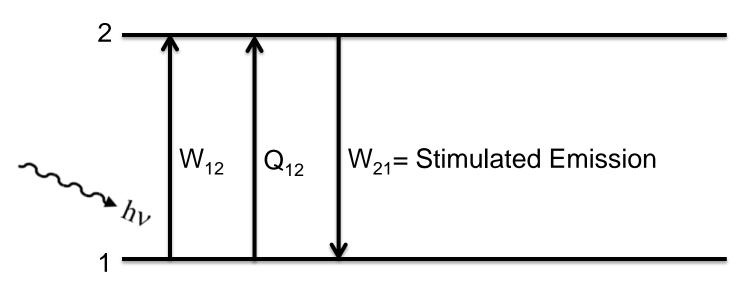
The excited state population is further increased by collisional excitation.

$$\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12})$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12})$$







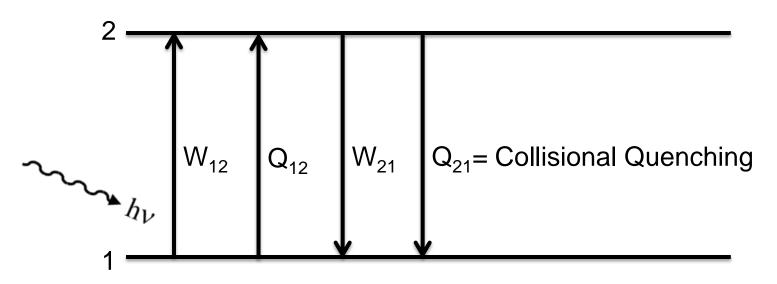
Some of the excited state population returns to the ground state through stimulated emission

$$\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2W_{21}$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2W_{21}$$





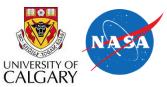


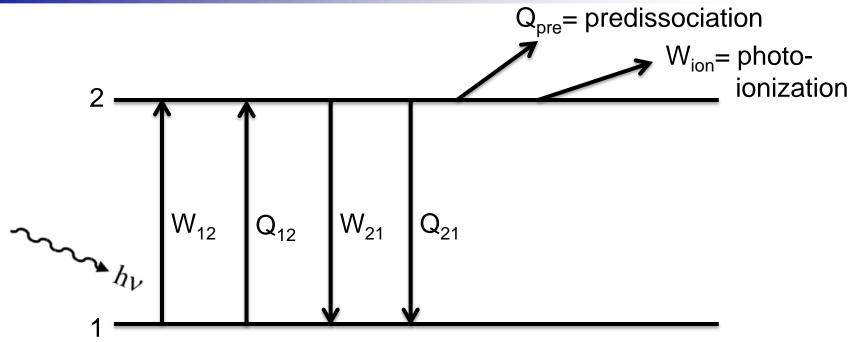
Some of the excited state population returns to the ground state through collisions (self or with other atoms/molecules)

$$\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21})$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21})$$







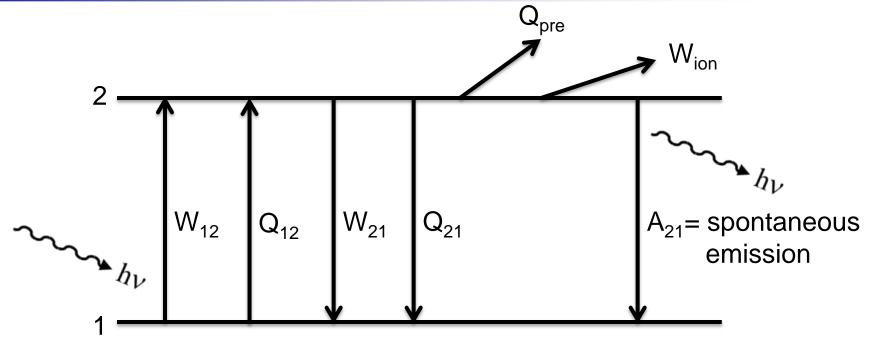
The excited state population gets depleted through dissociation and ionization (without returning to the ground state)

$$\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21})$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{\text{pre}} + W_{\text{ion}})$$







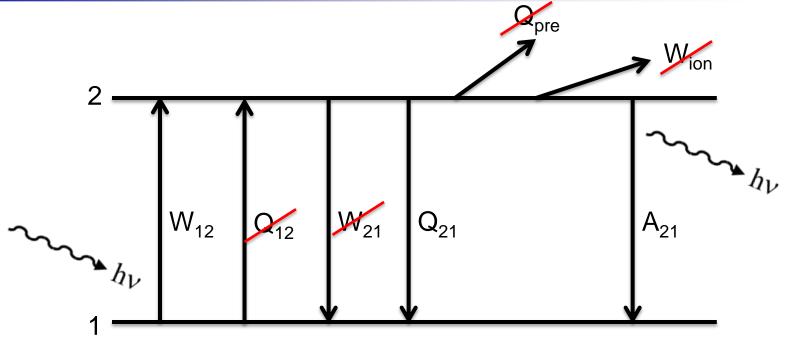
Finally, some of the excited population return to the ground state via spontaneous emission and emit a photon (fluorescence)

$$\frac{dN_1}{dt} = -N_1(W_{12} + Q_{12}) + N_2(W_{21} + Q_{21} + A_{21})$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{pre} + W_{ion} + A_{21})$$







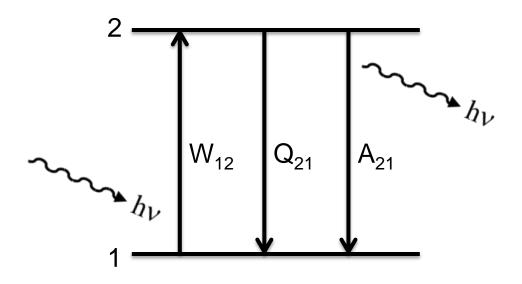
Fortunately, for many applications, Q₁₂, W₂₁, Q_{ion}, and Q_{pre} are negligible.

$$\frac{dN_1}{dt} = N_2(W_{21} + Q_{21} + A_{21}) - N_1(W_{12} + Q_{12})$$

$$\frac{dN_2}{dt} = N_1(W_{12} + Q_{12}) - N_2(W_{21} + Q_{21} + Q_{pre} + W_{ion} + A_{21})_{129}$$







Simplification of rate equation: $\frac{dN_1}{dt} = -\frac{dN_2}{dt} = N_2(Q_{21} + A_{21}) - N_1W_{12}$

Mole fraction of absorbing species

Conservation of mass for absorbing species:

 $N_1 + N_2 = N_s = \chi_s f_B N_T$

Number density of the absorbing species in the ground state prior to excitation

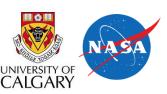
Boltzmann fraction

Total number

density



Steady State Two-Level Model



Steady state assumption (e.g. continuous wave laser):

$$\frac{dN_1}{dt} = -\frac{dN_2}{dt} = 0$$

detection

- Solve for N₂: $N_2 = \frac{\chi_s f_B N_T W_{12}}{W_{12} + O_{21} + A_{21}}$
- Weak excitation assumption: $W_{12} \ll (Q_{21} + A_{21})$
- rate:
- Integrate spontaneous emission $\int_{\hat{a}}^{\iota_{det}} N_2 A_{21} dt = N_2 A_{21} t_{det}$

volume

excited

solid angle

Include the optics of detection to get LIF signal:

$$S_{LIF} = \chi_{s}f_{B}N_{T}W_{12}\left(\frac{A_{21}}{Q_{21}+A_{21}}\right)t_{det}V\frac{\Omega}{4\pi}\eta$$
 total number of photons collected fluorescence yield (Φ) collection efficiency efficiency

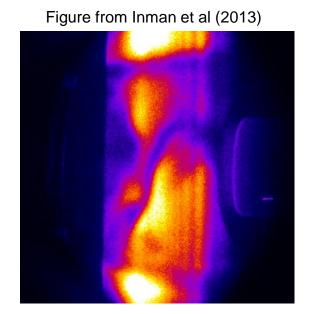


Concentration of Absorbing Species



$$S_{LIF} = \underline{\chi_s N_T} f_B W_{12} \Phi t_{det} V \frac{\Omega}{4\pi} \eta$$

- To first order, S_{LIF} is proportional to the concentration of the absorbing species
- Qualitative PLIF visualization often used to show the spatial distribution of absorbing species
- (see the text for measurement strategies for quantitative concentration)



 $S_{LIF} \propto \chi_{NO} N_T$



Boltzmann Fraction

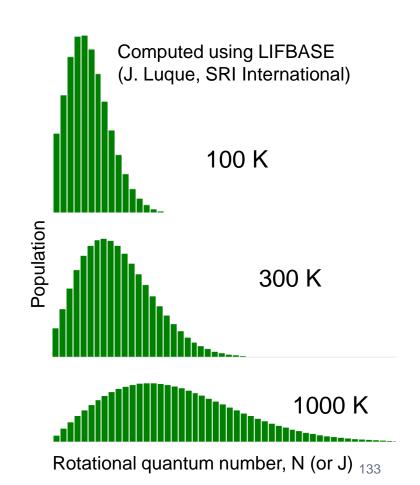


$$S_{LIF} = \chi_s N_T \underline{f_B} W_{12} \Phi t_{det} V \frac{\Omega}{4\pi} \eta$$

Rotational Boltzmann fraction

$$f_B = \frac{g_j e^{-E_j/k_B T}}{\sum_j g_j e^{-E_j/k_B T}}$$

- a function of temperature only
- Peak at 300 K is $^{\sim}3\%$ for N=7 (J=7.5)
- Vibrational and electronic Boltzmann fractions
 - Most molecules in ground state for T < 2000 for atoms, diatomics



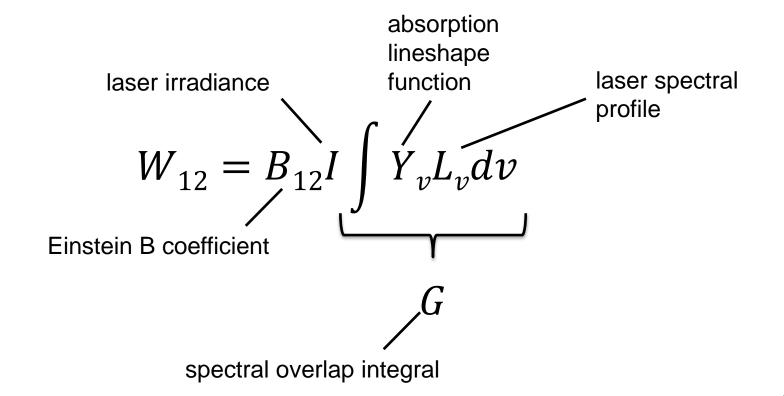


Stimulated Absorption



$$S_{LIF} = \chi_s N_T f_B \underline{W}_{12} \Phi t_{det} V \frac{\Omega}{4\pi} \eta$$

W₁₂ is the probability of an <u>absorption</u> transition per sec





Fluorescence Yield



$$S_{LIF} = \chi_{S} N_{T} f_{B} B_{12} I G \underline{\Phi} t_{det} V \frac{\Omega}{4\pi} \eta$$

The fluorescence yield is affected by collisional quenching

$$\Phi = \frac{A_{21} - Q_{21}}{Q_{21} + A_{21}}$$

Probability of an atom/molecule $\Phi = \frac{A_{21}}{Q_{21} + A_{21}}$ undergoing spontaneous emission per second (Einstein A coefficient)

Probability of a quenching collision per second

Collisional quenching is hard to predict since it depends on many factors

$$Q_{21} = N_T \sum_i \chi_i \sigma_{s,i} \nu_{s,i}$$

$$Q_{21} = N_T \sum_i \chi_i \sigma_{s,i} v_{s,i}$$

$$\begin{cases}
N_T = P/k_B T \\
\chi \text{ is mole fraction} \\
\sigma \text{ is quenching cross section} \\
\text{v is mean relative velocity}
\end{cases}$$



Steady State S_{LIF} dependencies



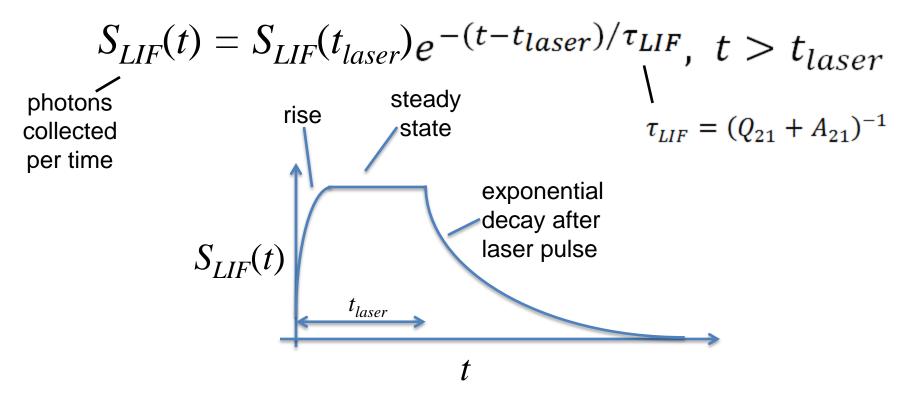
$$S_{LIF} \propto \chi_s f_B(T) B_{12} IG(\chi_s, P, T, U) \Phi(\chi_s, \chi_i, P, T) t_{det}$$

- LIF signal is sensitive to T, P, U, χ_s , χ_i
 - Can potentially measure these parameters
 - Complicates measurement of a single parameter
- Making quantitative measurements with LIF involves finding a way to make measurement sensitive only to the parameter being measured



Time Dependent S_{IIF} Solution





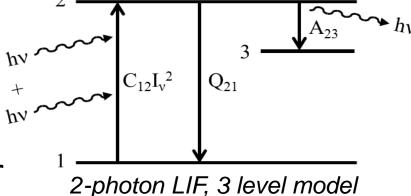
- Laser pulse length is typically ~10 ns
- LIF lifetimes can be a few ns to 100's of ns or longer
 - If you can measure lifetime, you can measure Q!
 - Can measure velocity from long lived decay (MTV)



More Complicated LIF Models



- More complete LIF theories and phenomena:
 - Saturation effects (see manuscript)
 - Line shapes
 - overlap integral, G, to be discussed below
 - Multi-level LIF models
 - 2 photon absorption
 - 3, 4, 5 level models
 - Predissociation
 - Rotational energy transfer
 - Vibrational energy transfer



For further reference:

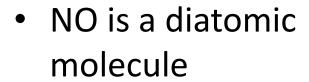
A. C. Eckbreth, *Laser Diagnostics for Combustion Temperature* and Species 2nd Ed., Combustion Science & Technology Book Series, Volume 3, Taylor & Francis, New York, 1996



A real molecule: NO

states





- Electronic
- Vibration
- Rotation
 - Not shown
- Absorption and fluorescence take place between electronic states
 - Show rotational and vibrational structure

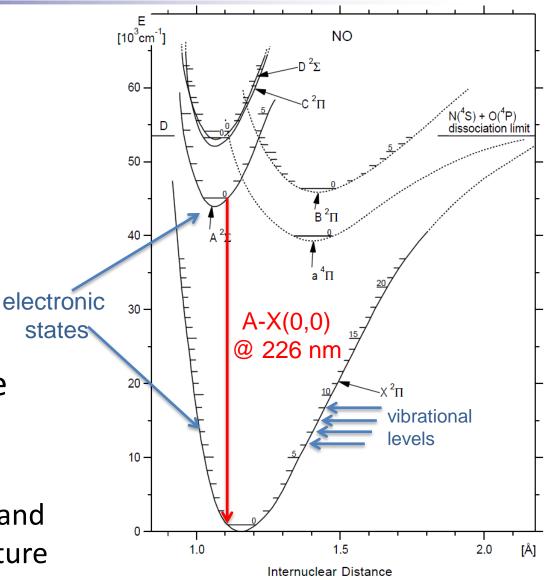
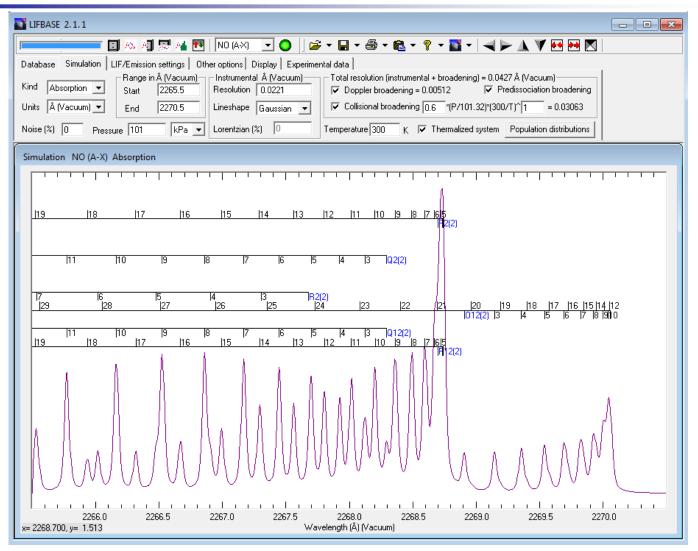


Figure A2.1. Selected potential energy curves that show the electronic structure of NO. In this experiment, we probed transitions in the A-X band of NO [adapted from (Scheingraber and Vidal,1985



LIFBASE Simulation of NO





LIFBASE freeware by J. Luque, SRI International

lifbase@yahoo.com

- LIF Excitation Scan between 226.6-227 nm, 1 atm, 300 K
 - Lines all have band names (O, P, Q, R, S) and N's or J's (rot quant #)



LIF Temperature Measurements

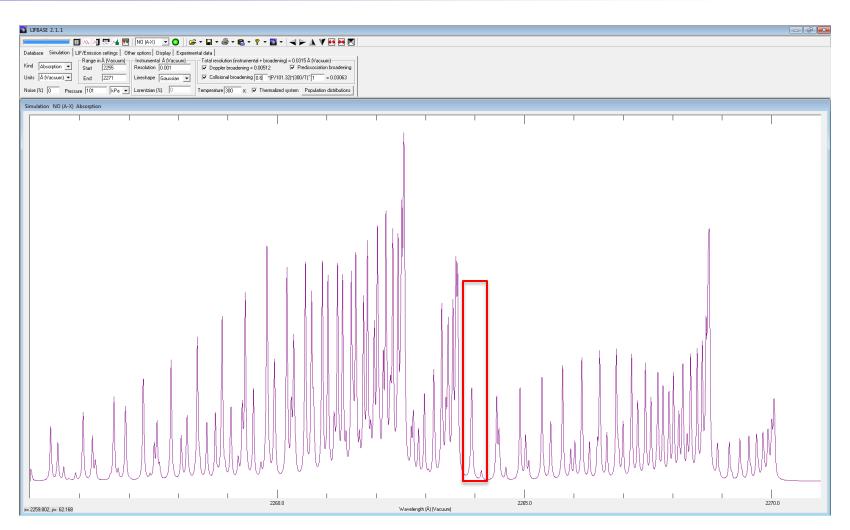


- Rotational Temperature
 - Ratio of 2 or more rotational lines
 - Describe general case
 - Example in a turbulent base flow
- Vibrational Temperature
 - Ratio of 2 or more vibrational lines
 - Example of freestream characterization
 - Boltzmann plot, where more than 2 lines used
- Translational Temperature



Rotational Lines of NO, 300 K



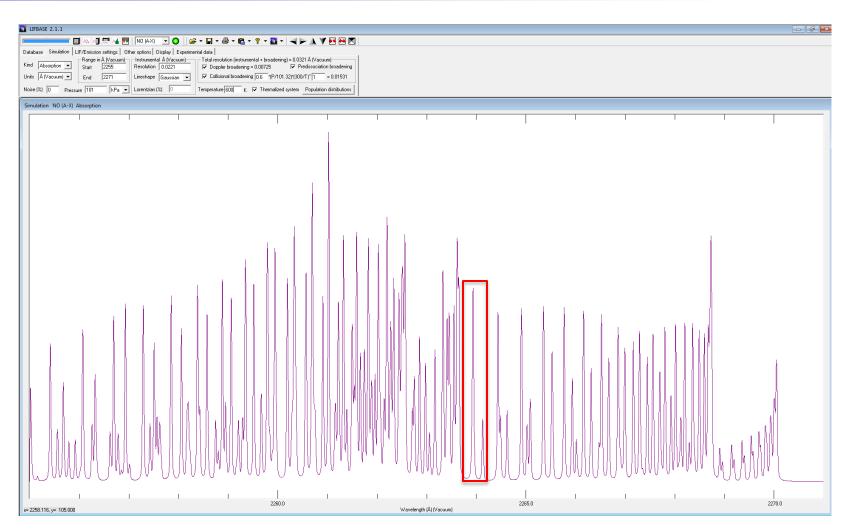


LIF Excitation Scan between 225-227 nm, 1 atm, 300 K



Rotational Lines of NO, 600 K





LIF Excitation Scan between 225-227 nm, 1 atm, 600 K



LIF: Rotational Temperature, T_{rot}





Recall:

$$S_{LIF} \propto \chi_s f_B(T) B_{12} IG(\chi_s, P, T, U) \Phi(\chi_s, \chi_i, P, T) t_{det}$$

 Obtain LIF or PLIF on two different rotational lines of a molecule: i and j. Take ratio, R:

$$\frac{S_{LIF,i}}{S_{LIF,j}} = R = C \frac{B_{12,i}E_i}{B_{12,j}E_j} \frac{(2J_i+1)\exp[-F_{J,i}/k_BT_{rot}]}{(2J_j+1)\exp[-F_{J,j}/k_BT_{rot}]}$$

- Where:
 - C is a constant
 - -E is the laser energy (in mJoules)
 - -J is the rotational quantum number
 - $-F_I$ is the energy of the state
 - $-k_R$ is Boltzmann's constant

 Ω , χ_s , η , G, V, N_T and Φ (including Q_{21}) cancel out!



LIF: Rotational Temperature, T_{rot} UNIVERSITY OF





$$T_{rot} = \frac{-\Delta E_{rot}}{k_B \ln \left[CR \frac{B_{12,j} E_j (2J_j + 1)}{B_{12,i} E_i (2J_i + 1)} \right]}$$

• Where:

$$\Delta E_{rot} = (F_{J,i} - F_{J,j})$$

Temperature sensitivity:

$$\frac{\delta T_{rot}}{T_{rot}} = \frac{k_B T_{rot}}{\Delta E_{rot}} \frac{\delta R}{R}$$

- Suggests to maximize ΔE_{rot} (as long as signals still strong) to minimize error in temperature, δT_{rot}
 - Should choose widely separated states: e.g. J = 3.5 & 35.5



Typical Strategies for T_{rot}



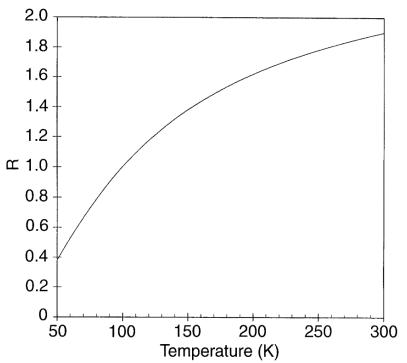
- Typically two approaches:
 - Steady laminar flow
 - Obtain images on one J, then scan laser to another J
 - Ratio images, determine temperature
 - Turbulent flow
 - Two lasers, two cameras (Cumbersome! Expensive!)
 - Acquire two images nearly simultaneously, different J's
 - Need to do this because ratio is a nonlinear function of temperature: $\frac{S_{LIF,i}}{S_{LIF,j}} = R = C \frac{B_{12,i}E_i}{B_{12,j}E_j} \frac{(2J_i+1)\exp[-F_{J,i}/k_BT_{rot}]}{(2J_j+1)\exp[-F_{J,j}/k_BT_{rot}]}$
 - Typical single-shot temperature measurement precision is ~20% at flame temperatures (Seitzman, 1994)
 - If you use 1 laser/1 camera, → bias errors in turb. Flows
 - (E. R. Lachney, and N. T. Clemens, "PLIF imaging of mean temperature and pressure in a supersonic bluff wake," Experiments in Fluids, 24, pp. 354-363, 1998.)
 - Average many measurements to reduce uncertainty

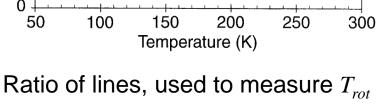


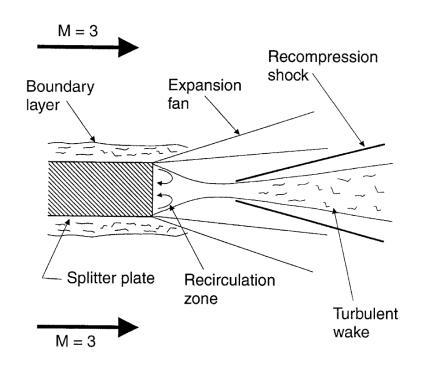
Single laser/camera for T_{rot} in turbulent flow



- Lachney and Clemens (1998) used 1 laser / 1 camera to map mean T_{rot} in a base flow.
- NO seeded N₂ at Mach 3
- Chose: J = 8.5 and J = 10.5







Turbulent supersonic wake flow

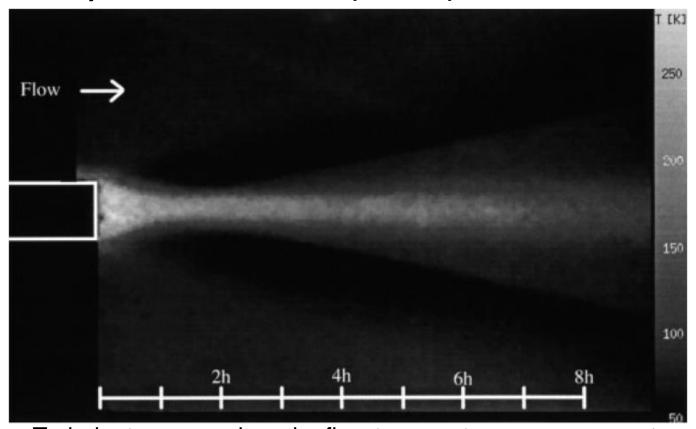


Single laser/camera for T_{rot} in turbulent flow





Lachney and Clemens (1998):



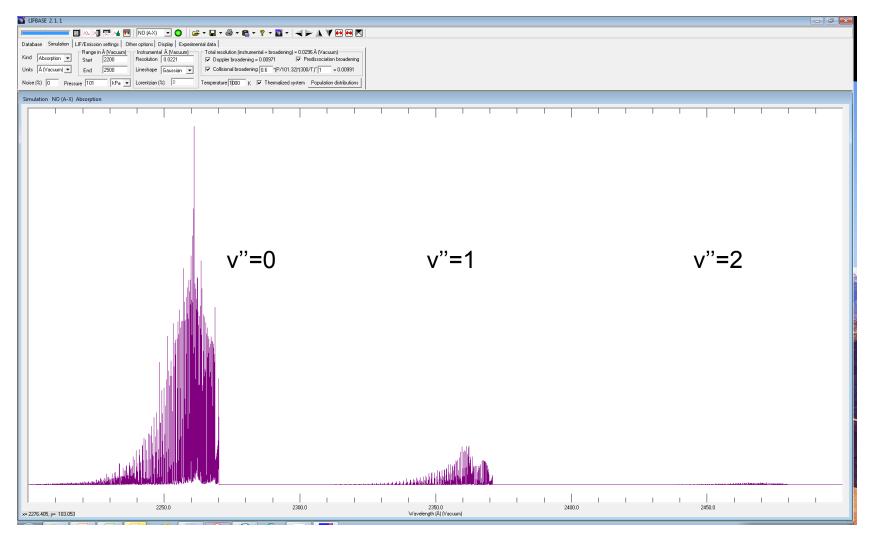
Turbulent supersonic wake flow temperature measurement Agreed with temperatures inferred from probe measurements to within 11%

E. R. Lachney, and N. T. Clemens, "*PLIF imaging of mean temperature and pressure in a supersonic bluff wake*," Experiments in Fluids, 24, pp. 354-363, 1998



Vibrational Bands of NO



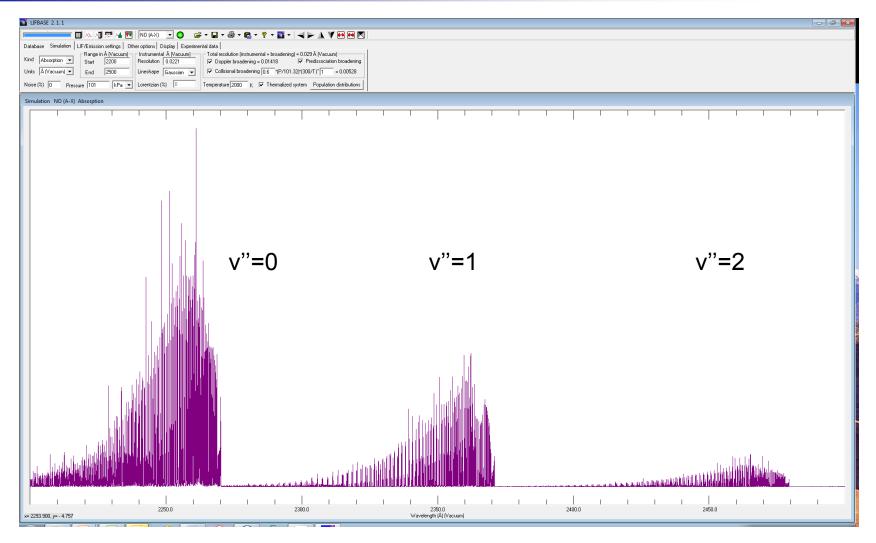


- Three vibrational bands: T = 1000 K
 - Vibrational bands have quantum number, v



Vibrational Bands of NO





• Three vibrational bands: T = 2000 K



Vibrational Temperature T_{vib} Measurement



vibrational

- A similar approach can be made to obtain vibrational temperature measurements
 - Typically excite the same rotational line (J) in 2 or more vibrational bands ($F_i \approx \text{constant}$)
 - Can do 2 line measurements as before
 - Can use a Boltzmann Plot:
 - Graph:

$$\ln \left[\frac{S_{LIF,i}}{B_{12,i}E_i(2J_i+1) \exp\left[-F_{J,i}/k_BT_{rot}\right]} \right]$$

/ energy of states probed versus $G_{v,i}$:

• Slope is: $-1/(k_B T_{vib})$

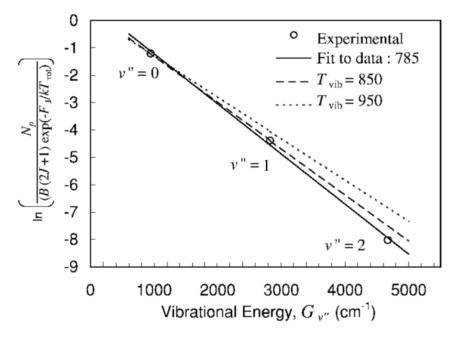
If $F_j \approx$ constant then T_{vib} can be determined independent of T_{rot}

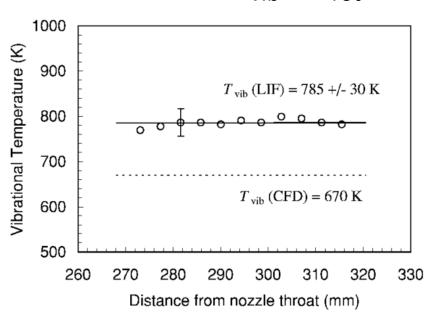


Vibrational Temperature T_{vib} Measurement



• Vibrational temperature measured in a nozzle exit flow verifying vibrational nonequlibrium $(T_{vib} \neq T_{rot})$





 $T_{rot} \approx 400 \text{ K}$ and decreasing with distance

P. C. Palma, P. M. Danehy, and A. F. P. Houwing, "Fluorescence Imaging of Rotational and Vibrational Temperature in Shock-Tunnel Nozzle Flow," AIAA Journal, 41(9), September 2003

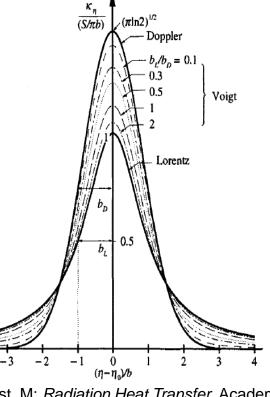


Translational Temperature



- Can measure T_{trans} (and P) from width and shapes of spectral lines
- Spectral lines have a shape
 - Molecular motion leads to:
 - Doppler Broadening (inhomogeneous)
 - Gaussian shape
 - FWHM: $\Delta v_D = \frac{v_0}{c} \sqrt{\frac{8 \ln(2) k_B T}{m}}$
 - Collisions lead to:
 - Pressure Broadening (homogeneous)

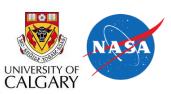
 - Lorentzian shape FWHM: $\Delta v_P = \frac{P}{101,325} \cdot \left[2\gamma \cdot \chi_i \cdot \left[\frac{295}{T} \right]^{0.75} + \dots \right]$
 - Combination is: Voigt
 - Convolution (if $\Delta v_P, \Delta v_D$ comparable)
 - Formulas in manuscript



Modest, M: Radiation Heat Transfer, Academic Press, Elsevier Science, USA, 2003 153



Translational Temperature

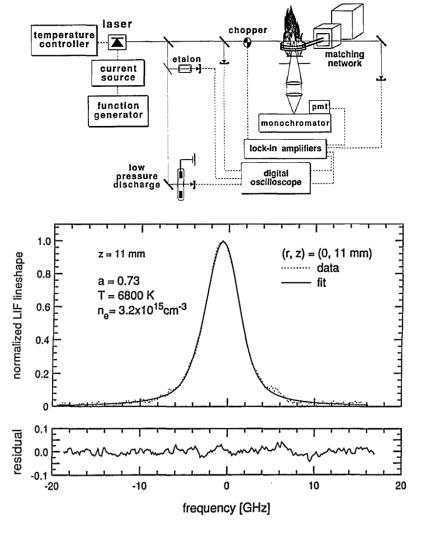


 If using a very narrow linewidth laser...

$$\Delta v_L << \Delta v_P, \Delta v_D$$

...can neglect laser width

- Semiconductor diode laser
- Scan laser frequency across a transition
 - Argon atom at 810.4 nm
 - Turbulent inductively coupled plasma (ICP) torch
- Fit measured LIF spectrum
 - Have homogeneous (Stark) and Doppler broadening
 - ${\color{blue}-}$ Determine $n_e^{}$ and T



D. S. Baer, H. A. Chang, and R. K. Hanson, "Fluorescence diagnostics for atmospheric-pressure plasmas using semiconductor lasers," Journal of the Optical Society of America B, 9(11), pp. 1968-1978, November, 1992



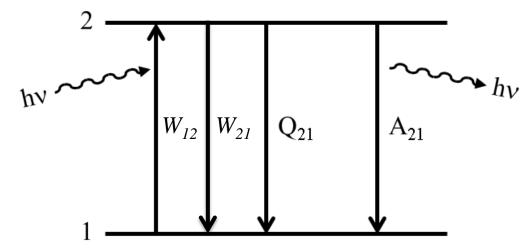
Species Concentrations



- Problem: How to deal with unknown Q_{21} ?
- Solutions:
 - Saturated LIF: $(W_{12} + W_{21}) \gg (Q_{21} + A_{21})$
 - Q_{2I} is negligible compared to W's
 - Hard to achieve
 - Predissociation
 - $Q_{pre} >> Q_{21}$
 - Measure τ_{HF}
 - Determine Q_{21} from au_{LIF}



- Raman/Rayleigh/LIF (Sandia and DLR)
- Counter-propagating beams, take ratio (Versluis, 1997)
- Potential problems: absorption, rad. trapping





LIF Advantages/Disadvantages



Advantages

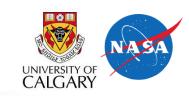
- Relatively easy to make planar measurements (PLIF)
- Provides flow visualization simultaneously
- Relatively easy to perform
- Can probe many different parameters (T, V, concentration)
 - Velocity measurements (MTV) can have with 1-2% precision

Disadvantages

- Precision of single-shot temperature measurements
 (~20%) is not good compared to CARS (2-3%) or LITA (1%)
- Difficult to do quantitative concentration measurements, especially planar



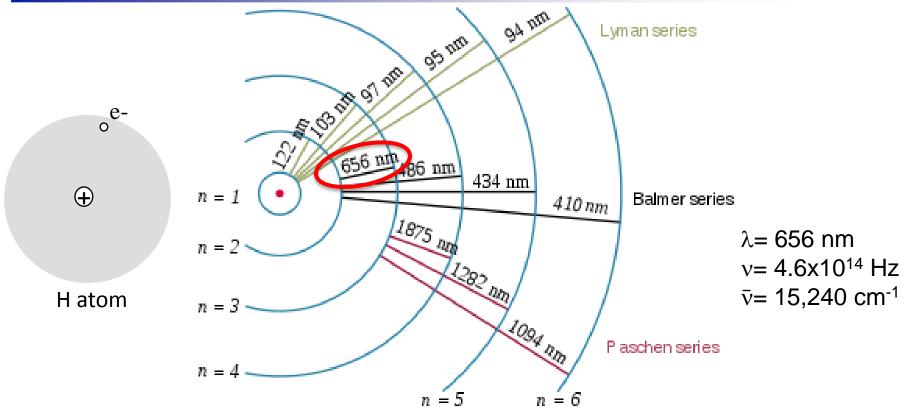
PLIF Backup Slides





LIF Theory: Atoms





- Two level model
 - e.g. Hydrogen atom
- Photon energy = $h\nu$

$$-c = \lambda v$$

wavenumbers = \overline{v} = $1/\lambda$ cm⁻¹

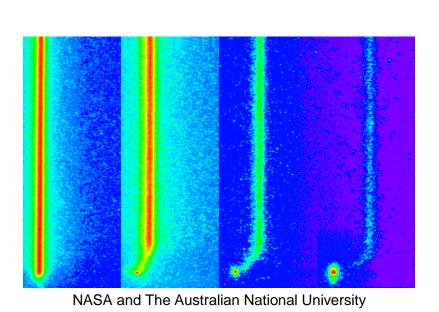
Hydrogen atom energy levels (from Wikipedia, "hydrogen spectral series") http://creativecommons.org/licenses/by-sa/3.0/deed.en

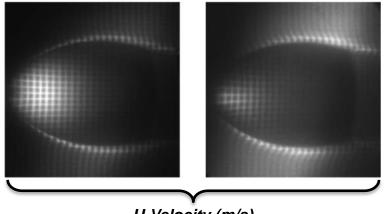


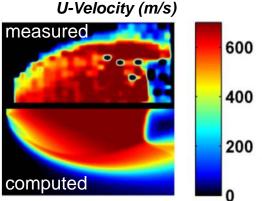
Introduction to LIF Velocimetry Techniques for Hypersonic Nonequilibrium Flows



<u>Brett Bathel</u>, NASA Langley Research Center, Virginia, USA Paul Danehy, NASA Langley Research Center, Virginia, USA Craig Johansen, The University of Calgary, Canada









Texas A&M



Outline: Velocimetry Techniques



- LIF-Based Velocimetry Techniques
 - Doppler shift
 - Based on laser frequency relative to absorption line
 - Molecular tagging velocimetry (MTV)
 - aka Flow tagging velocimetry
 - Time of flight
 - Single-laser method requires lifetime long enough for flow to move while light is being emitted
 - Summary
- Other Techniques
 - Particle: Particle Image Velocimetry (PIV), Laser Doppler Velocimetry (LDV)
 - Interference/Scatting: Laser-Induced Thermal Acoustics (LITA)
 - Schlieren: Density Tagging Velocimetry (DTV)
 - Scattering: Rayleigh





Doppler Shift Velocimetry



Doppler Shift Velocimetry



The Doppler shift:

$$\left| \left| \left(\left(\left(\sum_{i=1}^{n} \nu_{0} \right) \right) \right| \right| = \frac{U}{c} \nu_{0}$$

Wikipedia "Doppler Shift" http://creativecommons.org/licenses/by-sa/3.0/deed.en

- Can be used to measure velocity with LIF
 - Relative shift between laser and absorbing molecules
 - Angle of detection does not matter for LIF
- The overlap integral, G, which describes the overlap of the laser's spectrum with a line
 - L_{v} is laser's spectral shape, typically modeled as Gaussian or Lorentzian
 - Y_{ν} is the transition's absorption line shape, can be shifted by Doppler shift

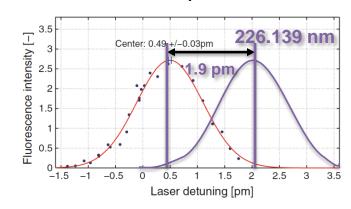
$$G = \int L_{\nu} Y_{\nu} d\nu$$



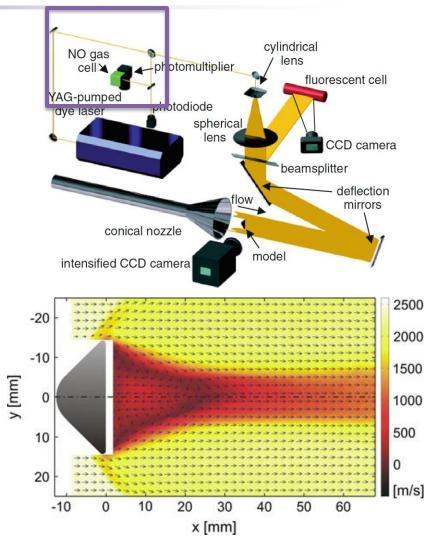
Doppler-based LIF Velocimetry



- Direct laser sheet into the flow
- Acquire images or signal at different laser frequencies
 - Choose frequencies near an absorption line
 - Measure absorption lineshape at each point
 - Reference data acquired simultaneously



- Measure from two different directions to get two different velocity components
- Do need to consider pressure shift



R. Hruschka, S. O'Byrne, and H. Kleine, "Two-component Doppler-shift fluorescence velocimetry applied to a generic planetary entry probe model," Experiments in Fluids, 48, pp. 1109-1120, 2010



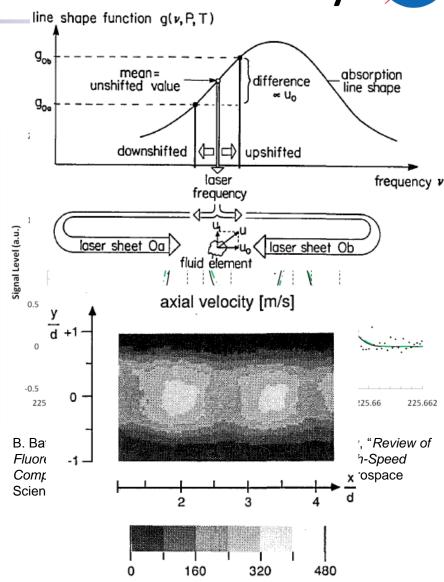
Doppler-based LIF Velocimetry



- Self-referenced tuning Doppler velocimetry
 - Does not require reference cell measurement

$$- \nu_0 = \frac{\nu_f + \nu_r}{2} \to U = \frac{c}{\cos \theta} \cdot \frac{(\Delta \nu / 2)}{([\nu_f + \nu_r] / 2)}$$

- Laser passed through measurement volume, followed by a delay line that returns beam along original path
- Requires high-speed measurement device (e.g. photomultiplier tube) to resolve forward and return signals
- Fixed frequency (single-shot)
 - Potential for time resolved velocity
 - Less accurate estimating Doppler shift with few measurements



B. Hiller and R. Hanson, "Simultaneous planar measurements of velocity and pressure fields in gas flows using laser-induced fluorescence," Applied Optics, 27(1), January 1, 1988.



Doppler Shift Velocimetry



Benefits

- Capable of providing 1- or 2-component velocity maps
- Relatively easy to implement

Drawbacks

- Typically not time resolved
- Typically requires reference measurement
- Spectral shift resulting from increased pressure needs to be accounted for
- Requires a gas 'seed' to either be naturally present or introduced into the flow





Molecular Tagging Velocimetry





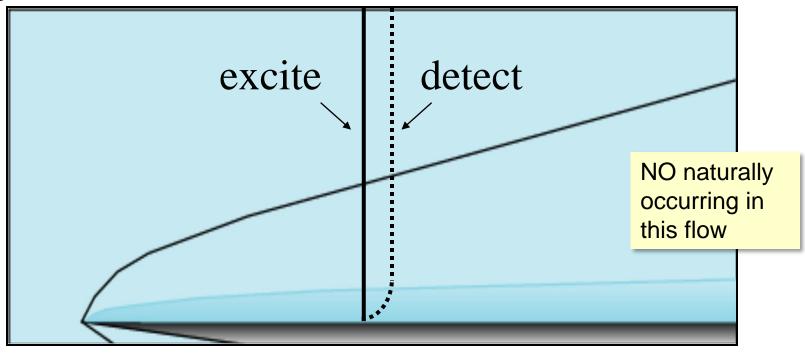
- Biacetyl (Hiller et al, 1984; Koochesfahani, 2007)
- Acetone (Lempert, 2002)
- NO (Danehy, 2003; Hsu, 2009; Bathel, 2011)
- I₂ (Balla, 2013)
- N₂ using FLEET (Femtosecond laser electronic excitation tagging) (Michael, 2011)
 - Does not require seeding
 - Does require an expensive fs laser
- LIF lifetime must be long enough so molecules still emit light after (slightly) moved



LIF Molecular Tagging Velocimetry (MTV)



Single-laser LIF MTV



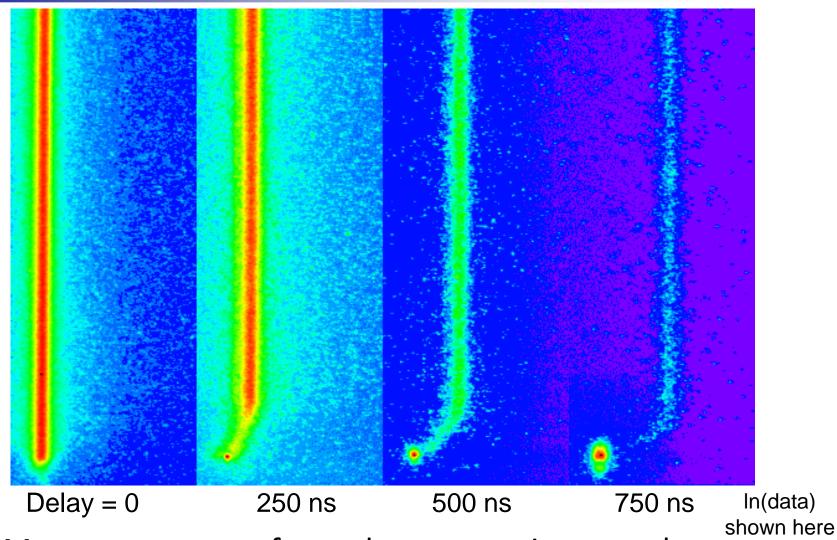
- Boundary layer: slow moving gas near surface
 - Important: heat transfer, drag, separation, etc.
- Instantaneous measure of 1 velocity component
 - Can be extended to 2 or 3 components

P. M. Danehy, S. O'Byrne, A. F. P. Houwing, J. S. Fox, and D. R. Smith, "Flow-Tagging Velocimetry for Hypersonic Flows Using Fluorescence of Nitric Oxide," AIAA Journal, 41(2), February 2003



MTV: Delayed Images

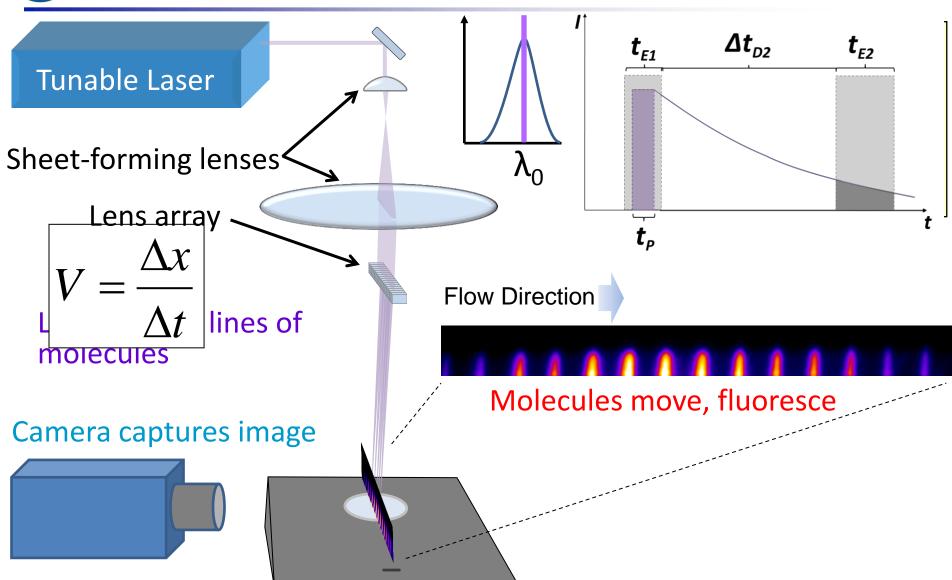




Measurements performed on successive tunnel runs

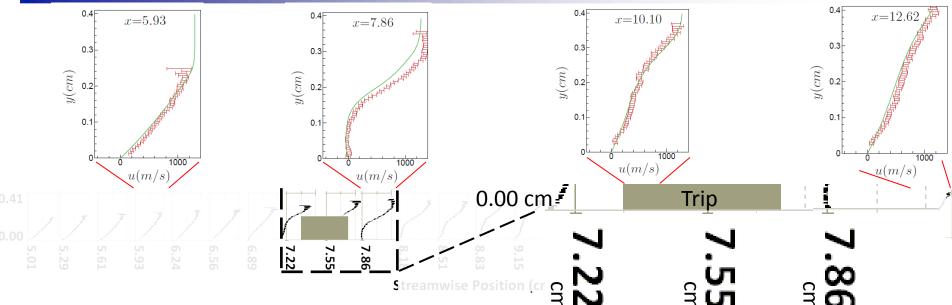












Velocity Measurement

- Instantaneous (<1 μs), single-component measure of 25 profiles simultaneously
- Developed thorough uncertainty analysis methodology
- Data used in subsequent CFD study by Iyer et al. of Univ. of Minnesota (AIAA 2011-566)

B. F. Bathel, P. M. Danehy, J. A. Inman, S. B. Jones, C. B. Ivey, C. P, and Goyne, "Velocity Profile Measurements in Hypersonic Flows Using Sequentially Imaged Fluorescence-Based Molecular Tagging," AIAA Journal, 49(9), September 2011



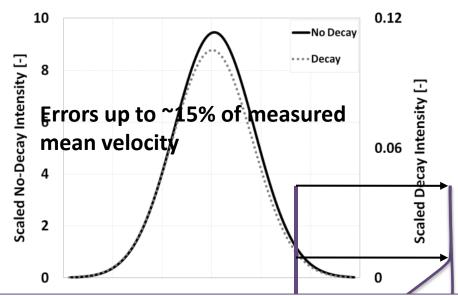


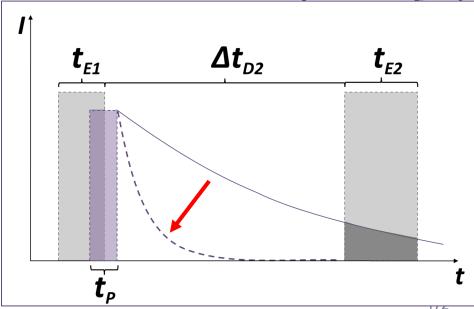
Analysis

- Uncertainties in mean: as good as 3% of freestream (~1000 m/s) for 38 images
- Modeled error from intensity decay, exposure duration, motion blur
- Error from velocity component parallel to MTV profiles quantified

Study conclusions

- Velocity gradients can bias measurement
- Scatter off of the model surface limited proximity of measurement to the wall
- Limited to low-pressure conditions
- Need higher pressure capability for higher Reynolds number required to study laminar-to-turbulent transition at least on this short model



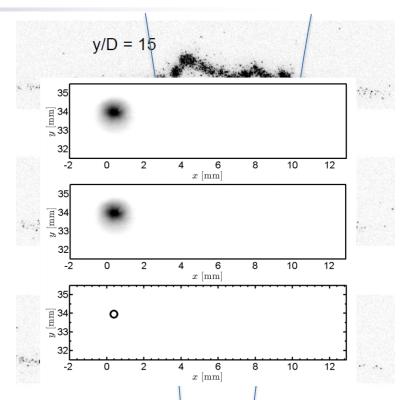




Single-laser MTV: FLEET



- Simple principle:
 - Works with N₂ seed
 - Femtosecond laser is focused down to a line or spot
 - Gas glows for 10's of μ s
- Originally developed at Princeton:
 - Air jet at room temperature, atmospheric pressure
 - Non-linear process
- Recently applied to transonic cryogenic flow at NASA Langley
 - Tracking of spot provided 2-D velocimetry
 - ~1 m/s accuracy and precision



R. Burns, P. Danehy, S. Jones, B. Halls, and N. Jiang, "Application of http://welocimetry in the NASA Langley 0.3-Meter Transonic Cryogenic Turne AIAA Paper 2015-2566, 31st AIAA Aerodynamic Measurement Technology and Ground Testing Conference, June 2015.

N₂ Jet





Benefits

- Instantaneous measurement
- Capable of providing velocity information along a line (1-component) or at grid points (2-component)
- 'Seedless' methods available
- Relatively simple to setup

Drawbacks

- Reduced spatial resolution compared to Doppler shift approach
- Operational limits often dictated by fluorescence lifetime
- Potential for model damage
- Potential for altering thermodynamic state of gas



Multilaser MTV



- Typically, one laser generates a line, series of lines or a grid pattern by, ionization (LEI¹²⁶⁻¹²⁸), vibrational excitation (RELIEF¹²⁹⁻¹³¹), photolysis, bleaching or other process. Additional laser(s) read out pattern.
 - Example: Excimer laser at 193 nm+ $N_2+O_2 \rightarrow NO$
 - Air Photolysis and Recombination Tracking (APART)
 - Dam et al, Optics Letters, 26 (1), pp. 36-38 2001
- A list of partner species used in the photolysis writing and reading process includes:

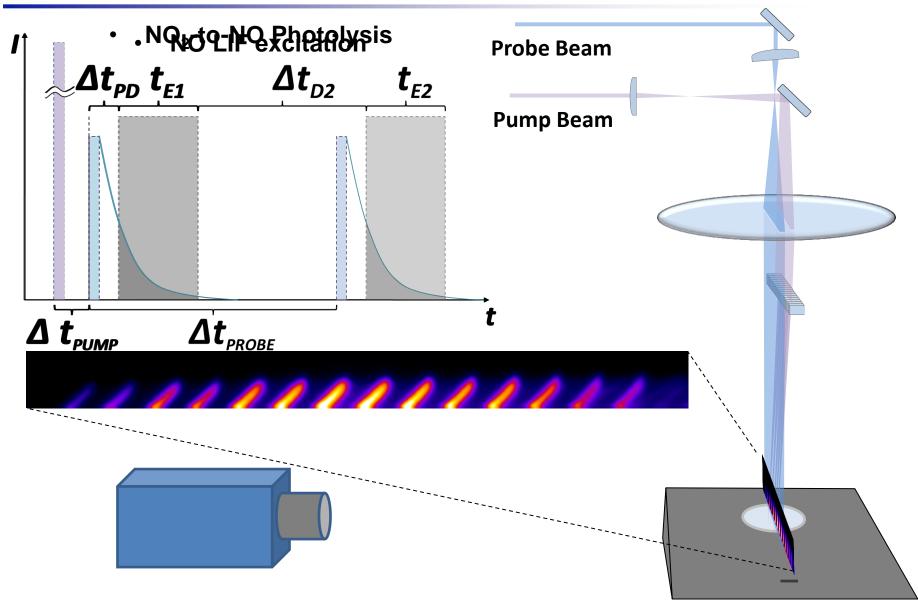
```
H_2O-OH_2^{133-139} N_2O-NO_3^{140} O_2-O_3^{141,142} N_2/O_2-NO_3^{143-146} and NO_2-NO_3^{116,147-154}
```

- Method can use air constituents (N₂/O₂, O₂, N₂) or can be seeded (H₂O, N₂O, NO₂, Na, etc.).
 - We have used $NO_2 \rightarrow NO$ to study transition



Multilaser MTV

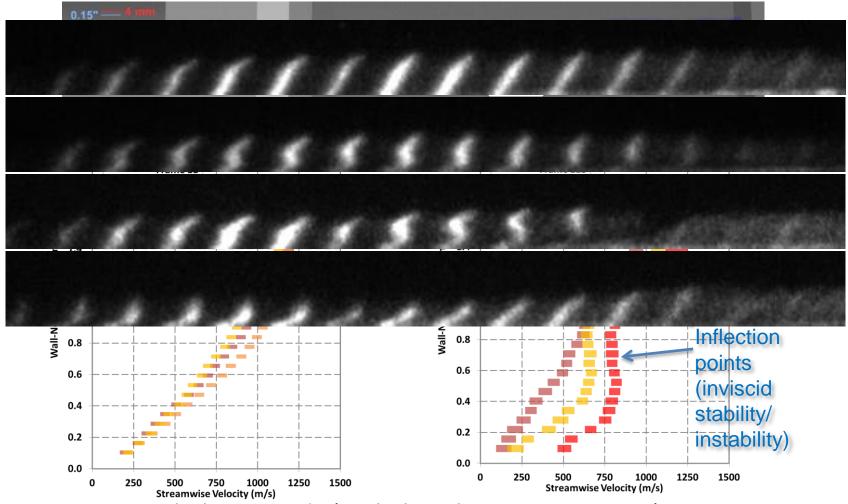






Velocimetry: 1-mm Tall Trip (centerline)





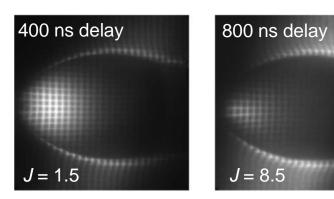
- Transition-to-turbulence study (Bathel et al. AIAA-2011-3246)
 - Reynolds number requirement necessitated higher operating pressures
 - Signal lifetime too short for single-laser NO LIF MTV



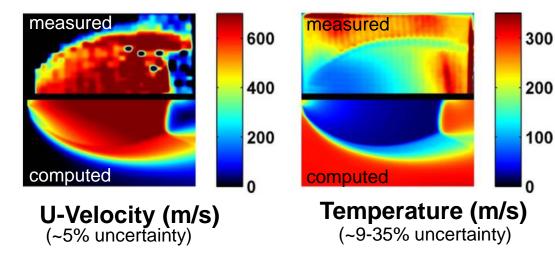
3 laser MTV: measure *u*, *v*, *T*



- Texas A&M has used 3 laser technique with crossed beam pattern for 2-component velocity and temperature in an underexpanded N₂ jet flow with NO₂:
 - VENOM: vibrationally excited nitric oxide monitoring
 - Excite to v' = 1 state



Raw data images



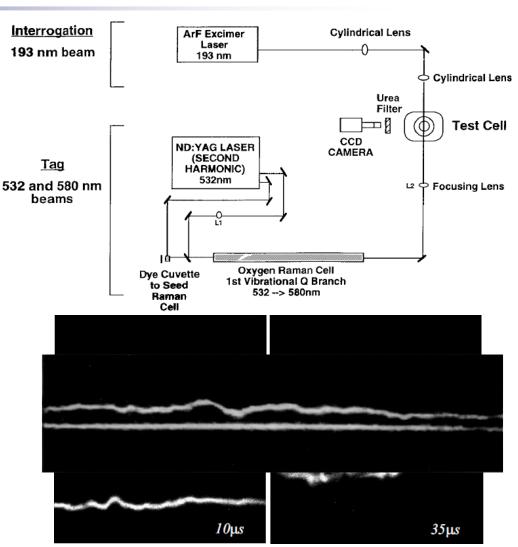
R. Sánchez-González, R. Srinivasan, R. D. W. Bowersox, and S. W. North, "Simultaneous velocity and temperature measurements in gaseous flowfields using the vibrationally excited nitric oxide monitoring technique: a comprehensive study," Applied Optics, 51(9), pp. 1216-1228, March 20, 2012



Multilaser MTV: Unseeded



- Air Photolysis And Recombination **T**racking (APART)
 - Nitric oxide generated in unseeded air via dissociation by UV excimer laser beam
 - NO then probed with LIF excitation wavelengths
- Raman Excitation and Laser-Induced **E**lectronic **F**luorescence (RELIEF)
 - O₂ vibrational excitation via Raman pumping
 - UV Excimer laser used to probe 1st vibration state of oxygen
 - Works for flows where T < \sim 750 K





Multi-laser MTV



Benefits

- Capable of providing instantaneous velocity along a line (1-component) or at grid points (2-component)
- Several 'seedless' methods available
- Not limited by fluorescence lifetime (works in high P)

Drawbacks

- Reduced spatial resolution compared to Doppler shift approach
- More complicated setup requires multiple lasers
- Potential for model damage
- Altering thermodynamic state of gas





Summary



Velocimetry Techniques



- Introduced three fluorescence-based techniques
 - Doppler shift velocimetry
 - Single-laser molecular tagging velocimetry
 - Multi-laser molecular tagging velocimetry
- Provided representative examples for each of the techniques
- Discussed benefits and drawbacks for each approach
- Following presentation will provide a more in-depth discussion of laser-induced fluorescence used for many of these MTV techniques.



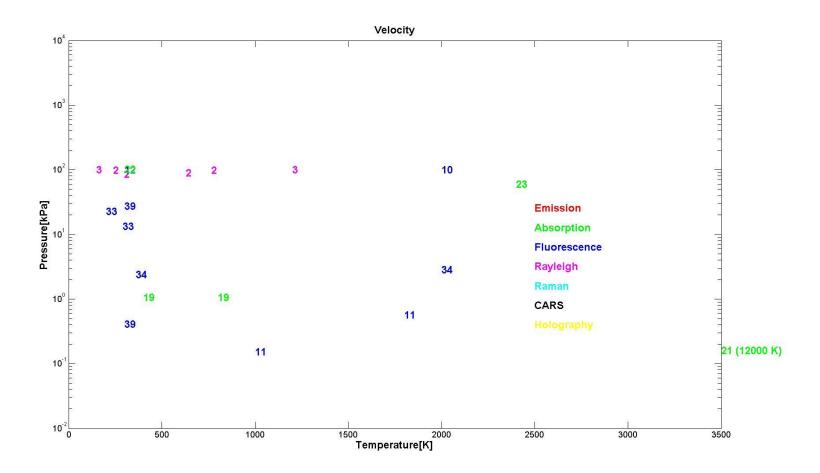


Backup Charts



Velocity

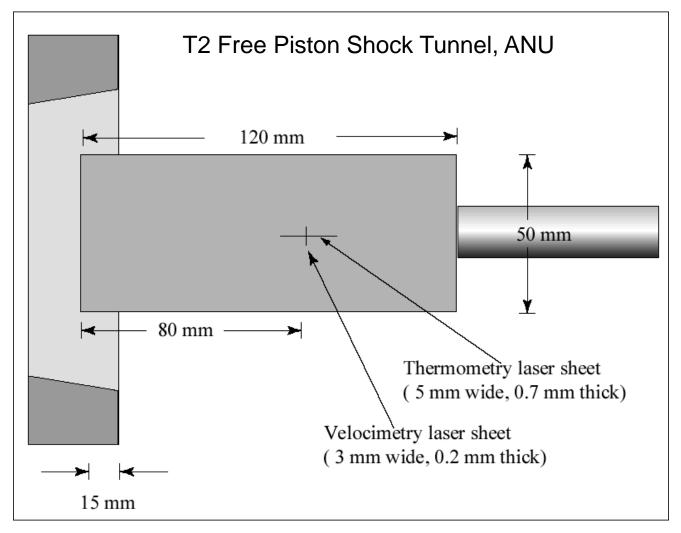






Experimental Setup: Top View



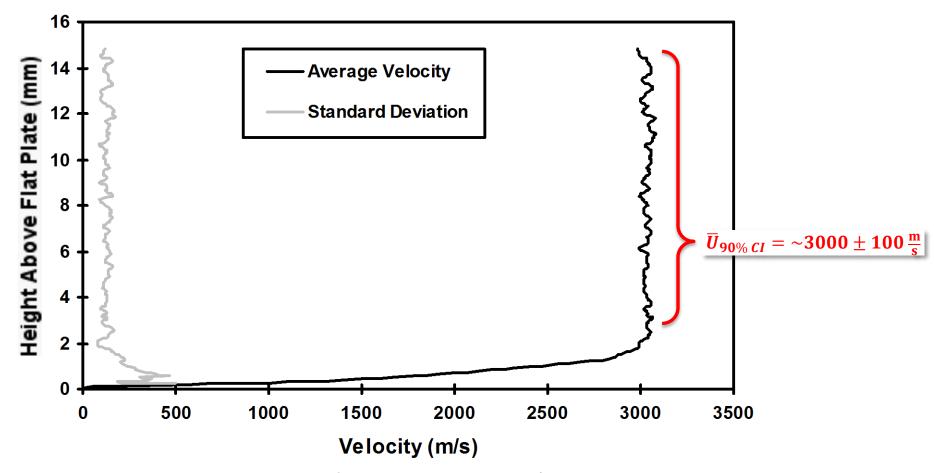


Velocity ~ 3000 m/s; Mach Number = 7, laminar boundary layer



Average of Single-Shot Measurements





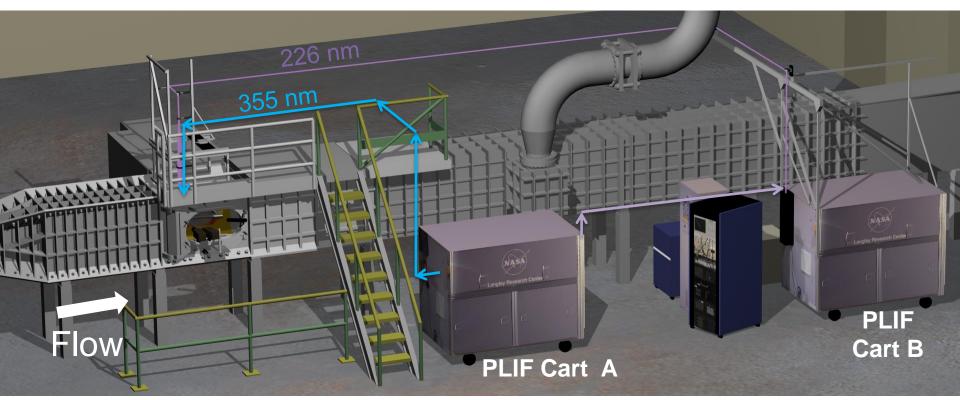
- Freestream velocity is uniform at 3035±60 m/s.
- 95% boundary layer thickness is 1.4±0.1 mm.
- Single shot measurement precision: ~60 m/s out of ~3000 m/s (2%)
 - spatially averaged uncertainty (freestream region) ~100 m/s (3%)



Three-Laser MTV ($NO_2 \rightarrow NO$ velocimetry)

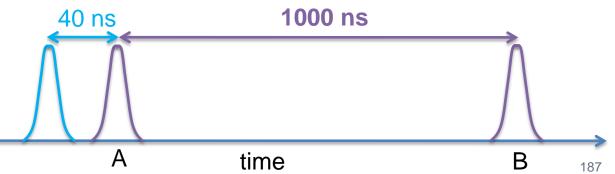


(for details of velocimetry method, see Bathel et al, AIAA-2011-3246 and others incl. TAMU¹⁴⁹, OSU¹⁵⁰, etc.)



 NO_2 +355 nm \rightarrow NO

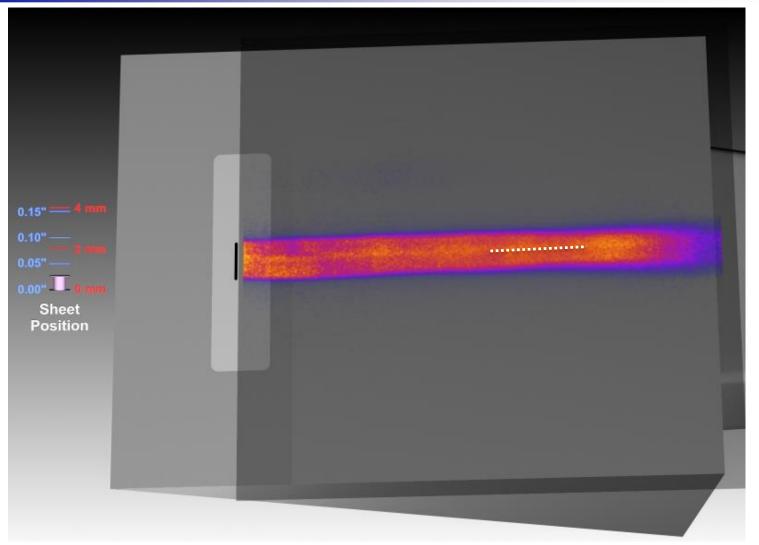
Write lines of NO into NO₂ seeded in the flow





Flow Visualization: No trip





 $PA = 20^{\circ}$ mid-Re

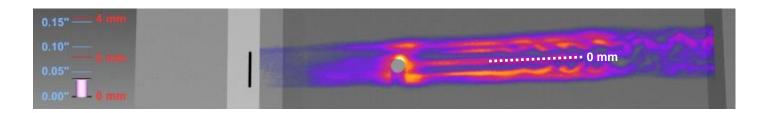
 $M_e \approx 4.2$

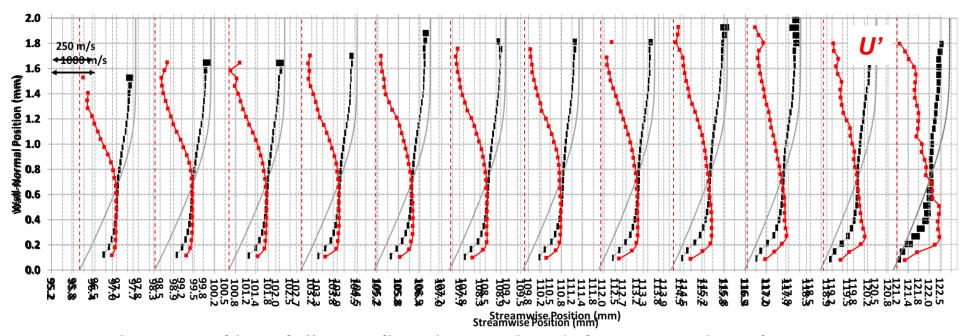
Flow appears laminar when no trip is present



Velocimetry: 1-mm Tall Trip (centerline)





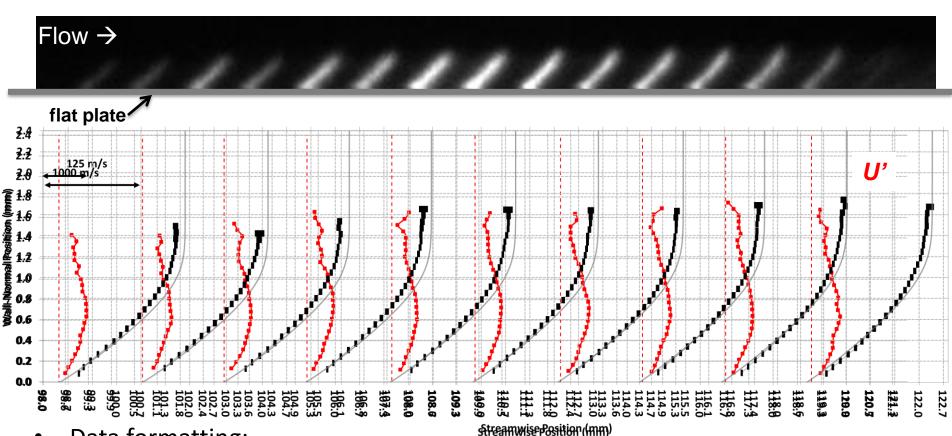


- Velocity profile is full near flat plate with a deficit near edge of BL
 - Note: 2x lower flowrate in this run compared to no-trip case previously shown.
- U' data has increased to peak ~250 m/s (3x larger than laminar case).
- Shape of U' profile changes slightly with distance downstream.



Velocimetry: No Trip



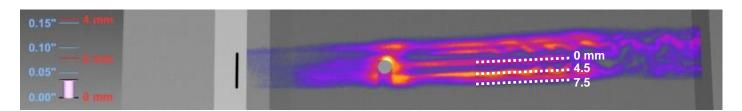


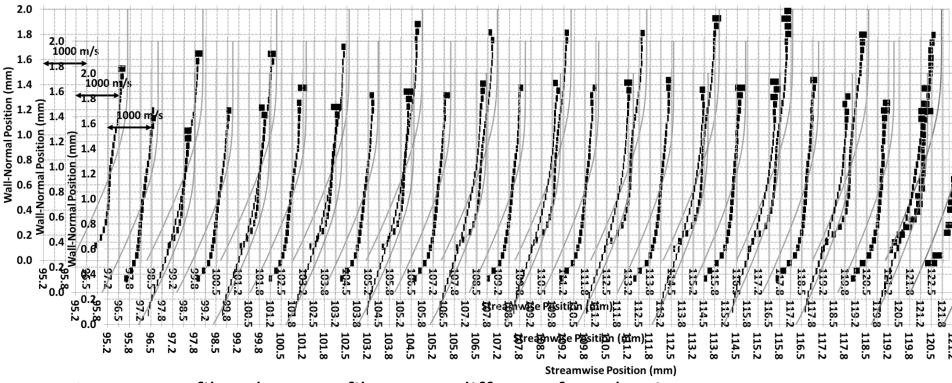
- Data formatting:
 - Center of the data point is mean velocity; Width is uncertainty in mean
 - Standard deviations shown in red (instrument error ~2% of max U was subtracted)
- Blasius-like boundary layer profiles observed (to within 100 μm of wall)
 - Deficit near edge is likely caused by seeding in zero velocity gas into BL (see Johansen et al)
 - U' ~ 80 m/s at maximum. Peak U' is ~ 0.7 mm above surface.



Velocimetry: 1-mm Tall Trip





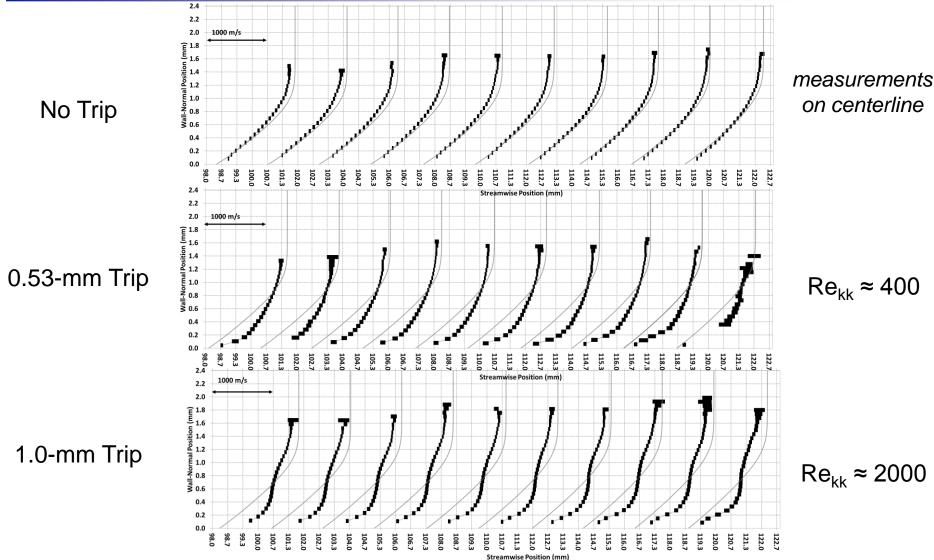


- 4.5 mm profiles show profiles most different from laminar
- Flow becomes more laminar far from centerline (similar to flow vis)
 - U' drops back to ~80 m/s



Comparison of *U* for different trip heights



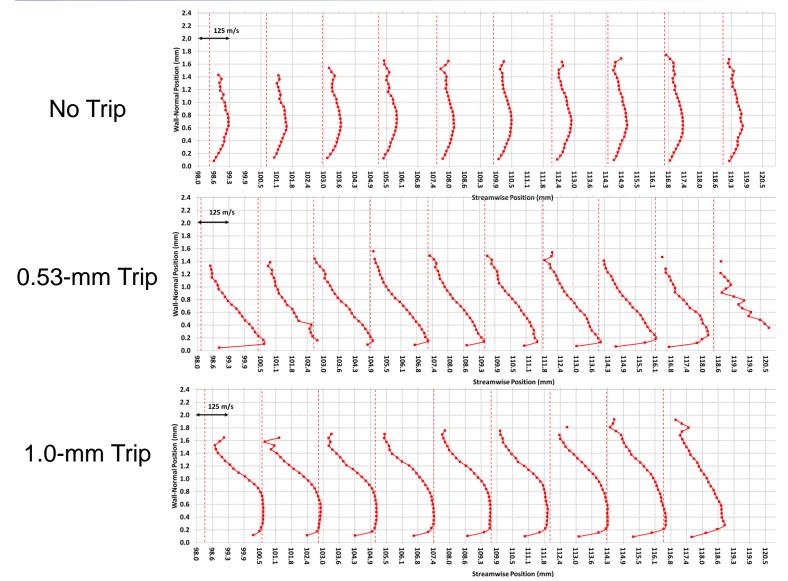


0.53 mm trip profile is between no and 1-mm but no inflection point.



Comparison of *U'* for different trip heights





measurements on centerline

0.53 mm trip U' peak much closer to plate.



Three-laser MTV: uncertainty & design

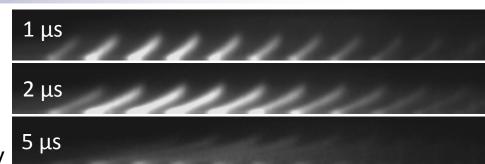


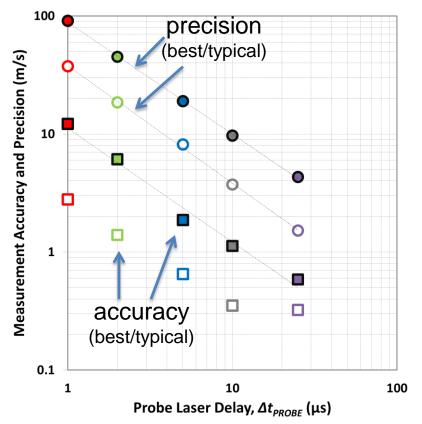
Analysis

- Uncertainty for high s/n data
 - Mean: 1% of edge velocity (~1300 m/s) in 200 images
 - Single-shot: 1-2% of edge velocity
- Measurement within 100 µm from wall

Tradeoffs for experiment design

- Accuracy and precision improve with probe delay
- Spatial resolution worse with longer probe delay
 - Can use longer delay for slow flow
- Current configuration requires relatively large blowing rates for adequate signal-to-noise
 - May be significant wall-normal velocity component





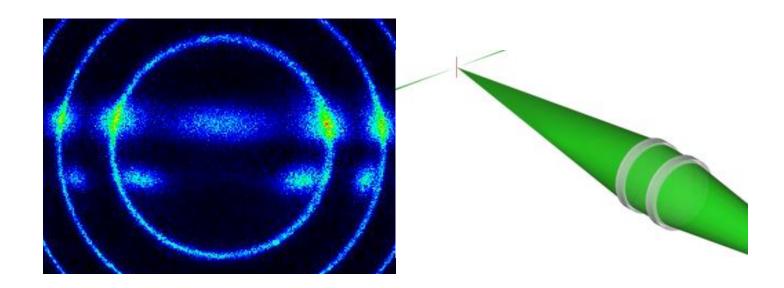
Data obtained at static, low pressure conditions 194



Intro to Rayleigh and Raman Spectroscopy for in Hypersonic Nonequilibrium Flows



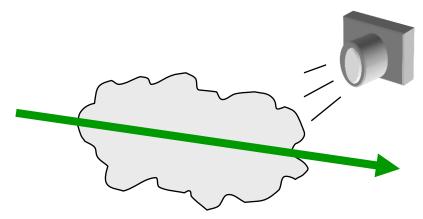
Paul Danehy, NASA Langley Research Center, Virginia, USA





Rayleigh and Raman Scattering





- When light passes through a gas:
 - LIF is a resonant absorption/emission process
 - Mie, Rayleigh and Raman are <u>scattering</u> processes
 - Mie Scattering: $d \ge \lambda$ (d is the particle size)
 - Spontaneous Rayleigh and Raman scattering: $d << \lambda$
- Will explain Rayleigh and Raman two ways
 - Physical interpretation
 - Classical description
 - (Not going to discuss quantum treatment)



Rayleigh Scattering

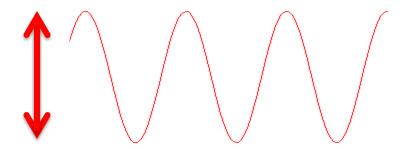


- Rayleigh scattering:
 - Electric field causes electron cloud to oscillate with respect to the nucleus: <u>induced dipole</u>



http://www.timkelf.com/Research/ResearchSERS.html

- An oscillating dipole acts like an antenna: radiates!
 - Radiation is perpendicular to oscillation

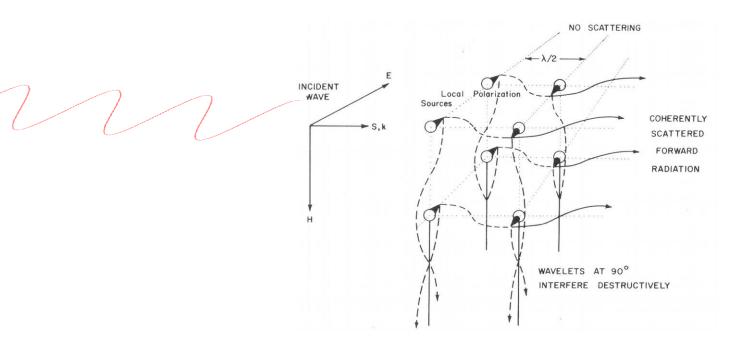




Many Particle Scattering



- A plane-wave perturbs many particles: they radiate
 - Interfere constructively in direction of propagation
 - Interfere destructively in other directions



G.C. Baldwin "An introduction to nonlinear optics." *New York: Plenum Press,* (1969).

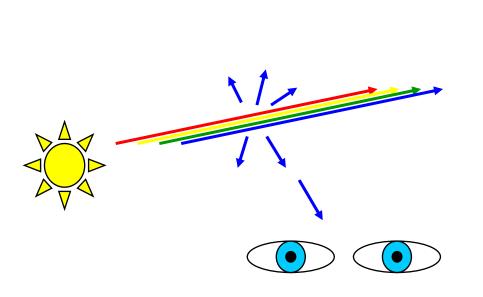
- If exact same number of particles everywhere in gas, destructive interference would give no side scatter
 - But random statistical variation in particle concentration: deconstructive interference is incomplete: Rayleigh Scattering!



Rayleigh Scattering



- Very weak process
 - 1 photon in 0.1 million scatters / meter at STP
- Wavelength dependence: $1/\lambda^4$





Rayleigh scattering in the atmosphere after sunset, picture taken over the ocean, at 500m altitude. http://ms.wikipedia.org/wiki/Selerakan_Rayleigh

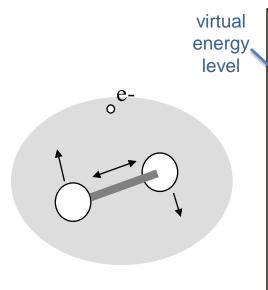
- Causes blue sky and red sunsets
 - Mie scattering from aerosols also contributes



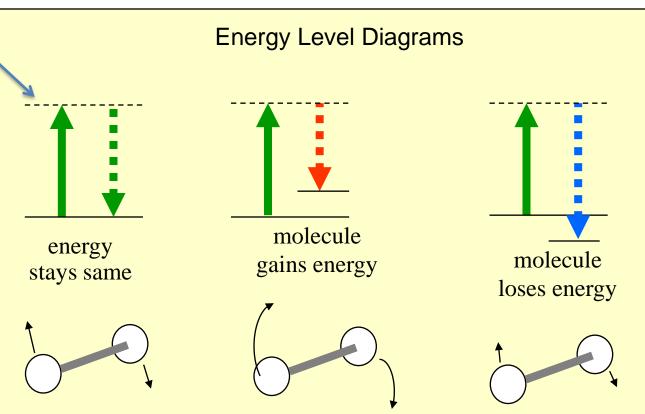
Raman Scattering



- Similar to Rayleigh scattering but molecules gain or lose energy during scattering process
- Raman x1000 lower probability than Rayleigh



N₂ molecule

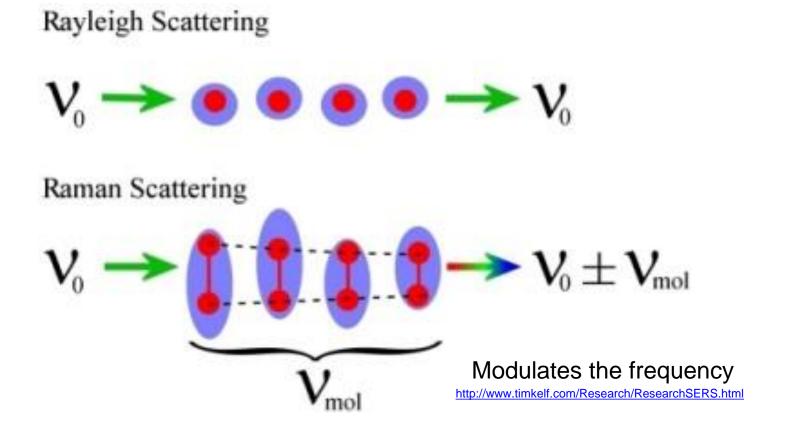




Raman Scattering



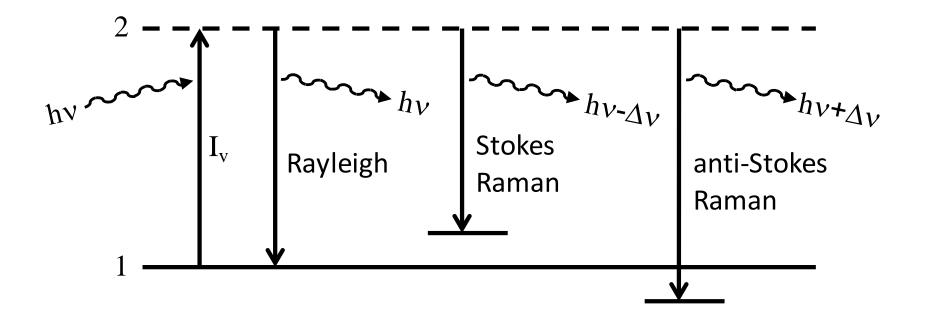
- Raman scattering results in a frequency shift
 - Molecule vibrating at frequency $v_{
 m mol}$





Rayleigh and Raman Scattering



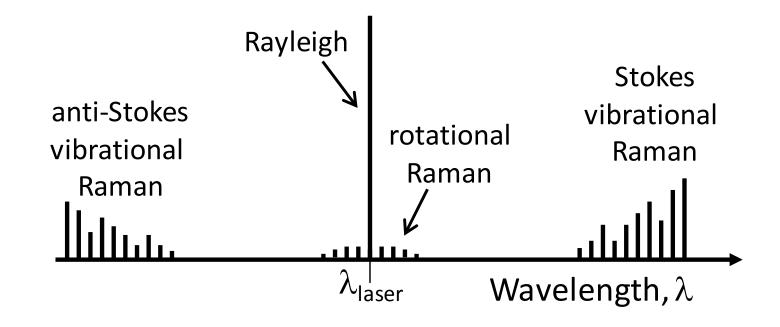


- Energy level diagram:
 - Stokes Raman: energy absorbed by molecule
 - anti-Stokes Raman: energy lost by molecule
 - Initial state must not have been a ground state



Rayleigh and Raman Spectra





- Rayleigh: near laser's wavelength
- Raman: frequency shift depends on molecule, state (sensitive to concentration and temperature)
 - Rotational Raman
 - Vibrational Raman





• Scattered intensity, I, is proportional to the square of the induced dipole moment, \vec{p} :

$$\vec{p} = \varepsilon_0 \alpha \vec{E}$$

where ε_0 is the permittivity of free space, α is the molecular polarizability and \vec{E} is the incident electric field given by:

$$\vec{E} = \overrightarrow{E_0} \cos(\omega_0 t)$$

where $\overrightarrow{E_0}$ is the amplitude of the electric field, ω_0 is the frequency of the laser light and t is time.





- Polarizability, α , depends on internal structure
 - varies with time during vibrational oscillations at the natural frequency of the molecule, $\omega_{\rm v}$



- $-\alpha$ varies with spatial coordinate, Q
 - More loosely held electrons → more polarizable
 - Taylor Series Expansion:

$$\alpha = \alpha_0 + \left(\frac{\partial \alpha}{\partial Q}\right)_0 dQ$$

where dQ is small displacement about equilibrium positions which occurs during normal vibration

$$dQ = Q_0 \cos(\omega_v t)$$





• Substituting previous equations into $\vec{p} = \varepsilon_0 \alpha \vec{E}$:

$$\vec{p} = \left[\alpha_0 + \left(\frac{\partial \alpha}{\partial Q}\right)_0 Q_0 \cos(\omega_v t)\right] \varepsilon_0 \vec{E_0} \cos(\omega_0 t)$$

Expanding and using trig identity:

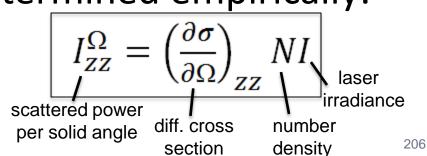
$$\overrightarrow{p} = \alpha_0 \varepsilon_0 \overrightarrow{E_0} \cos(\omega_0 t) + \frac{1}{2} \left(\frac{\partial \alpha}{\partial Q}\right)_0 \varepsilon_0 Q_0 \overrightarrow{E_0} \left[\cos(\omega_0 - \omega_v)t + \cos(\omega_0 + \omega_v)t\right]$$
Rayleigh Scattering

Stokes Raman

anti-Stokes Raman

- Resulting induced dipole moment (and scattering) is at three frequencies
- Amplitude is usually determined empirically:

$$\left(\frac{\partial \sigma}{\partial \Omega}\right)_{ZZ} \equiv \frac{I_{ZZ}^2}{NI}$$
 Differential Cross Section (varies by molecule and with I but not with P, T) (zz indicates polarization of laser and detection)





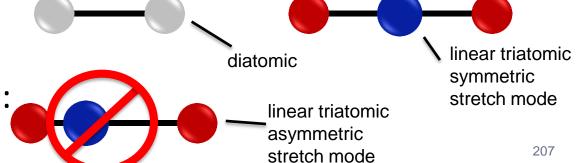


- Selection Rules: Raman Activity
 - Not every molecule or vibrational mode produces Raman

$$\vec{p} = \alpha_0 \varepsilon_0 \vec{E_0} \cos(\omega_0 t) + \frac{1}{2} \left(\frac{\partial \alpha}{\partial Q}\right)_0 \varepsilon_0 Q_0 \vec{E_0} [\cos(\omega_0 - \omega_v)t + \cos(\omega_0 + \omega_v)t]$$

- Amplitude of Raman is proportional to the magnitude of: $\left(\frac{\partial \alpha}{\partial \rho}\right)$
- Polarizability, α , \mathring{m} \mathring{u} st *change* during vibrations to be Raman active
- Raman active:

- Raman inactive:

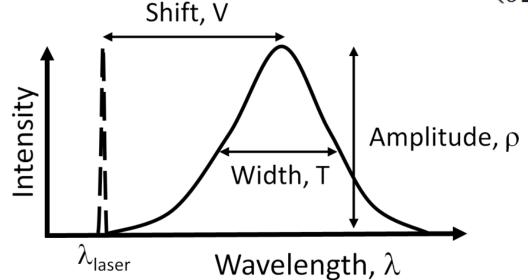






- Rayleigh Scattering is at or near the laser's wavelength.
 - Doppler broadened (${}^{\sim}T^{1/2}$)
 - Can be Doppler shifted ($\sim V$)
 - Signal proportional to N ($\sim \rho$)

$$I_{ZZ}^{\Omega} = \left(\frac{\partial \sigma}{\partial \Omega}\right)_{ZZ} NI$$



- Can potentially measure these simultaneously
 - Requires high spectral resolution



Rayleigh and Raman Examples



Rayleigh

- Velocimetry, multi point
- -V, T, ρ , single point
- -V, T, ρ , imaging
- $-\rho$ measurement (and infer T)

Raman

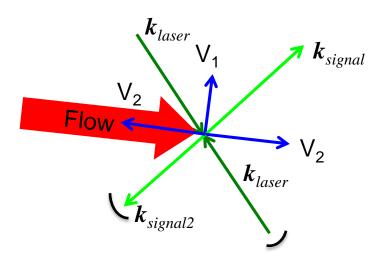
- Concentration
- Temperature



Rayleigh Velocimetry



- Rayleigh scattering velocimetry can measure selected velocity components
 - Measured component is bisector between incident laser and collection optics



Wave vector:

 $\mathbf{k} = 2\pi/\lambda$

D. Bivolaru, P. M. Danehy, R. L. Gaffney, Jr. and A. D. Cutler, "Direct-View Multi-Point Two-Component Interferometric Rayleigh Scattering Velocimeter," 46th AIAA Aerospace Sciences Meeting and Exhibit, Reno, Nevada, AIAA Paper 2008-236, January 7-10, 2008

 Can measure multiple velocity components by adding additional detection angles or laser beams

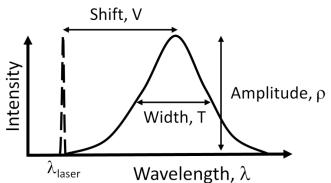


Rayleigh Velocimetry



- Rayleigh scattering velocimetry has been performed different ways, always requiring a high resolution device to resolve the Doppler shift
 - $-I_2$ filter in front of CCD
 - Imaging capability
 - limited dynamic range
 - Fabry Perot etalon
 - PMT based (faster)
 - CCD based (multi-point)
 - Combined I_2 filter and Fabry Perot etalon



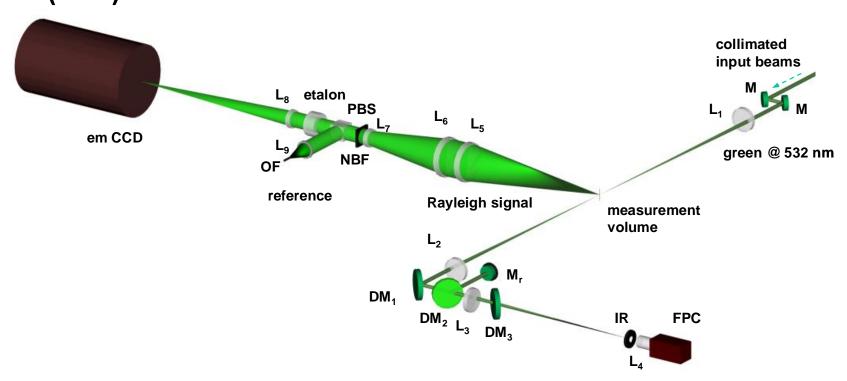




Rayleigh Velocimetry using Fabry-Perot Etalon



 Velocimetry using a Fabry Perot Interferometer (FPI) with CCD camera

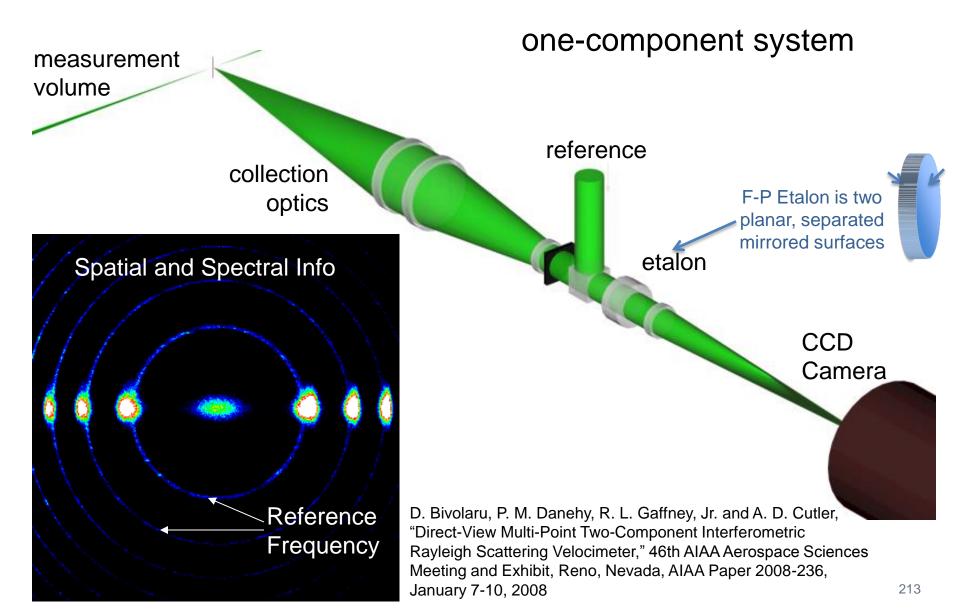


 D. Bivolaru, P. M. Danehy, R. L. Gaffney, Jr. and A. D. Cutler, "Direct-View Multi-Point Two-Component Interferometric Rayleigh Scattering Velocimeter," 46th AIAA Aerospace Sciences Meeting and Exhibit, Reno, Nevada, AIAA Paper 2008-236, January 7-10, 2008



Rayleigh Velocimetry using Fabry-Perot Etalon

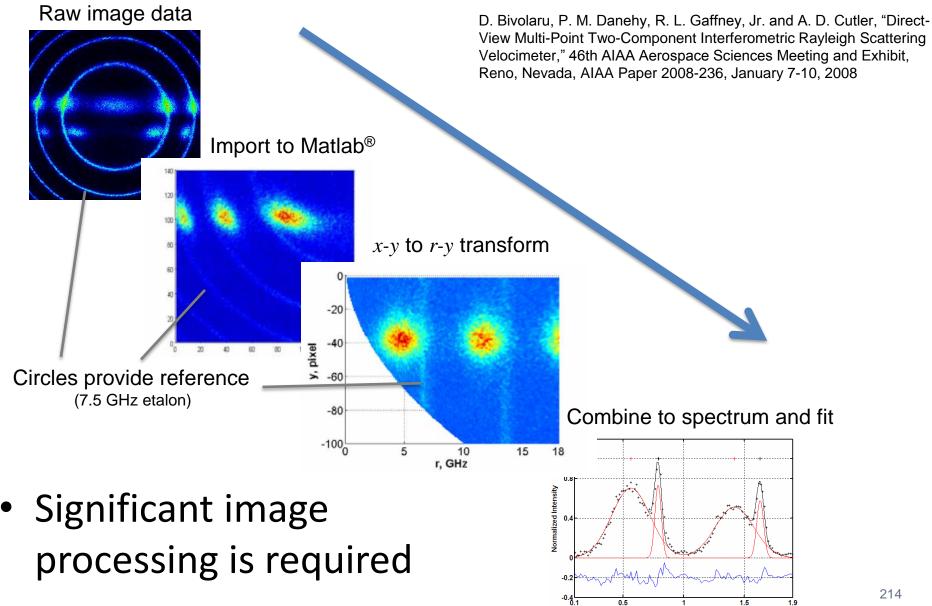






Rayleigh Scattering Image Processing

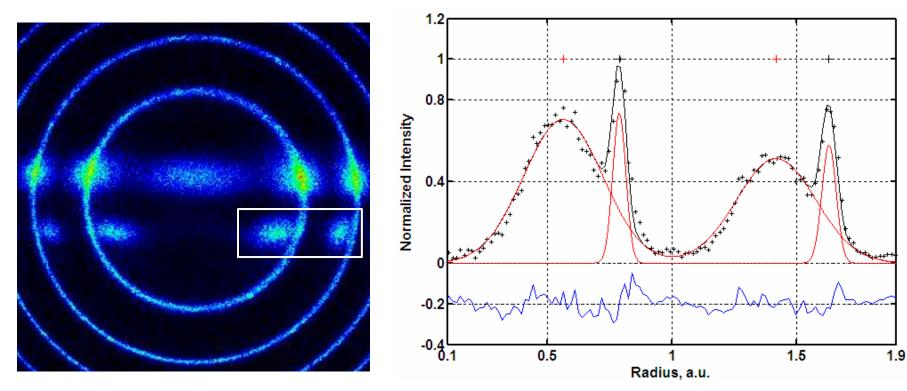






Rayleigh Scattering Velocity Results





 Rayleigh scattering in a large scale (6 cm diameter) Mach 1.6 H₂-air combustion heated jet operating at Mach 5.5 enthalpy at NASA Langley

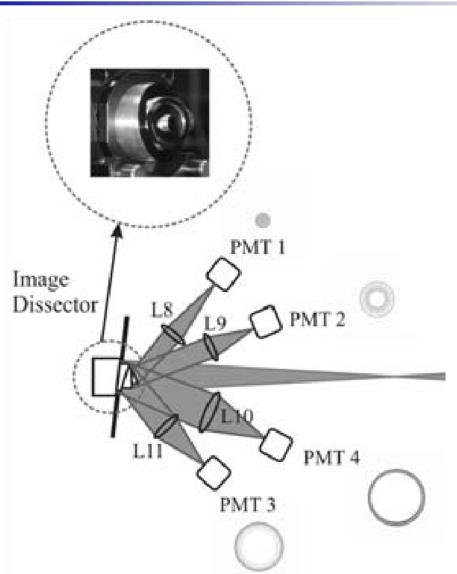
Velocity precision of ~40 m/s out of 1200 m/s, (3%) The dynamic range of the instrument was ~3000 m/s

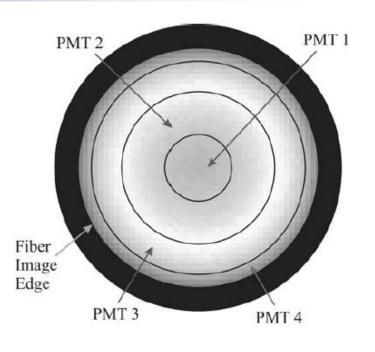
- precision 1% of dynamic range



Rayleigh Scattering: T, V, ρ







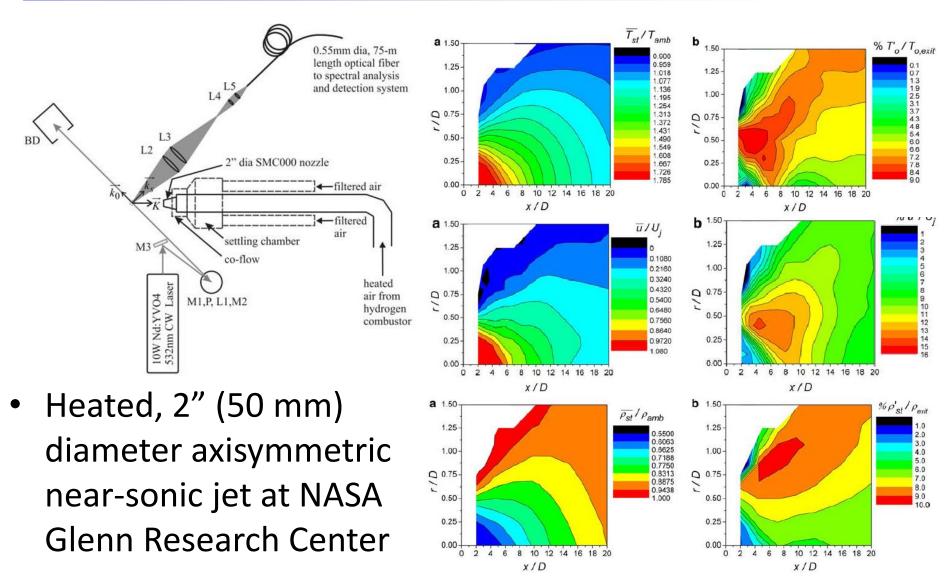
- Continuous laser excitation
 - 10 W at 532 nm
- Fiber optic collection
- Data rate: 10 kHz
- Single point measurement

A. F. Mielke and K. A. Elam. "Dynamic measurement of temperature, velocity, and density in hot jets using Rayleigh scattering." *Experiments in fluids* 47, no. 4-5 (2009): 673-688.



Rayleigh Scattering: T, V, ρ





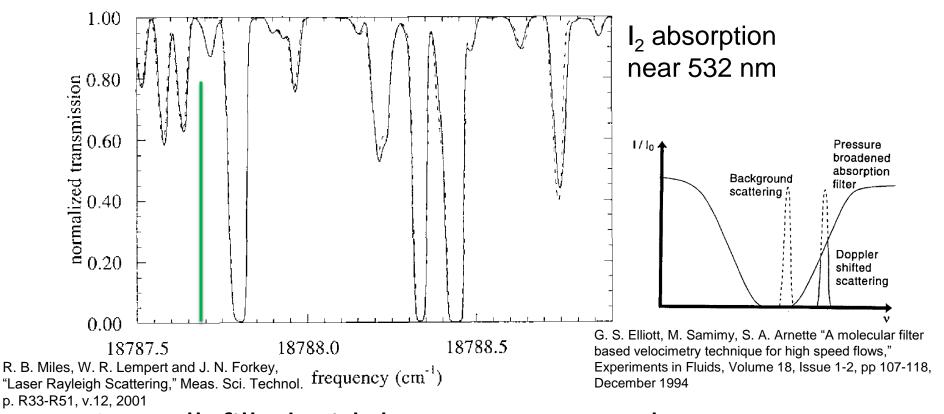
A. F. Mielke and K. A. Elam. "Dynamic measurement of temperature, velocity, and density in hot jets using Rayleigh scattering." *Experiments in fluids* 47, no. 4-5 (2009): 673-688.



Rayleigh Velocimetry (I_2 filter)



Instead of an etalon, use I₂ filter → 2D imaging



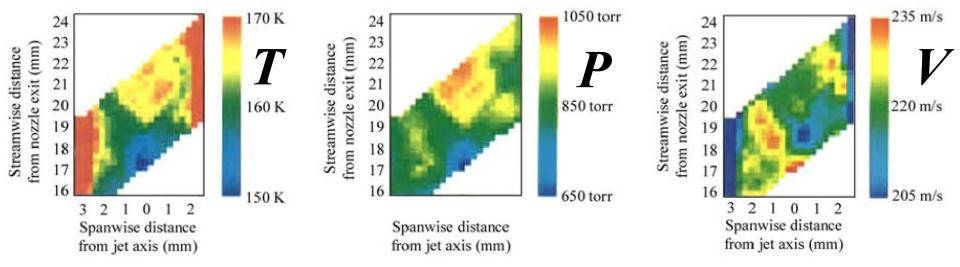
- Gas cell, filled with low-pressure N₂ plus some I₂ crystals; control temperature to determine absorption
- Scan Nd:YAG laser frequency (or fixed)



Rayleigh Imaging of T, V, ρ (or P)



Direct YAG laser sheet into a Mach 2 jet



R. B. Miles, W. R. Lempert and J. N. Forkey, "Laser Rayleigh Scattering," Meas. Sci. Technol. p. R33-R51, v.12, 2001

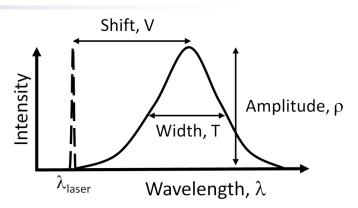
- Scanned laser frequency, determine T, V, ρ (report P) based on measured spectrum at each pixel
- Same method can be used for velocimetry from particles (usually fixed frequency, multiple detection angles)
 - Planar Doppler Velocimetry (PDV) or Doppler Global Velocimetry (DGV)

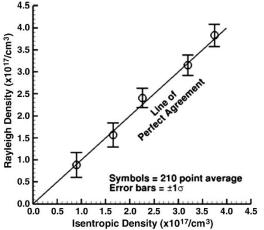


Rayleigh Scattering: ρ



- Rayleigh scattering has a spectrum:
 - Sensitive to T, V, ρ
 - Prior examples used Fabry Perot
 Etalon or I₂ cell to observe spectrum
 - These devices reject signal, making them less sensitive detectors of ρ .
- Collect all of the scattering
 - Less equipment/less setup/simpler
 - Bigger signal
 - Can do single point or imaging
 - Only sensitive to ρ .
 - o (If you know P and composition you can convert ρ to T.)





Using a UV laser (e.g. ArF at 193 nm) allows measurements to be made at low pressures (e.g. 1/300 atmospheric density)

Balla, R. Jeffrey, and Joel L. Everhart. "Rayleigh scattering density measurements, cluster theory, and nucleation calculations at Mach 10." AIAA Journal 50, no. 3 (2012): 698-707.



Raman Spectroscopy



- Raman spectrum obtained in a CH₄-air flame:
 - Average of 500 pulses using stretched 0.5 J/pulse, 532 nm
 - Stretch 10 ns pulse to 500 ns to avoid laser-induced breakdown

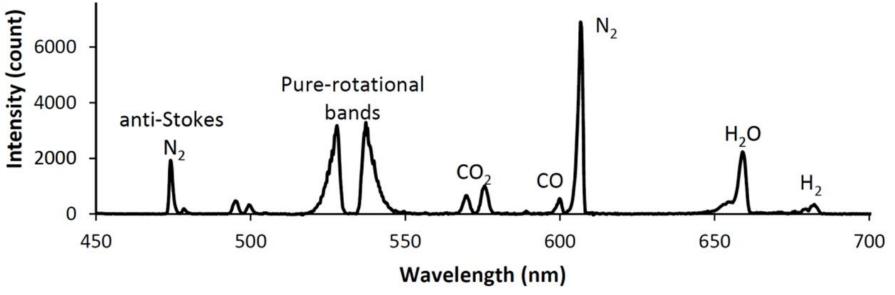


Figure courtesy of Jun Kojima, NASA Glenn Research Center (Jun.J.Kojima@nasa.gov)

 Can measure species (N₂, CO, CO₂, H₂, H₂O) from such spectra &temperature from Stokes/anti-Stokes

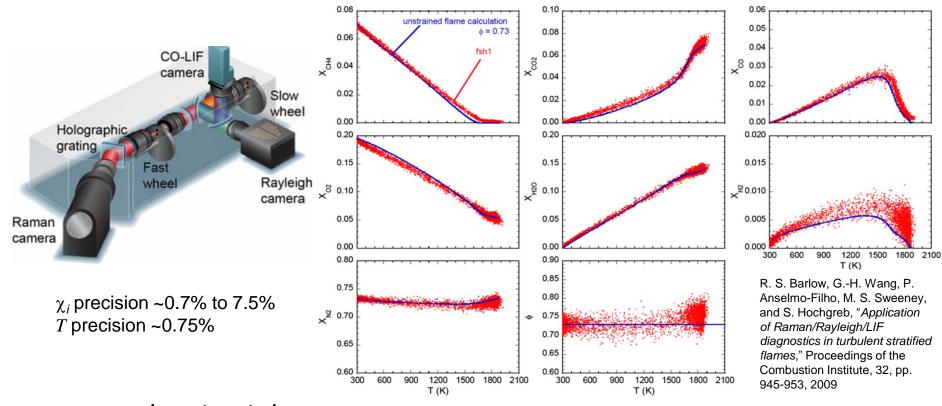


Raman Concentration Measurement



(and Rayleigh Temperature and LIF concentration)

- Example of Raman concentration measurements in a subsonic turbulent CH₄/air flame at Sandia National Laboratories, California
 - 4 Nd:YAG lasers at 532 nm to produce 1.8 Joules/pulse, focused to a point



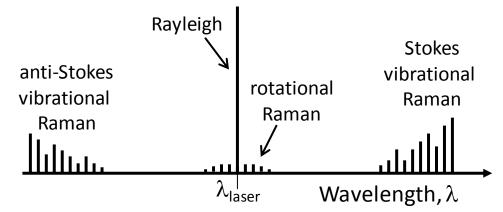
- Raman/Rayleigh/LIF line imaging (~10 pixels / mm along the 6-mm-long probe volume)
 - N₂, O₂, CH₄, CO₂, H₂O and H₂ from Raman, CO from 2 photon LIF
 - Temperature from Rayleigh density measurement (idea gas law)



Raman Temperature Measurement



- Several ways to measure temperature with Raman
 - none as precise as CARS (3%)



- Rotational Temperature from pure-rotational Raman
- Vibrational temperature measurements
 - Only good above 700 K
 - Stokes / anti-Stokes vibrational Raman
 - Low resolution, so can measure concentrations at same time
 - ~20% precision in measurements along a line (Wehrmeyer, 1996)
 - Spectrally resolved vibrational band (Sharma et al, 1993)

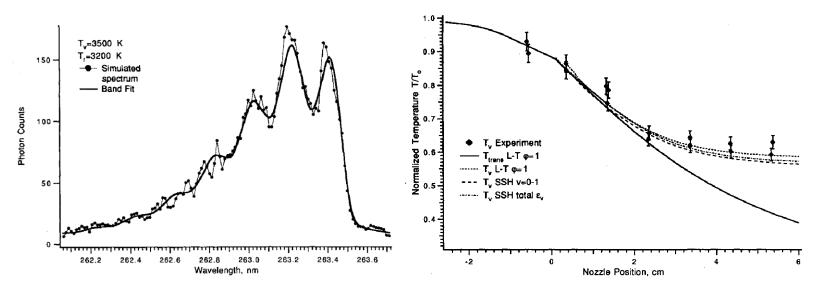
(see Kojima, 2008)



Raman Temperature Measurement



- Raman temperature measurement from spectrally resolved vibrational N₂ band.
 - Excited with KrF Excimer laser 0.25 J at 248 nm (25 ns pulse)



S. P. Sharma, S. M. Ruffin, W. D. Gillespie and S. A. Meyer, "Vibrational Relaxation Measurements in an Expanding Flow Using Spontaneous Raman Scattering," J. of Thermophys. and Heat Trans. Vol. 7, No. 4, Oct.-Dec. 1993

- Single shot precision ~5% (not explicitly stated)
 - More precise than Stokes/anti-Stokes but cannot measure species concentrations with same instrument.



Rayleigh Scattering: ρ

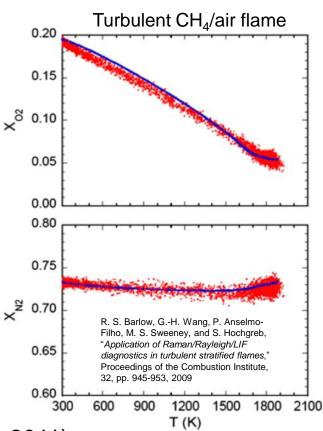


- When precise measurements are required, high S/N is needed
 - Use high powered lasers, focused to a point
 - If too high: laser-induced breakdown
- Sandia, Livermore, Calif.:
 - Raman/Rayleigh/LIF line imaging at P = 1 atm
 - 4 double-pulse Nd:YAG lasers: 1.8 J/pulse
 - Camera images Rayleigh along line
 - ~10 pix / mm along 6-mm-long probe volume
 - N₂, O₂, CH₄, CO₂, H₂O and H₂ from Raman
 - CO from 2 photon LIF

 - CO from 2 proton 2...

 Temperature from Rayleigh density, ρ ,

 massition to determine $\left(\frac{\partial \alpha}{\partial \alpha}\right)$
 - If known P, idea gas law give T
 - T precision reported: ~0.75%
 - (ρ precision is probably same)
 - Cutting edge MHz laser: 40x lower energy (Jiang, 2011)





Advantages and Disadvantages: Rayleigh & Raman



Advantages:

- No seeding required
- Only one color of laser used (simplicity)
- Multiple properties measured at once
 - T, V, ρ for Rayleigh
 - T, many species for Raman
 - Can do Raman and Rayleigh together and with LIF

Disadvantages:

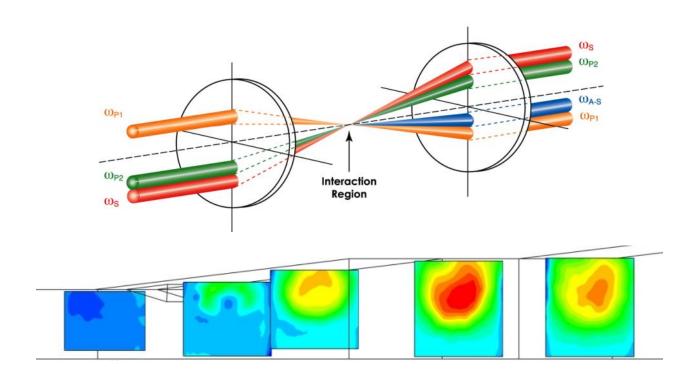
- Weak signal:
 - Requires very high power laser
 - stretched to avoid laser induced breakdown
 - Requires large windows, big, close collection optics
 - Usually singe point or line measurements
- Temperature less accurate & precise than CARS



Intro to Coherent anti-Stokes Raman Spectroscopy (CARS) for Hypersonic Nonequilibrium Flows



Andrew Cutler, The George Washington University, USA Paul Danehy, NASA Langley Research Center, Virginia, USA





Outline



- Brief introduction to nonlinear optics
- Introduction to CARS and basic theory
- NASA / GWU CARS System
 - Temperature and composition measured in UVa dual mode scramjet
 - Thermometry shows vibrational nonequilibrium
- CARS in a non-thermal plasma
- Concluding remarks



Nonlinear Optics



- First, a few words about nonlinear optics
 - Conservation of energy
 - Conservation of momentum
 - Wave equation from Maxwell's equations
- Second Harmonic Generation as an Example
 - 2nd order nonlinearity (solid)
 - CARS is a 3rd order nonlinearity (gas)



Intro: Nonlinear Optics WILLIAM STATES OF THE STATES OF TH



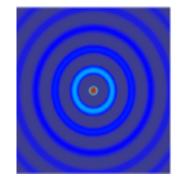


Second Harmonic Generation (SHG)



– Solved using the Wave Eqn:

$$\nabla^2 \mathbf{E} - \frac{1}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2} = \mu_0 \frac{\partial^2 \mathbf{P}_{\text{NL}}}{\partial t^2}$$



– Assume SVEA and 1st Born Approx:

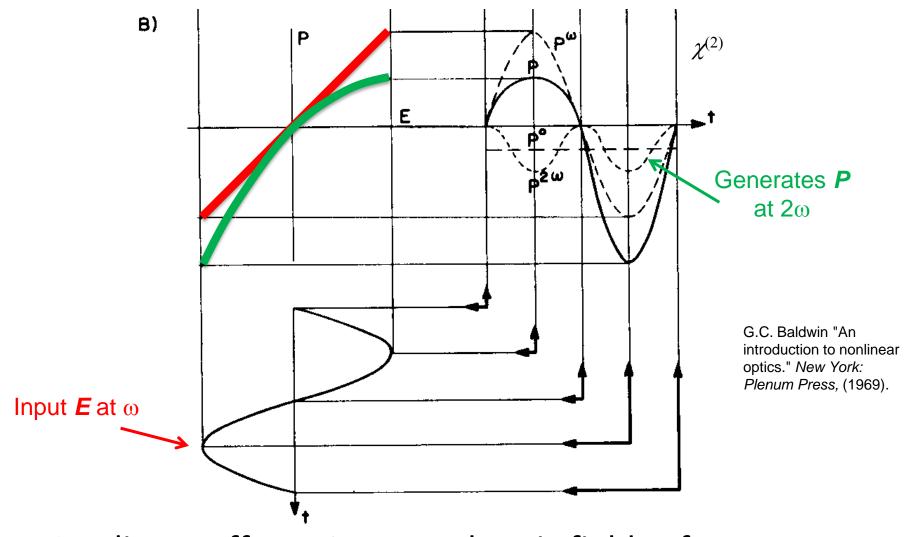
$$I_{\omega_2} \propto rac{d^2 P_{\omega_1}^2 L^2}{\mathsf{A}^2}$$

-d is a coefficient, P is power, L is length, A is area



Non-linear Susceptibility





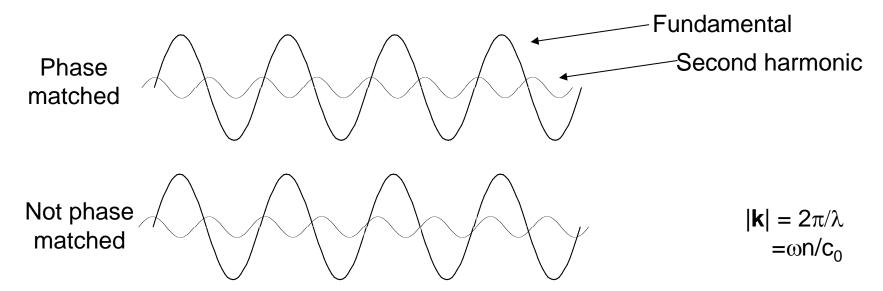
 Non-linear effects: Intense electric fields of one frequency can generate a P at another



Phase Matching



- What is Phase Matching?
 - Ensuring that the light wavefronts 'match up'.

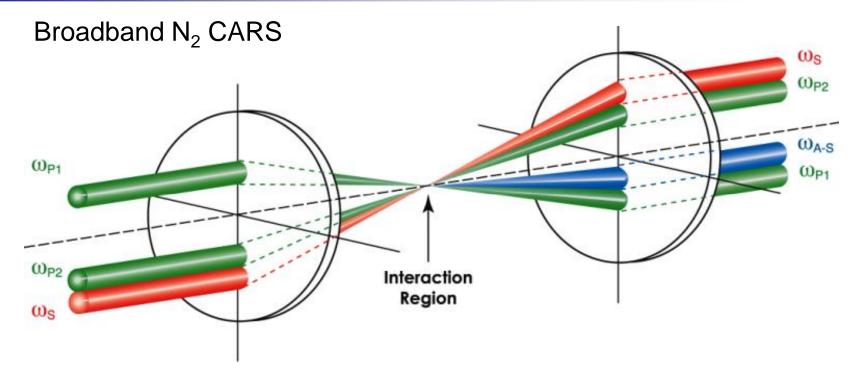


- Dispersion causes deconstructive interference
- New photons generated are out of phase with previous ones: resulting in loss
- For SHG there are tricks to make it phase matched
- Conservation of momentum: phase matching
- Conservation of energy: $\omega_2 = 2\omega_1$



What is CARS?





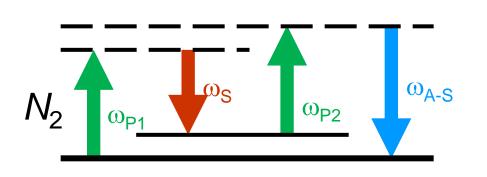
Spectrally-broad red beam +
Spectrally-narrow green beams =
Single-shot blue CARS spectrum

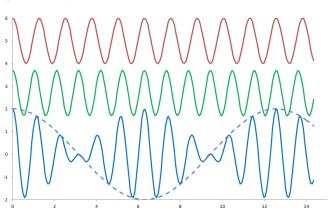


CARS Energy Level Diagram (conservation of energy)



- Lasers: 2 Green (532 nm) and 1 Red (607 nm)
 - Frequency difference between Green and Red
 Probes N₂ vibrational Raman Shift





Result: Blue signal beam at 473 nm.

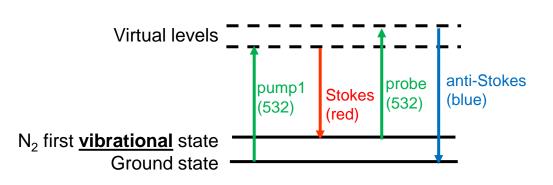


- Spatially, spectrally, temporally filter this signal
 - Good technique for luminous flows
- Send to spectrometer equipped with CCD camera
- Measured CARS spectra is best fit to a library of theoretical spectra on a single-shot basis (10 ns)

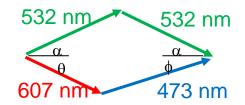


CARS Phase Matching (conservation of momentum)





Planar Boxcars Geometry



$$k_{p1} + k_{p2} = k_S + k_{A-S}$$

It is straight forward to compute the CARS phase matching angles:

N2 cars		adjust inpu	
	lambda	wavenum	angle (degrees
stokes	607	16474.46	3.963
pump 2	532	18796.99	3.500
pump 1	532	18796.99	3.500
anti stokes	473.4956	21119.52	3.091
			0.023576939
N2 Raman =	2322.528	cm-1	0.023576939
(nominal N2 = 2330 cm-1)			3.00927E-20

Different molecules require different angles (can get multiple signals at different spatial locations: Dual-Stokes)



CARS Phase Matching Geometries

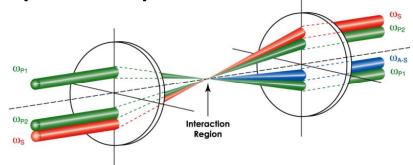


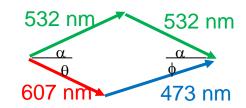


Poor spatial resolution

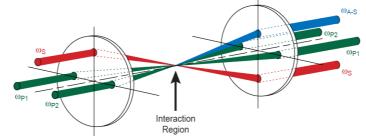
 $k_{p1} + k_{p2} = k_S + k_{A-S}$ 532 nm
532 nm
607 nm
473 nm

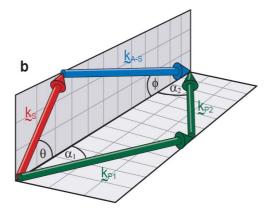
(Planar) BoxCARS:





Folded BoxCARS:





 Best spatial resolution (1.5 mm x 0.1 mm x 0.1 mm) but lower signals and affected by beam steering from turbulence



B)





Non-linear effects:

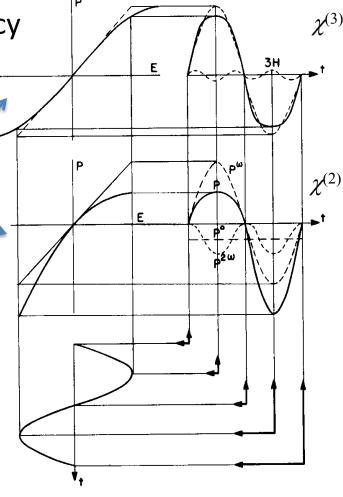
 Intense electric fields of one frequency can generate a P at another

-
$$P = \varepsilon_0 (\chi E + \chi^{(2)} E^2 + \chi^{(3)} E^3 + ...)$$

 $-\chi^{(2)}$ = 2nd order susceptibility

 Only media lacking a centre of symmetry (ie, no gases, liquids)

- \chi^{(3)} = 3rd order susceptibility
 All dielectric media
- Generally $(\chi E >> \chi^{(2)} E^2 >> \chi^{(3)} E^3)$



G.C. Baldwin "An introduction to nonlinear optics." New York: Plenum Press, (1969).





Polarization generated at CARS signal frequency:

$$P^{(3)}(\omega_{signal}) = \epsilon_0 \chi_{CARS} E(\omega_{pump}) E(\omega_{Stokes}) E(\omega_{probe})$$

Substitute into the wave equation. Result:

$$I_{signal} \propto I_{pump} I_{Stokes} I_{probe} |\chi_{CARS}|^2 L^2$$

• To obtain large signals, want long L, high laser power (tight focus) and strong resonance

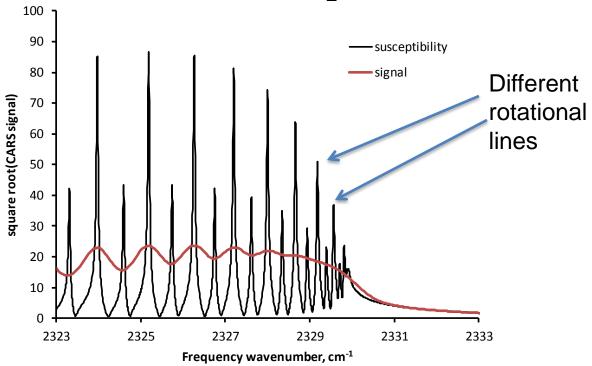
$$\chi_{CARS} = \sum_{j} \frac{K_{j} \Gamma_{j}}{2\Delta \omega_{j} - i\Gamma_{j}} + \chi_{nr} \text{ where } K_{j} \propto N \Delta_{j} \left(\frac{\partial \sigma}{\partial \Omega}\right)_{j}$$

- $\Gamma_{\rm j}$ is damping coefficient, N is number density, $\Delta_{\rm j}$ is the population difference
 - $-N \rightarrow$ concentration; $\Delta_i \rightarrow$ Temperature sensitivity





Instructive to graph example N₂ spectra:

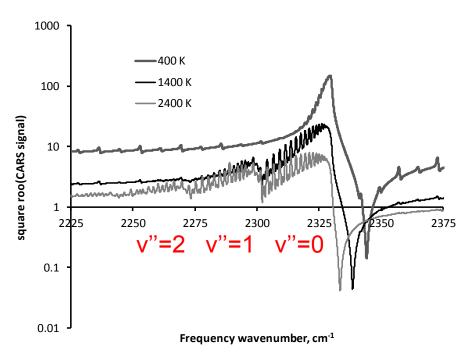


- N₂ is commonly probed with CARS because it is often present and spectroscopy is well known
- CARS spectrum at 1 atm., 1400 K, v" = 0 band.
 - N_2 Q-branch ($\Delta v = +1$, $\Delta J = 0$)
 - CARS signal spectrum is convolved with lasers used

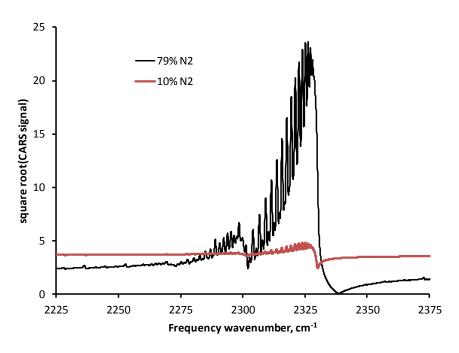




Effects of temperature (left) and composition (right):



Vibrational "hot band" becomes populated above 700 K

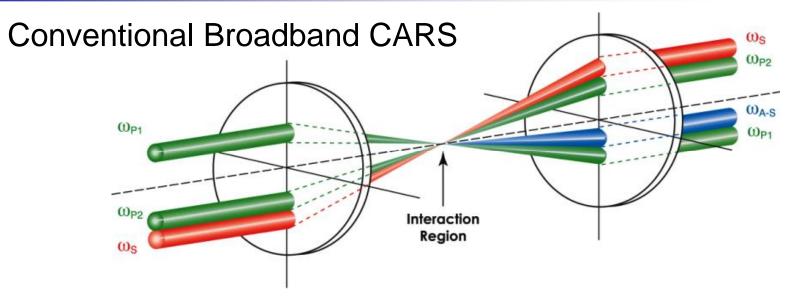


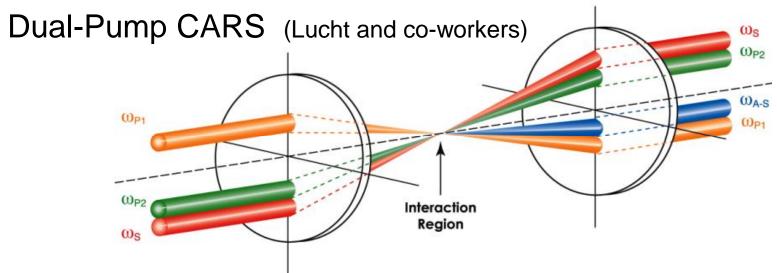
CARS spectra are sensitive to the gas composition through resonant and nonresonant parts



Multi-Species Measurement: Dual-Pump CARS





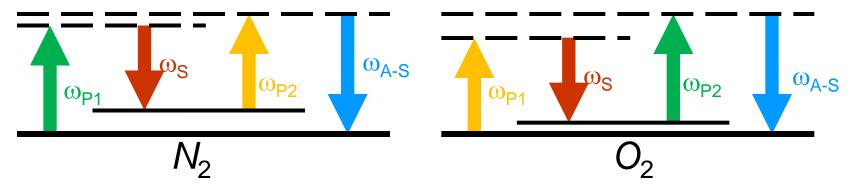




Dual-Pump CARS: N₂, O₂, H₂



- Green and Red Probe N₂ Raman Shift
- Red and Yellow Probe O₂ Raman Shift



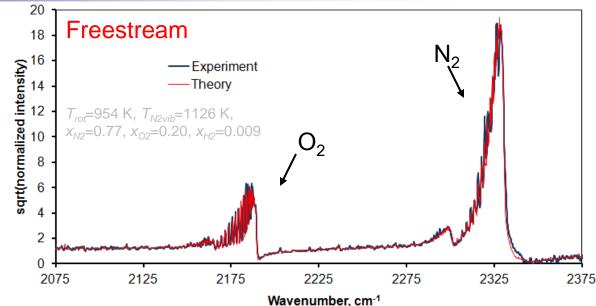
- Result: Two different spectral regions of Raman Shift appear coincident in the 490 nm CARS beam.
 - 'self calibrating' compared to other methods
 - H₂ pure rotational Raman lines present
 O'Byrne et al AIAA Journal v. 45, 2007

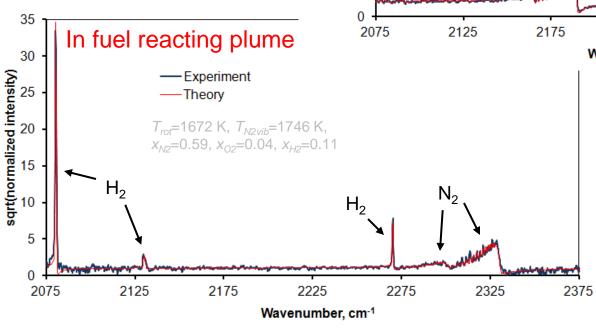


Typical Dual-Pump CARS Spectra and Fits



- Single-shot spectra obtained in combustor shown with best fit
- Absolute measurement of rotational, vibrational temperature, N₂, O₂, and H₂ mole fractions





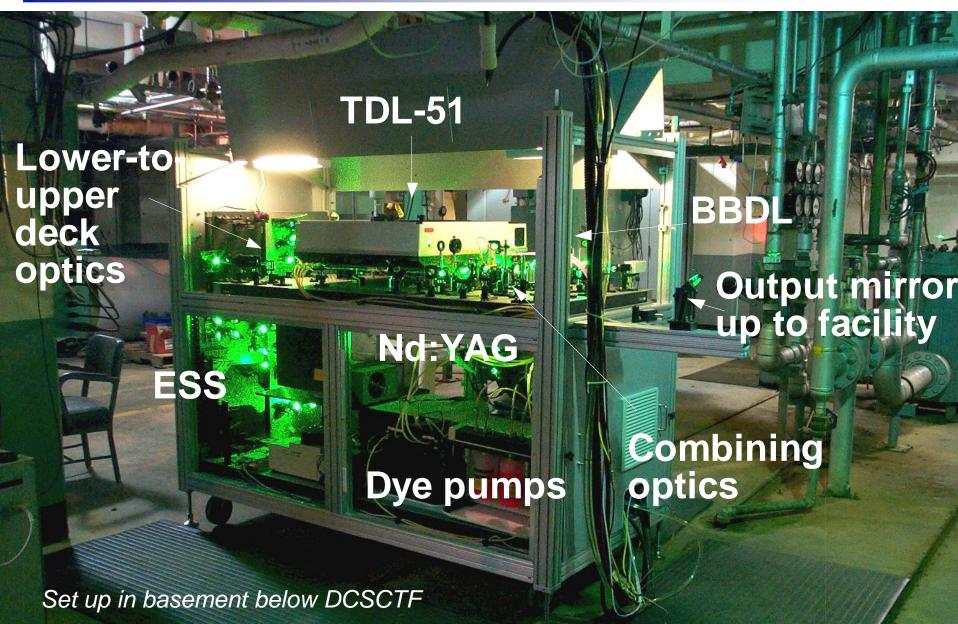
- Measurement obtained:
 - In UVa Scramjet (Conf C)
 - $-\varphi = 0.18$, Plane 2, z/H = 0
 - in10 ns (instantaneous)
 - at 20 Hz repetition rate
 - Measurement volume =1.7 x 0.2 x 0.2 mm³



NASA/GWU Mobile CARS System



→ Simplifies/speeds set up in facility





Features of NASA/GWU Mobile CARS System

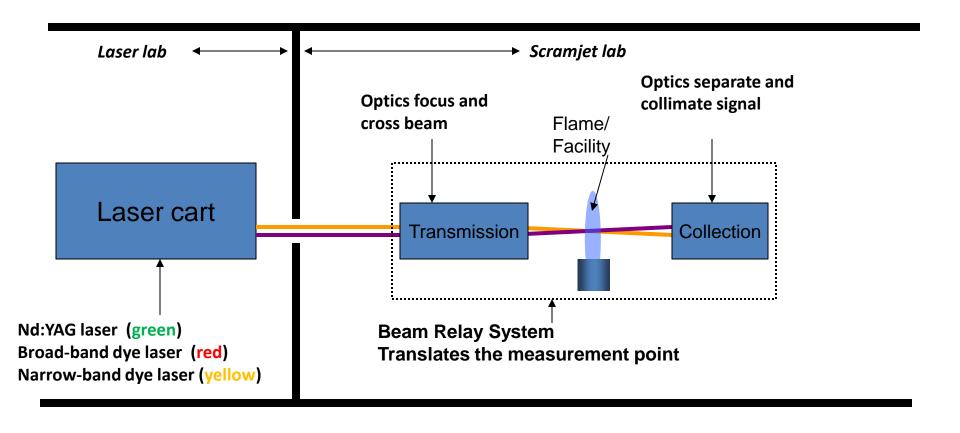


- YAG laser plus 2 dye lasers on single cart
- Transmission and receiving optical stages
- Can put system on a truck and moved to facilities
- Measures T_{rot} , T_{vib} , N_2 , O_2 , H_2 mole fractions at 20 Hz.
 - Quantified accuracy, precision
- Fully automated data acquisition
 - Remote operation of system
 - X-Y (-Z) probe volume traverse capability
 - Input test matrix; then system acquires and automatically saves data for hours until complete
 - Laser power automatically adjusted to prevent saturation effects (detector saturation, Stark broadening, Raman pumping)
 - Beam alignment monitors; remote control alignment
- Beam shaping capability to maintain alignment measurement in turbulent/vibration flows
 - 10x improvement compared to USED CARS



Setup at UVa: Optical System 1

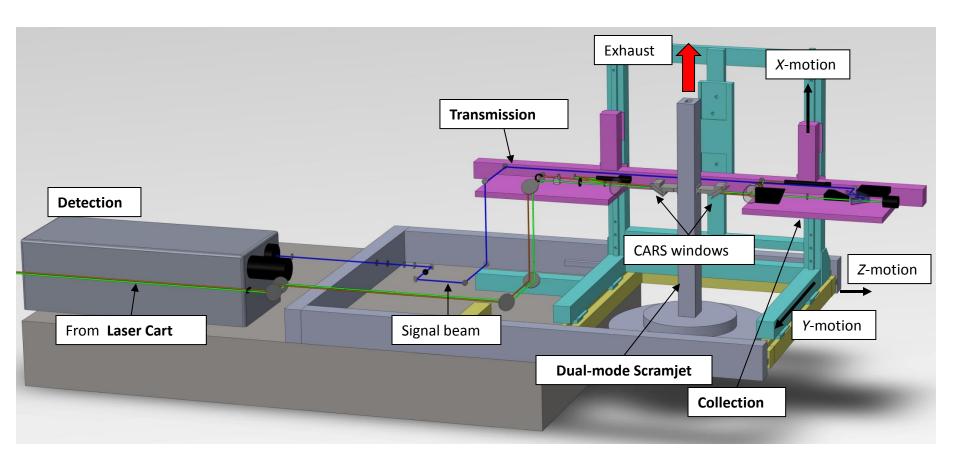






Setup at UVa: Optical System 2

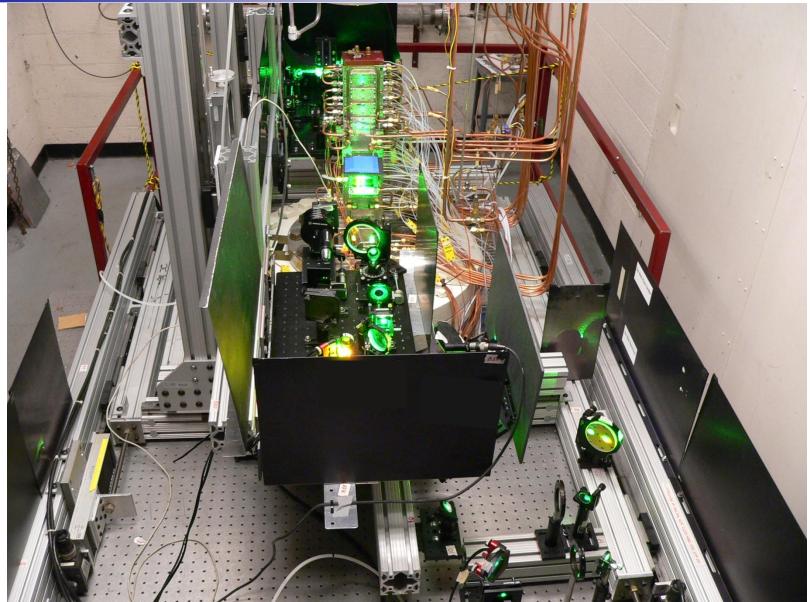






Transmission stage and test section at UVa

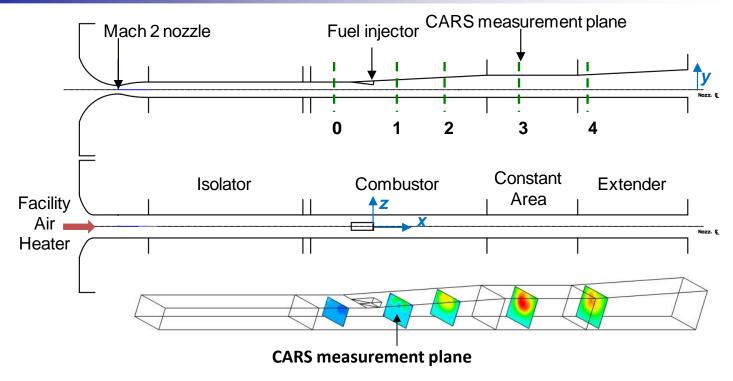






Facility / Dual Mode Scramjet at UVa



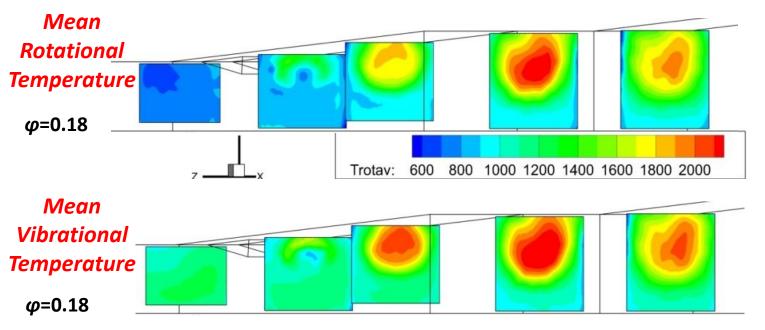


- Electrically heated clean air, nominal $T_t = 1200 \text{ K}$, M = 2 nozzle
- Long test times allow large data sets at steady inflow conditions
- Highly turbulent flowfield
- Good optical access



Nonequilibrium: CARS T_{rot} and T_{vib}

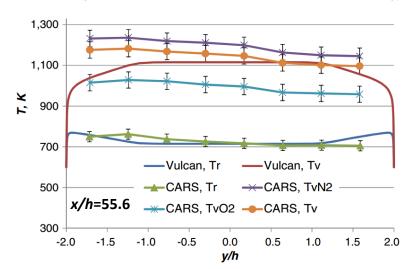




H₂ fuel, Config. C

A. D. Cutler, G.
Magnotti, L. Cantu, E.
Gallo, P. M. Danehy, R.
Rockwell, C. Goyne,
and J. McDaniel, "DualPump CARS
Measurements in the
University of Virginia`s
Dual-Mode Scramjet:
Configuration C," Paper
AIAA-2013-0335, 2013.

 T_{N2vib} observed to be 600 K higher than T_{rot} in facility freestream; not anticipated before experiment



Vibrational Temperature

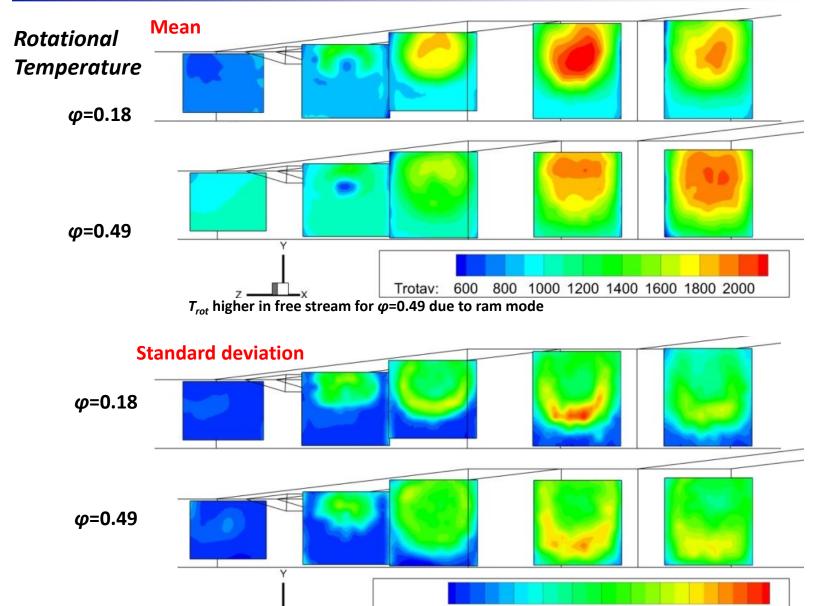
CARS vibrational O₂ and N₂ temperatures "lumped" together and used to validate the vibrational nonequilibrium model implemented in VULCAN code by R. Baurle (NASA).

A.D. Cutler, L. M. L. Cantu, E. C. A. Gallo, R. Baurle, P. M. Danehy, R. Rockwell, C. Goyne, and J. McDaniel, "Nonequilibrium Supersonic Freestream Studied Using Coherent Anti-Stokes Raman Spectroscopy," AIAA Journal (in press)²⁵⁰



Temperature Mean, Standard Deviation





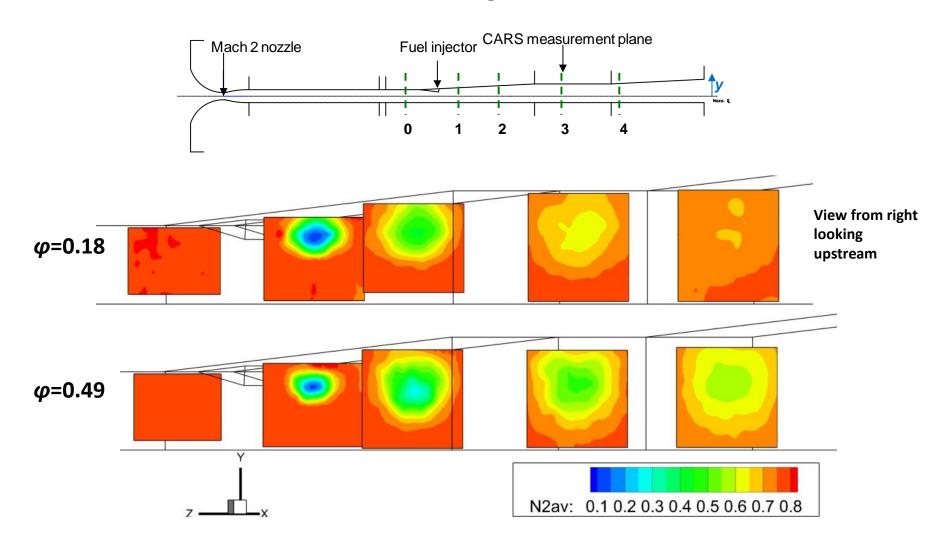
20 60 100 140 180 220 260 300 340 380 420



Contours of Mole Fraction N₂



Since inert shows overall mixing





CARS compared with CFD (LES from NC State)



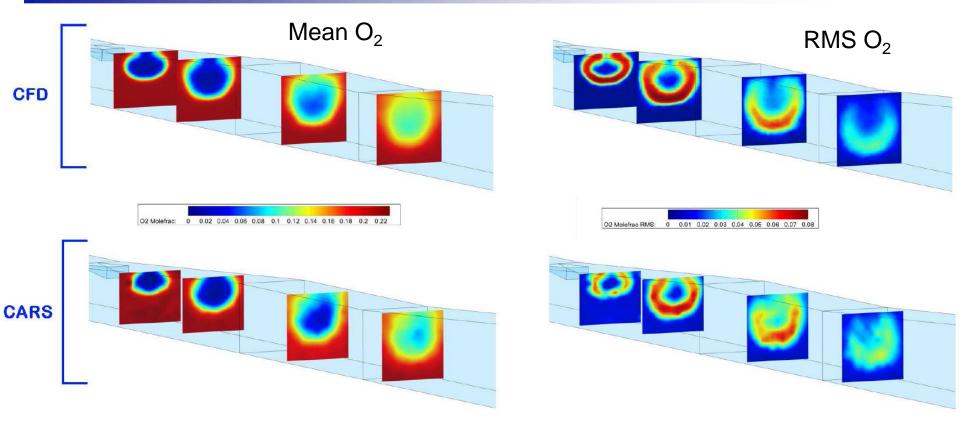


Figure 9. Comparison between CARS and O₂ concentrations and RMS fluctuations for '0.17' equivalence ratio.

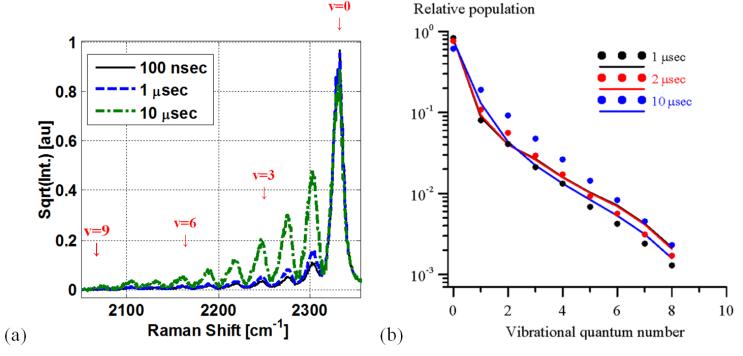
- CARS provides valuable quantitative comparison data
 - Fulton, Edwards, et al, (Configuration C) AIAA-2013-0117, 2013
 - The comparisons are not always this good!



CARS for nonthermal plasma



100 Torr pulsed discharge at Ohio State



- CARS can measure individual state populations for model validation.
- A. Montello, Z. Yin, D. Burnette, I.V. Adamovich, and W.R Lempert, "Picosecond CARS Measurements of Nitrogen Vibrational Loading and Rotational/Translational Temperature in Nonequilibrium Discharges," J. Phys. D: Appl. Phys., Sept, 2013.



Additional Thoughts on CARS



- CARS is a relatively accurate and precise hightemperature and species measurement technique in reacting and nonequilibrium flow
 - Temp. Accuracy 2-3%; Precision 2-3% (Magnotti, 2012)
- CARS can be performed through small windows or slots but need access on 2 sides.
- It is a relatively complicated technique, theoretically and experimentally, though seedless.
 - Takes months to analyze data carefully.
- Is being extended to much faster measurements ~10 kHz with fs CARS
 - Very recently: 2 beam CARS, CARS imaging (Sandia)
- Has been performed using optical fibers to deliver the laser beams, both in ns and ps regimes



Conclusion



- Variety of different molecular-based measurement technologies are available for measuring hypersonic nonequilibrium flows.
 - Can measure temperature, density, velocity, species concentrations, etc.
 - Which is best? Which technique to use?
- Must start measurement campaign with an interview of "customer" to determine the requirements
 - How do different measurement technique capabilities satisfy the requirements?



Conclusion



- Variety of different molecular-based measurement technologies are available for measuring hypersonic nonequilibrium flows.
 - Can measure temperature, density, velocity, species concentrations, etc.
 - Which is best? Which technique to use?
- Must start measurement campaign with an interview of "customer" to determine the requirements
 - How do different measurement technique capabilities satisfy the requirements?
 - Also consider practical issues:
 - Experience of the research team
 - Available equipment / budget
 - Schedule, difficulty of method, etc.
 - Rarely a perfect match, but a match can provide the data needed to advance or validate theory or computations



The interview: prior to getting started



- What parameter(s) need to be measured?
- Must multiple parameters be obtained simultaneously to determine correlations?
- What spatial resolution is required?
- Is imaging required or are single-point or line measurements sufficient?
- What temporal resolution is required? (e.g. time required for a single measurement)
- Do measurements need to be time resolved? (e.g. a continuous sequence of data)
- What accuracy is needed?
- What precision is needed?
- What quantity of data is required?
- When is the data needed? Is instant (real-time) data required?
- Where in the flow are measurements required? (inflow, exit, near walls, etc.)
- What type of optical access is available?
- Can (toxic) seed gases be introduced? Will they influence the properties being measured?
- What is the ordered priority of the above requirements?